

Contemporary Challenges in Computational Accelerator Physics



TECHNISCHE
UNIVERSITÄT
DARMSTADT

**Herbert De Gersem, Erion Gjonaj, Wolfgang Ackermann,
David Bizzozero, Wolfgang F.O. Müller, Steffen Schmid**

**Joint DESY and University of Hamburg Accelerator Physics Seminar
Hamburg, Tuesday, 7.07.2020**

**Collaboration with
Martin Dohlus, Nicoleta Baboi, Dmitry Bazyl, Yong-Chul Chae,
Ye Chen, Winfried Decking, Michael Ebert, Mikhail Krasilnikov,
Sven Pfeiffer, Holger Schlarb, Jacek Sekutowicz, Frank Stephan,
Alexey Sulimov, Rainer Wanzenberg, Igor Zagorodnov**

simulate electromagnetic fields
in accelerator components
in the presence of

- beam (charged particles)
 - ultra-relativistic, non-relativistic
 - single particles, bunches (bunch shape)
- surrounding structures
 - (complicated) geometry
 - materials (dispersive, lossy, superconducting, permeable)
 - surroundings (waveguides, couplers, (corrugated) walls, diagnostics)

Categorisation : EM Field Simulation



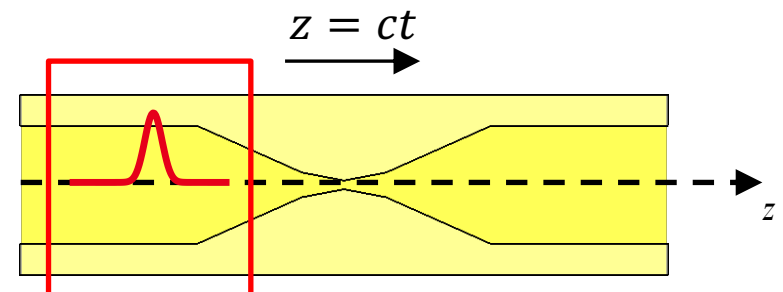
- volumetric meshes
 - structured (hexahedra)
 - unstructured (tetrahedra, possibly +pyramids +bricks)
 - meshless
- volumetric discretisation
 - finite-difference time-domain (FDTD), finite-integration technique (FIT)
 - finite-element methods (FE)
 - discontinuous Galerkin
 - particle-particle models
- discretisation in time
 - time domain
 - frequency domain
 - eigenmodes

- motivation
- categorisation
- solvers + examples
 - PBCI : e.g. wakefield simulation
 - FD : e.g. impedance simulation
 - CSRDG : e.g. coherent synchrotron radiation
 - PAMASO : e.g. pulsed waveform acceleration
 - REPTIL : e.g. tracking + space charge
 - LW : e.g. radiation in undulators
 - CEM3D : e.g. cavity simulation
- conclusions

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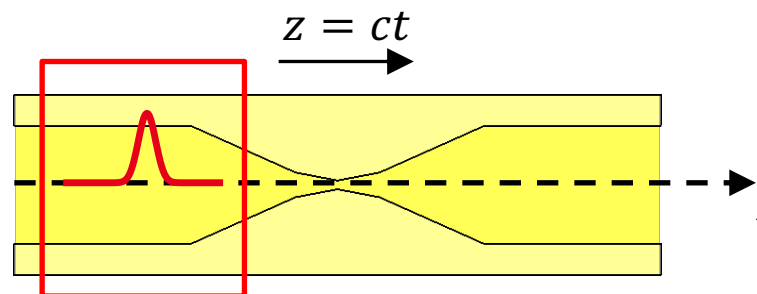
PBCI, e.g., wakefield simulation
main developer: Erion Gjonaj



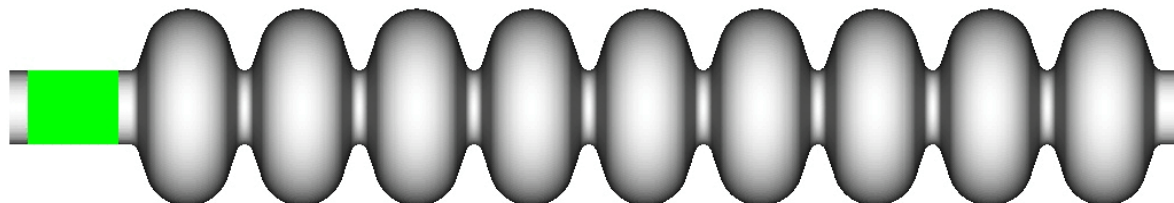
Wake field computation time domain (PBCI)

Wake fields and wake potentials

$$W_{\parallel}(r, s) = \frac{1}{Q} \int dz E_z(r, z, t(s, z))$$



- Solve Maxwell's equations in the time domain
 - Dispersion-free Finite Difference / Integration Method*
 - Indirect wake integration
 - Resistive / roughness losses by surface impedance approach
 - Very short ultra-relativistic bunches



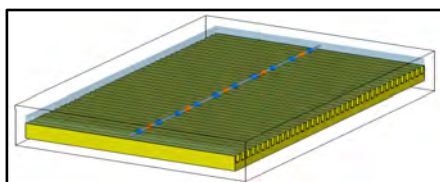
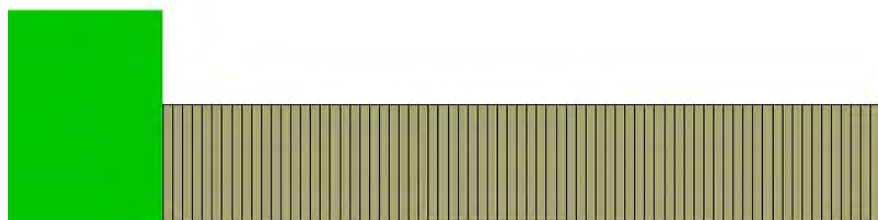
Geometric (longitudinal) wake fields in the TESLA cavity

*ICAP 2006

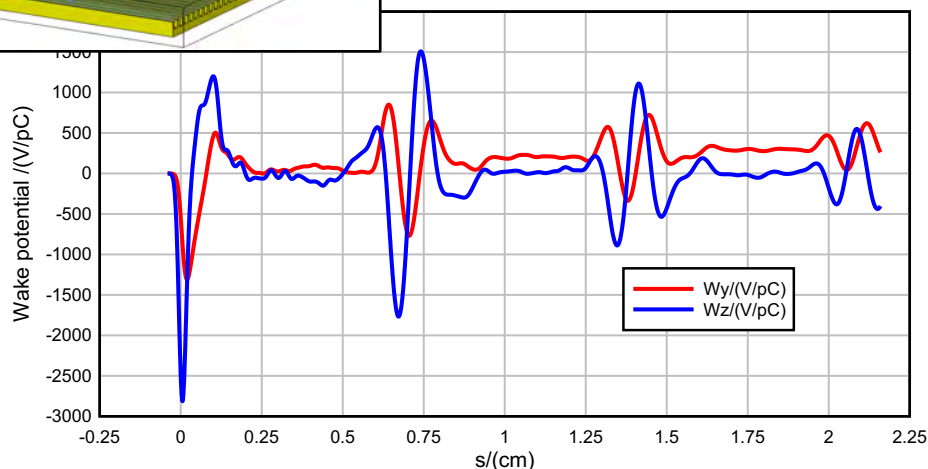
Erion Gjonaj

Wake field computation time domain (PBCI)

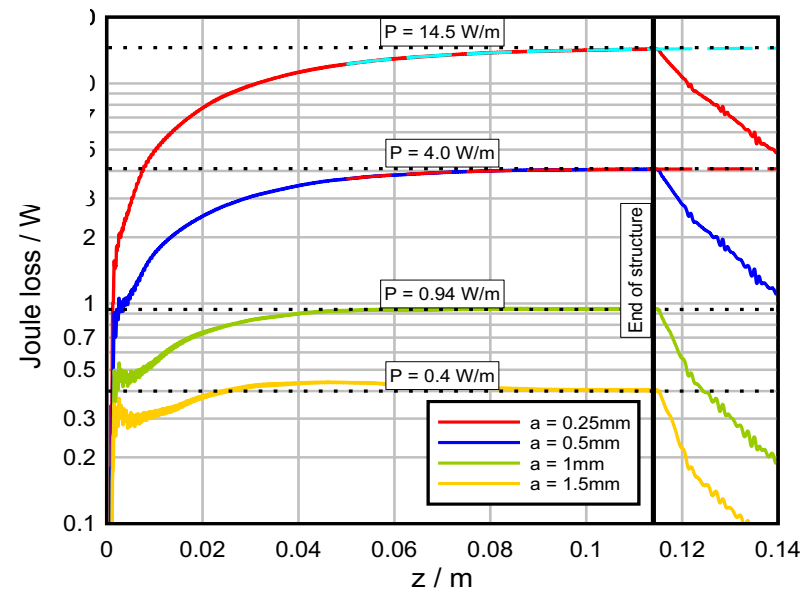
- Corrugated plate dechirper (XFEL / LCLS II)



Wake potential ($\sigma_z = 100\mu\text{m}$)



Joule losses*



Extremely long-range wake and transient heating times

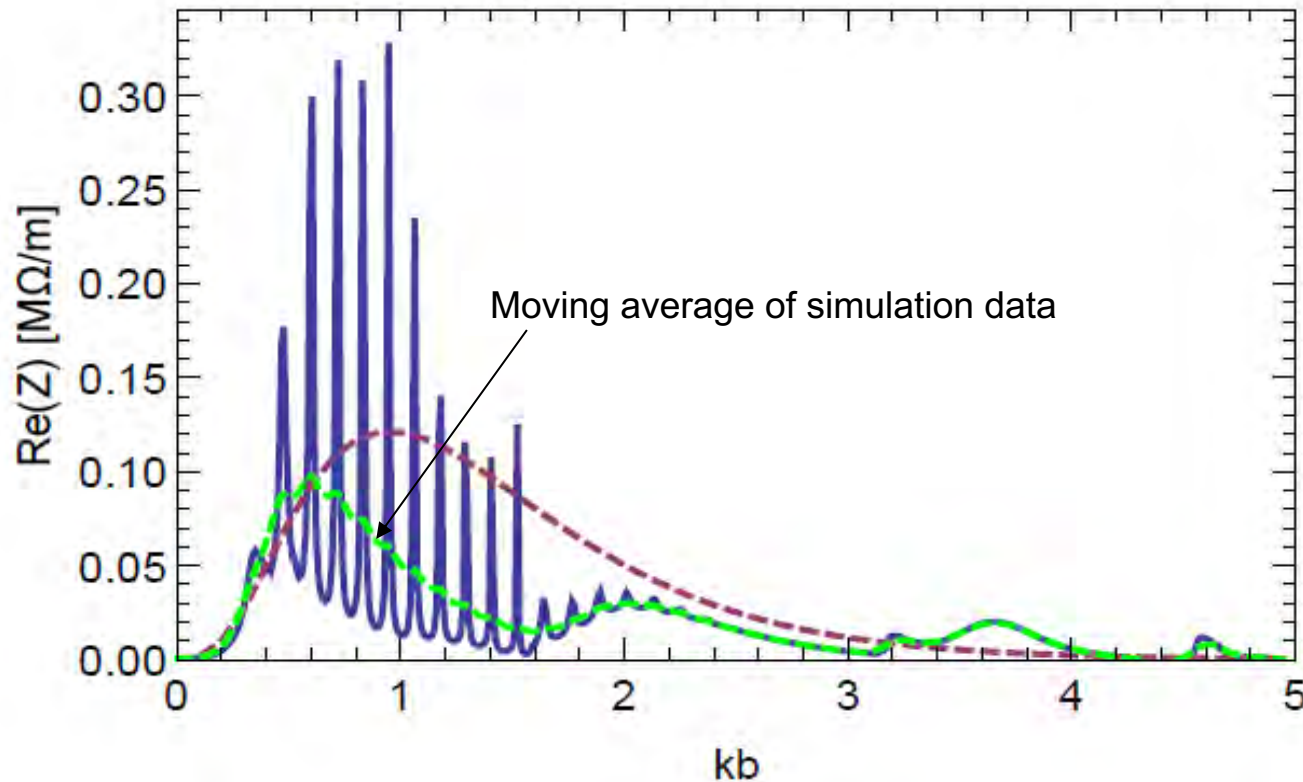
*Phys. Rev. Accel. Beams 20 (2017)

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Wake field computation time domain (PBCI)

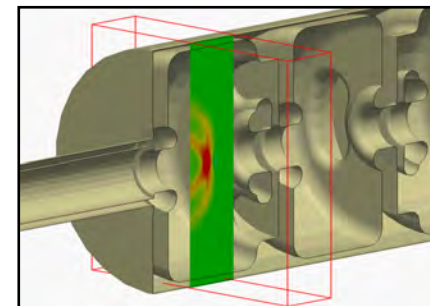
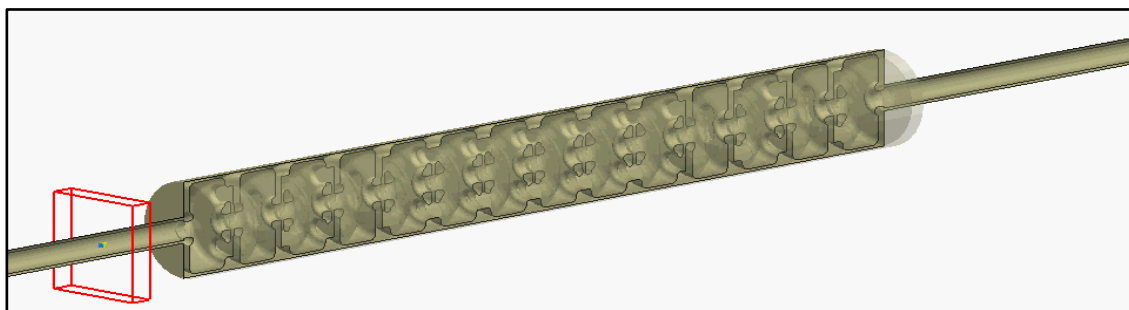
- Corrugated plate dechirper (XFEL / LCLS II)

Comparison of theory vs. simulation for longitudinal impedance ($a=1.5\text{mm}$)

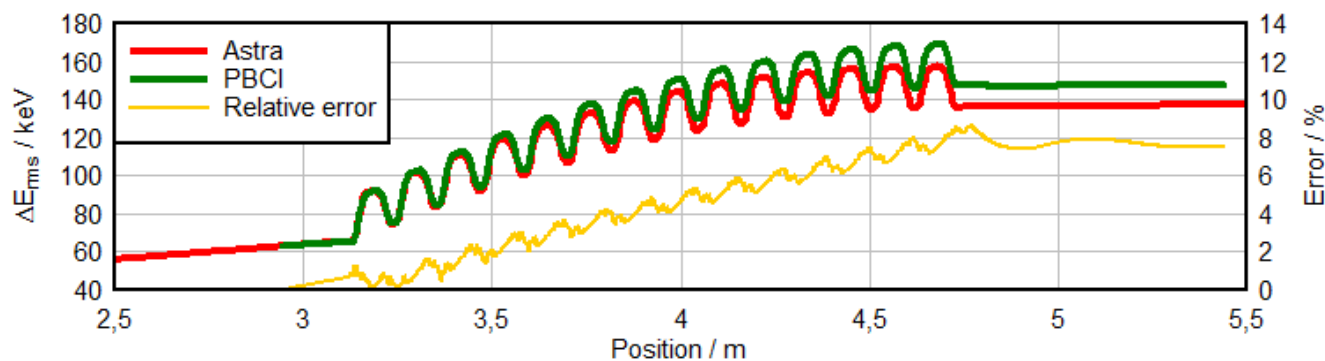


Wake field computation time domain (PBCI)

- CDS Injector Booster Cavity (DESY, PITZ)
 - Effect of wake fields on beam dynamics for soft beams



- PIC simulations with geometrical wakefields*



Energy spread:
Pure space-charge vs.
space-charge + wakefield
simulation

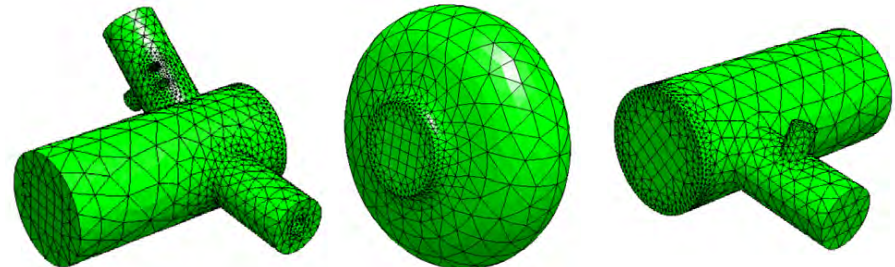
*ICAP 2012, DESY 2012

Erion Gjonaj

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FD, e.g., impedance simulation
main developer: Erion Gjonaj

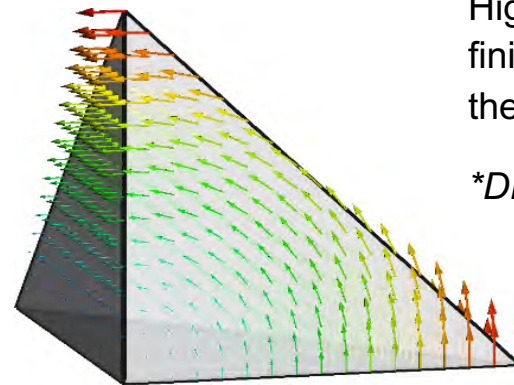


- Wake fields and impedances

$$Z_{\parallel}(r, \omega) = -\frac{1}{c\tilde{\lambda}(\omega)} \int ds W_{\parallel}(r, s) e^{-\frac{i\omega s}{c}} = -\frac{1}{Q\tilde{\lambda}(\omega)} \int dz \tilde{E}_z(r, z, \omega) e^{\frac{i\omega z}{c}}$$

- Solve Maxwell's equations in the frequency domain*

- High order conforming and hierarchic FE
- Specialized 3D-beam absorbing boundary condition
- Long range wakefields
- Arbitrary geometry
- Curved beam paths & $\beta < 1$
- Lossy wall and resistive impedance
- Hybrid meshes / charge conservation

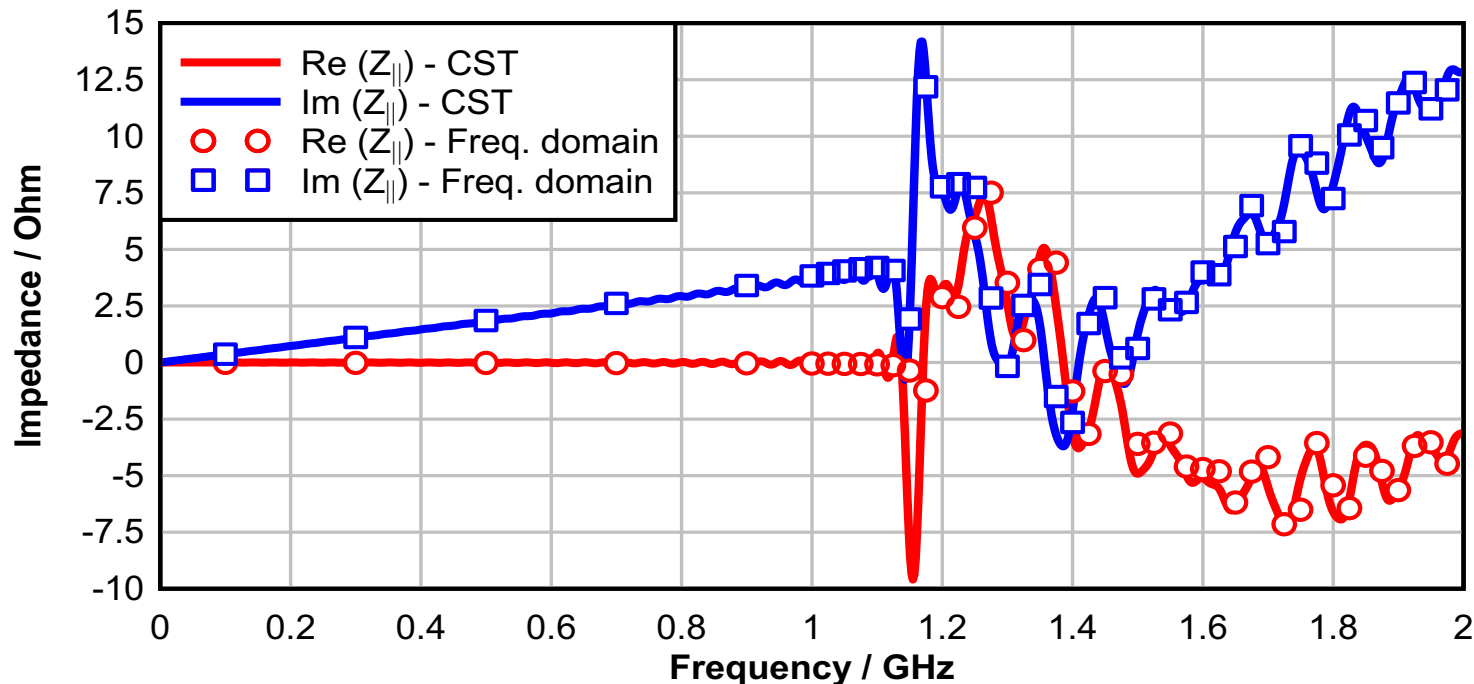
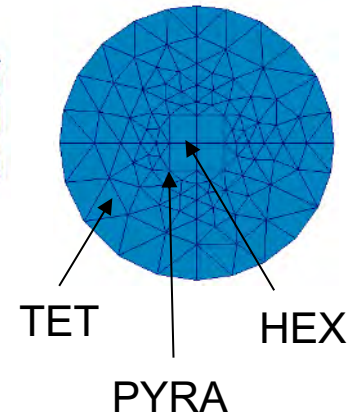
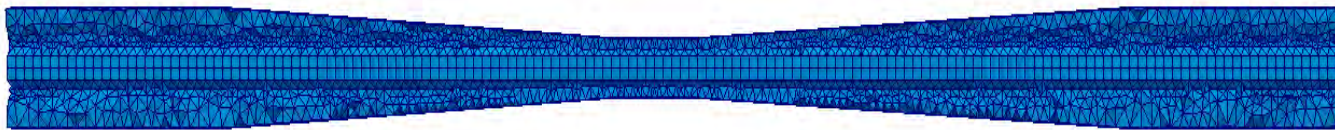


High order tangential
finite element used in
the discretization

*DESY 2019

Impedance computation frequency domain

- Tapered collimator example – hybrid meshes

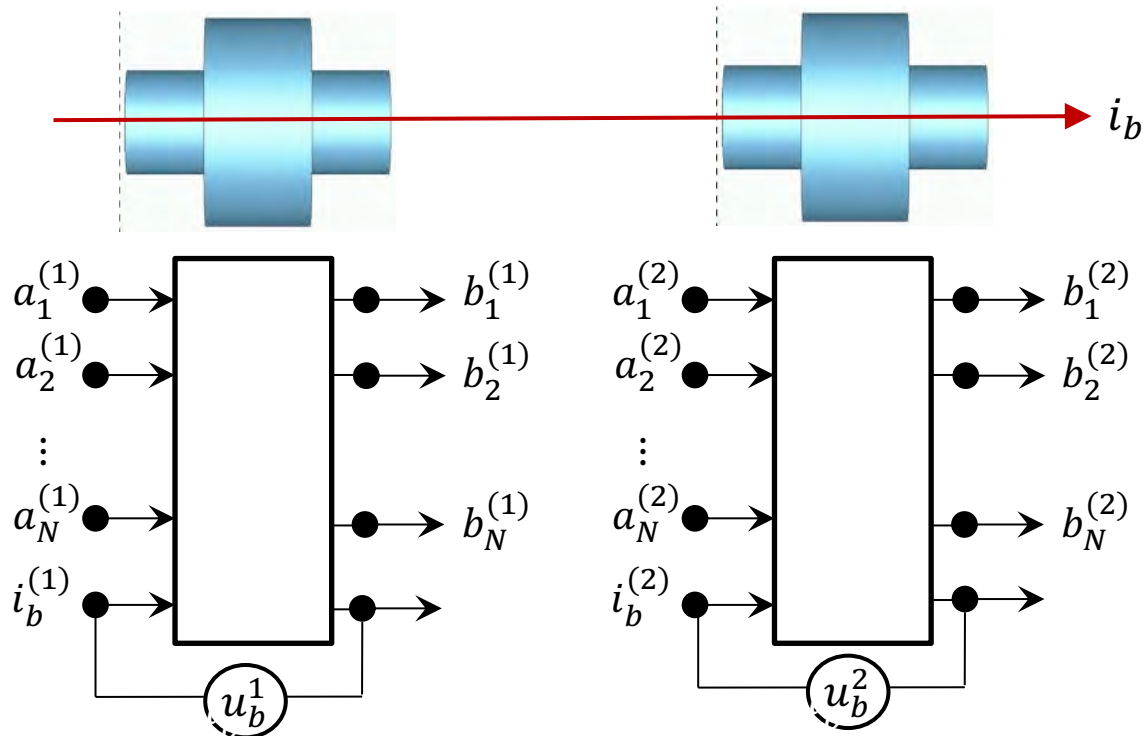


Longitudinal impedance.
Frequency domain vs. time domain

Erion Gjonaj

Impedance computation frequency domain

- Concatenation of long accelerator structures*



Matching conditions:

$$b_i^{(n)} = a_i^{(n+1)}$$

$$i_b^{(n)} = i_b^{(n-1)} e^{ik_0 L_{n-1}}$$

$$\sum_n u_b^{(n)} = u_b^{tot}$$

- Generalized S-Matrix*:

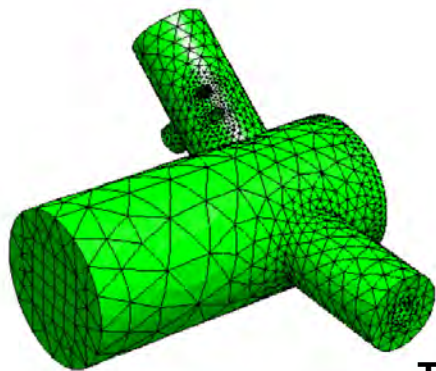
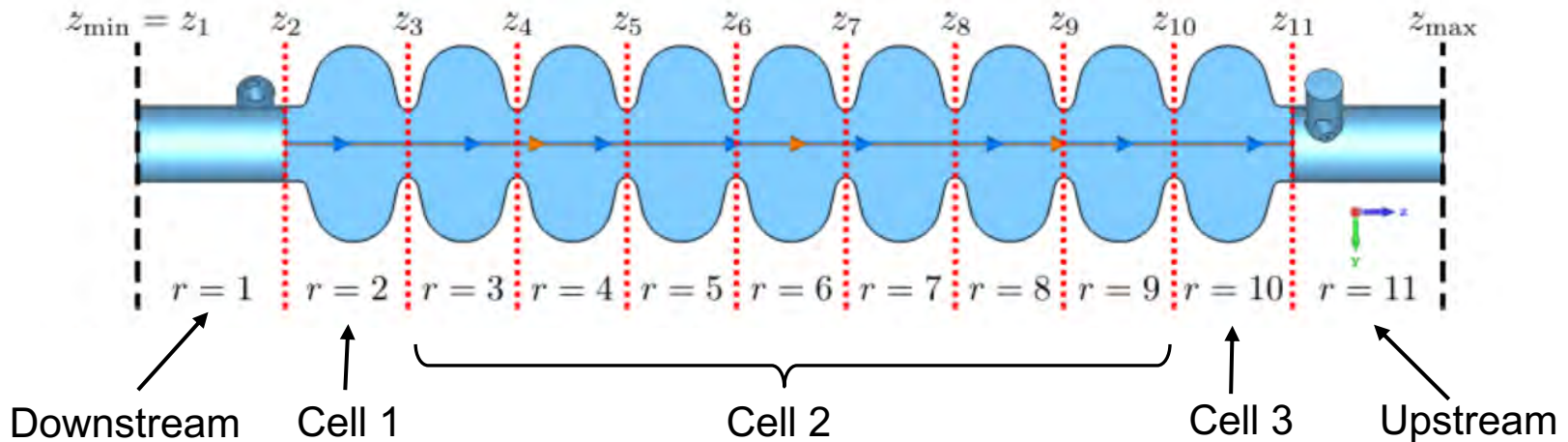
$$\begin{pmatrix} S^{tot} & k^{tot} \\ h^{tot} & Z_b^{tot} \end{pmatrix} \begin{pmatrix} a_m \\ i_b \end{pmatrix} = \begin{pmatrix} b_m \\ u_b^{tot} \end{pmatrix}$$

*Phys. Rev. Accel. Beams (2020)

Erion Gjonaj

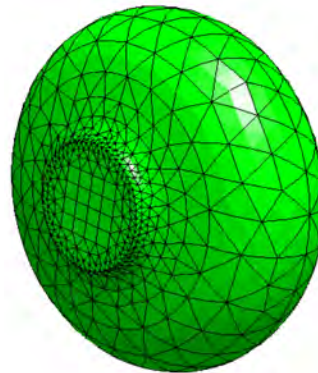
Impedance computation frequency domain

- Tesla 1.3GHz cavity

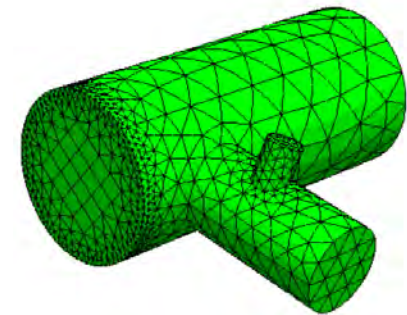


15 TE-Modes
($f_{max} = 8.2\text{GHz}$)
15 TM-Modes
($f_{max} = 10.6\text{GHz}$)

TEM, ...



15 TE-Modes
($f_{max} = 8.2\text{GHz}$)
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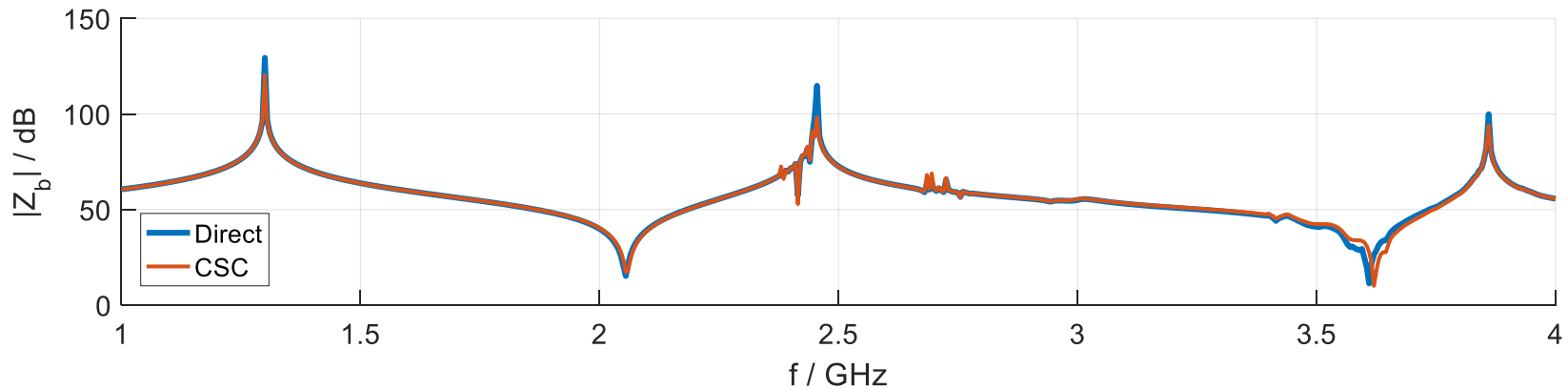


Erion Gjonaj

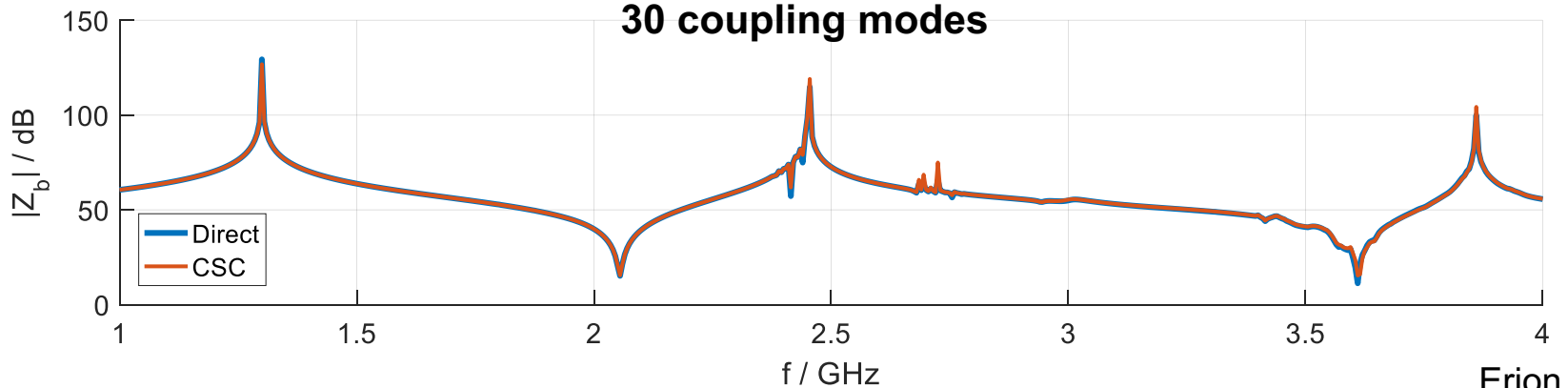
Impedance computation frequency domain

- Tesla 1.3GHz cavity

10 coupling modes



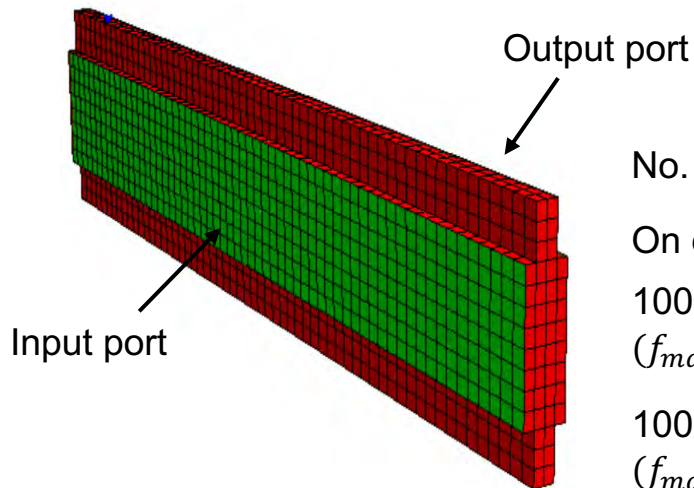
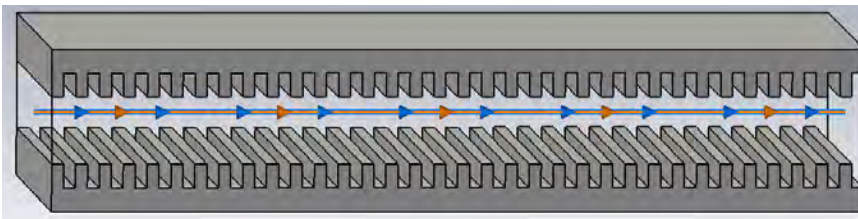
30 coupling modes



Impedance computation frequency domain

- Other applications - frequency domain impedance solver

(Quasi-) Periodic structures

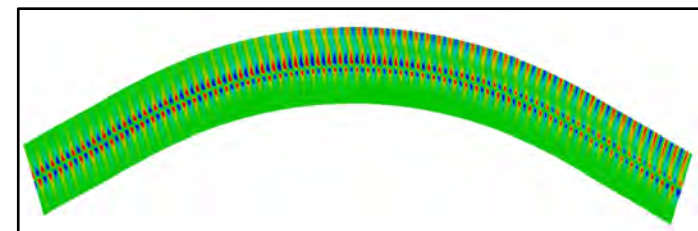
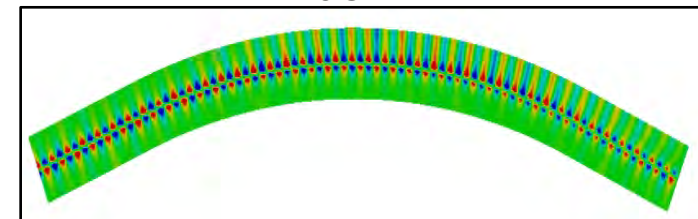
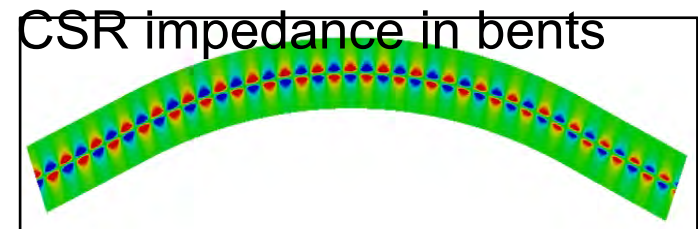


No. elements: 2640

On each port:

100 TE-Modes
($f_{max} = 375\text{GHz}$)

100 TM-Modes
($f_{max} = 448\text{GHz}$)

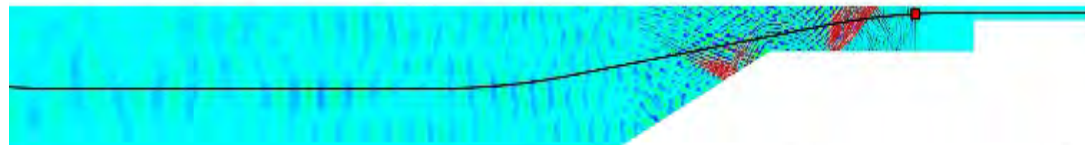


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Categorisation : EM Field Simulation

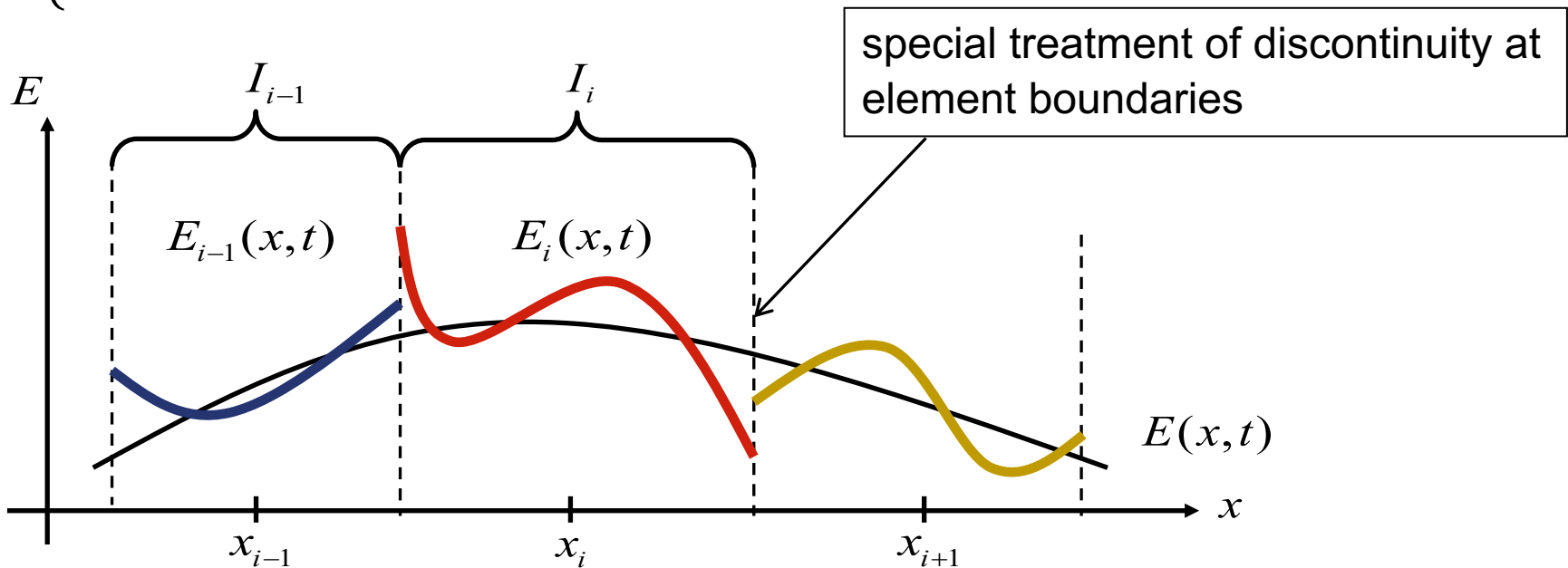
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CSRDG, e.g., simulation of
coherent synchrotron radiation
main developer: David Bizzozero



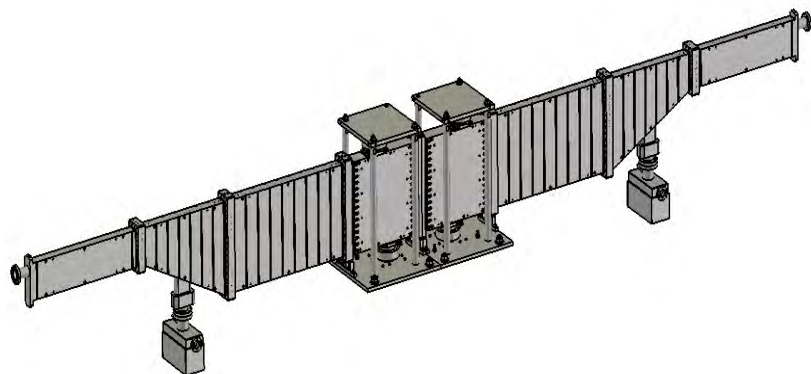
- DG discretization of Maxwell equations

$$\begin{cases} \frac{\partial \epsilon \mathbf{E}}{\partial t} - \nabla \times \mathbf{H} = -\mathbf{J} \\ \frac{\partial \mu \mathbf{H}}{\partial t} + \nabla \times \mathbf{E} = 0 \end{cases} \quad \mathbf{E} = \sum_{j,q} \mathbf{E}_{j,q}(t) \phi_{j,q}(\mathbf{r}) \quad \text{with } \phi_{j,q}(\mathbf{r}) \in P^Q(I_j)$$

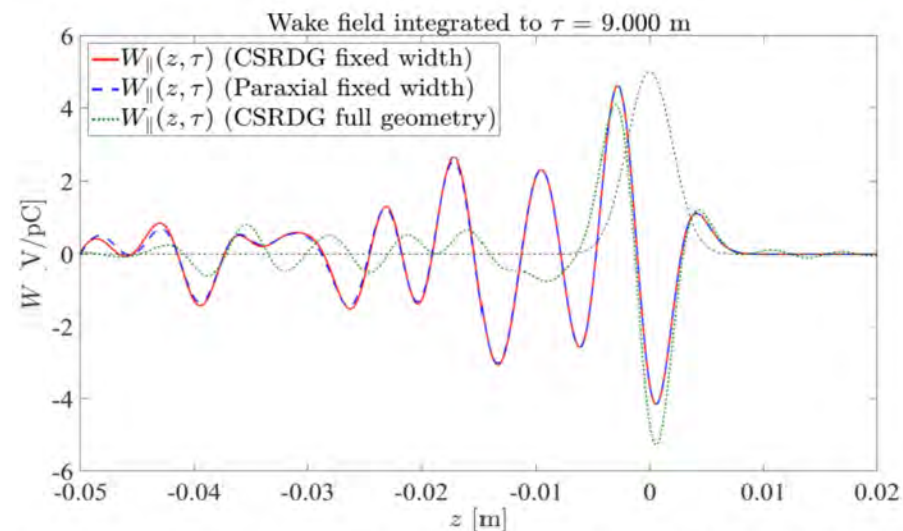
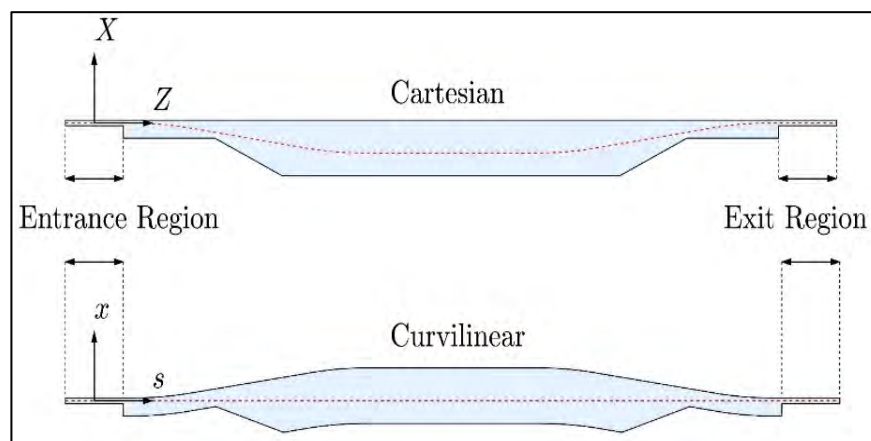


High order DGTD methods (CSR DG)

- CSR wakefields in XFEL BC0 bunch compressor*



- Transform to Frenet-Serret frame
- Parallel plate modal decomposition
- High order DG on the plane

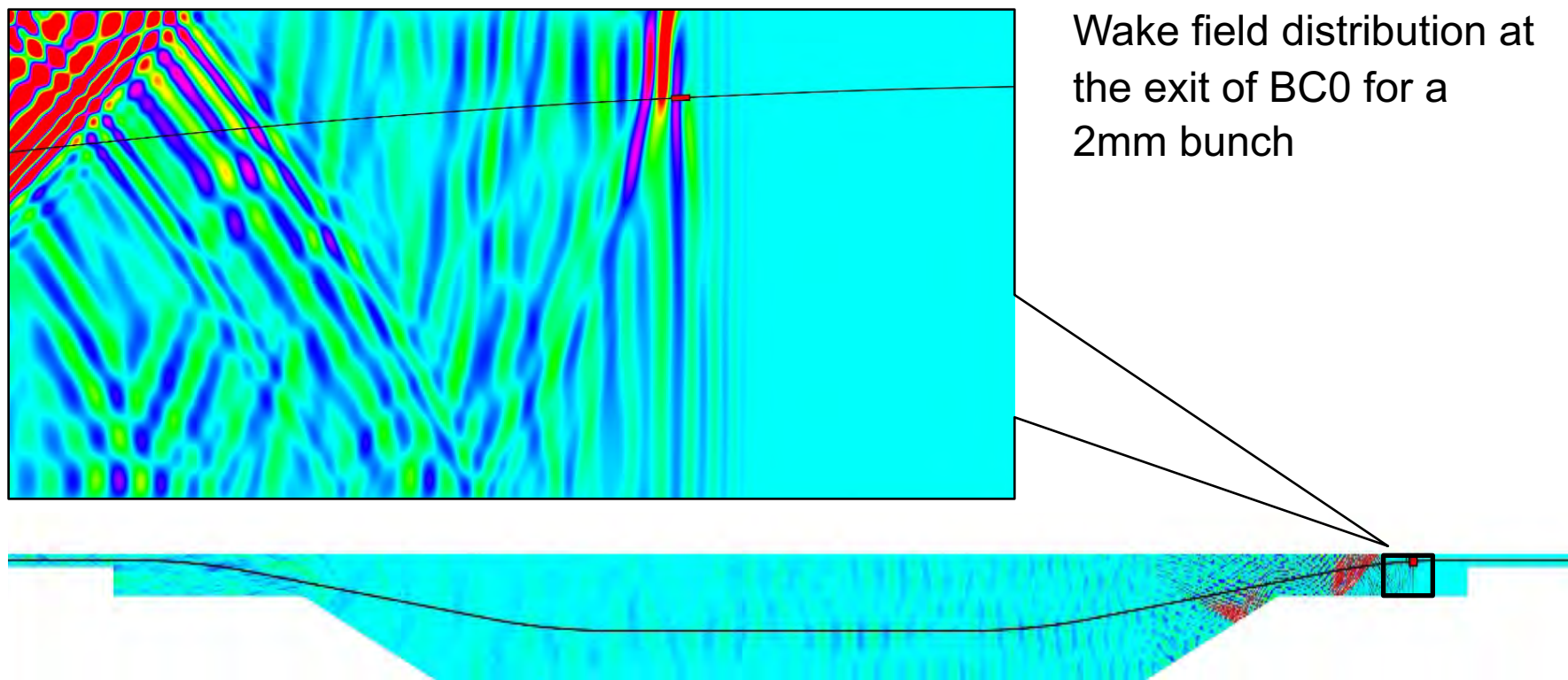


**J. Comp. Phys.* (2019)

David Bizzozero

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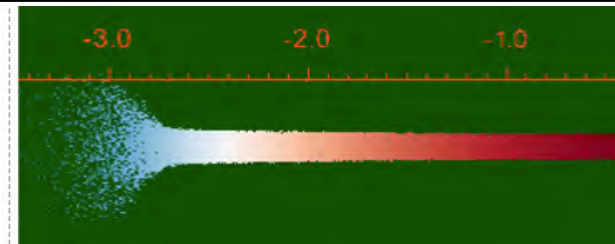
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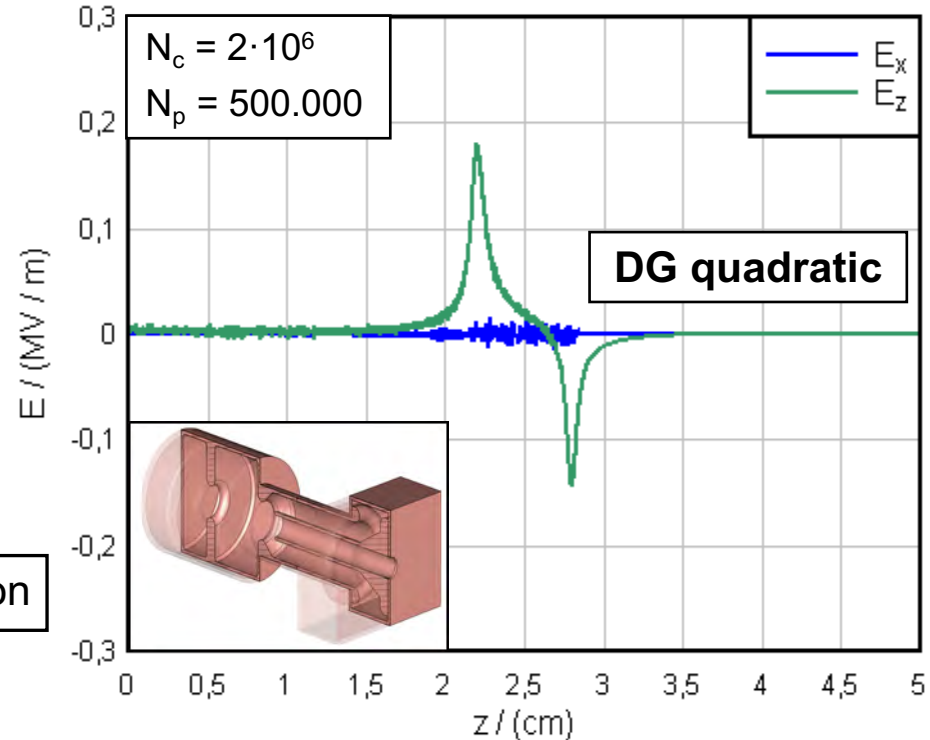
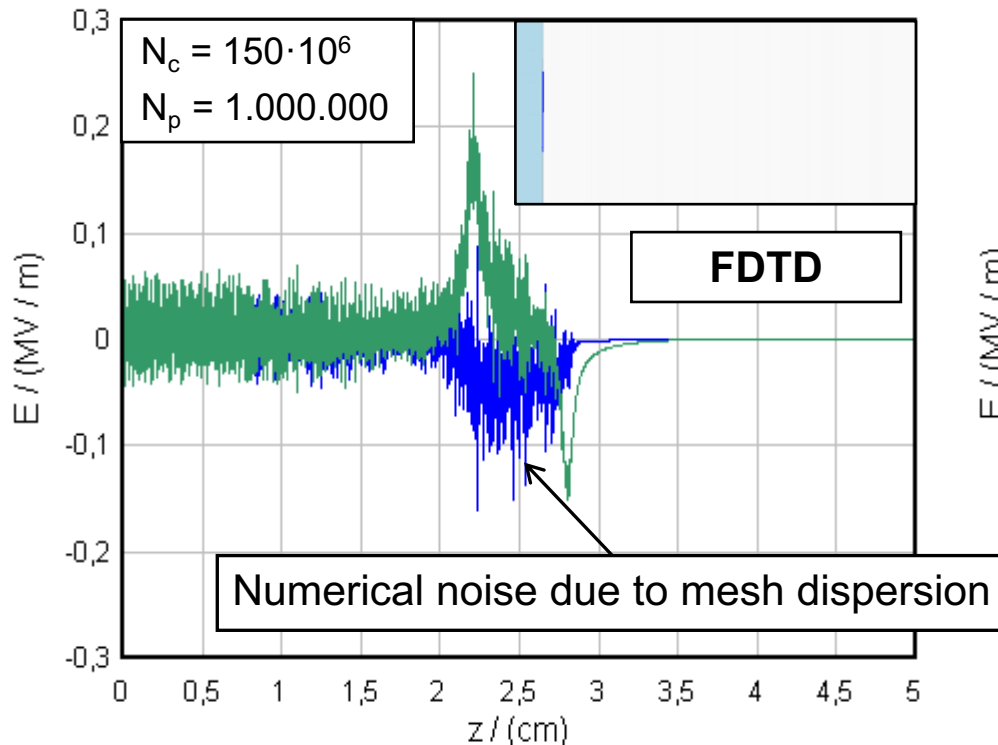
PAMASO, e.g., simulation of pulsed waveform acceleration
main developer: Erion Gjonaj



High order DGTD methods (PAMASO)

- Self-consistent beam dynamics using DG

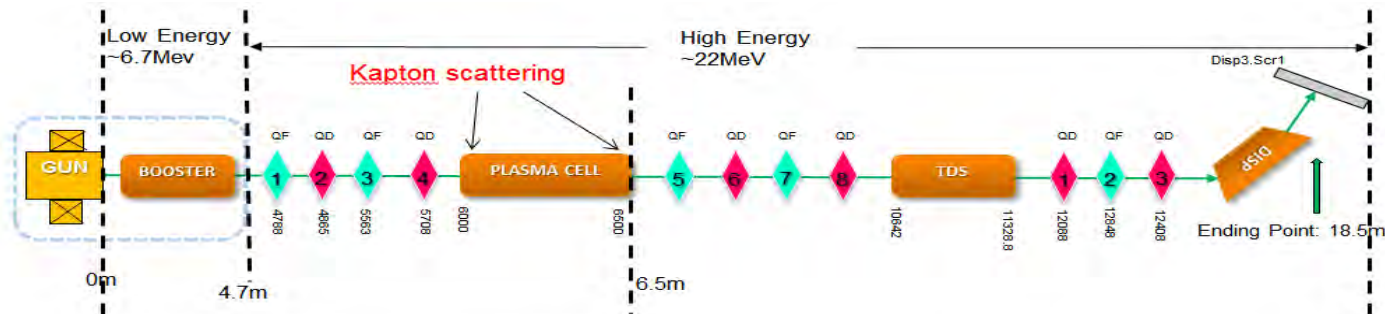
Space charge field on-axis – DESY, PITZ gun



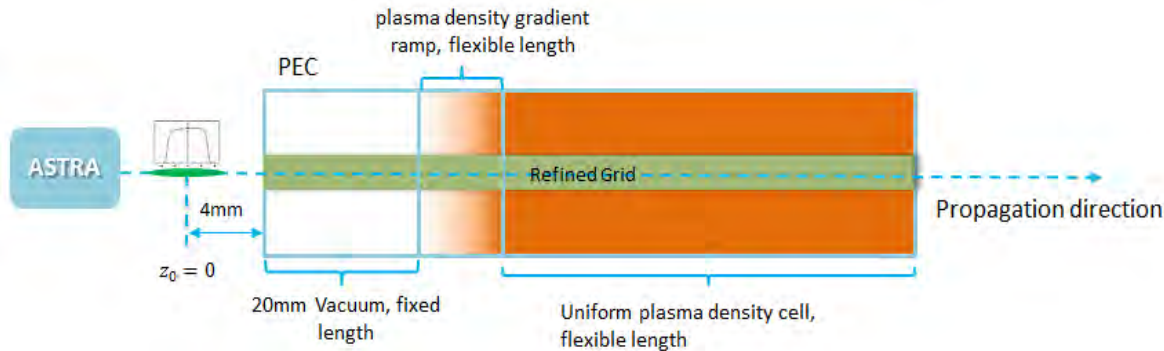
Erion Gjonaj

High order DGTD methods (PAMASO)

- Validation studies for beam driven PWFA experiments*
 - PITZ beam line with plasma cell



- Purpose: validation of the paraxial code (HiPACE) developed at DESY



PAMASO simulation setup for the transformer ratio experiment at PITZ

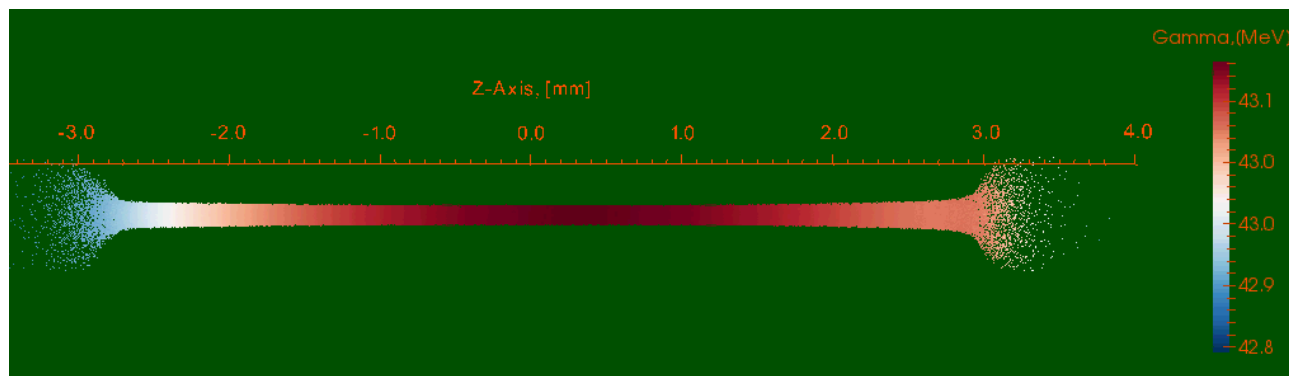
**Phys. Rev. Lett.* (2019)

High order DGTD methods (PAMASO)

- Validation studies for beam driven PWFA experiments*



Wake fields of a PITZ bunch entering the plasma cell



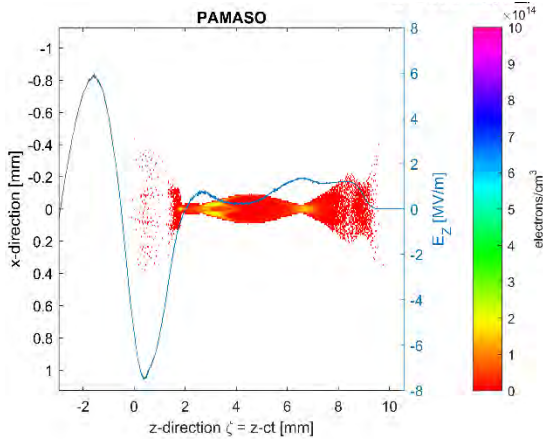
Self modulation of the bunch in the cell

with G. Loisch, Uni Hamburg

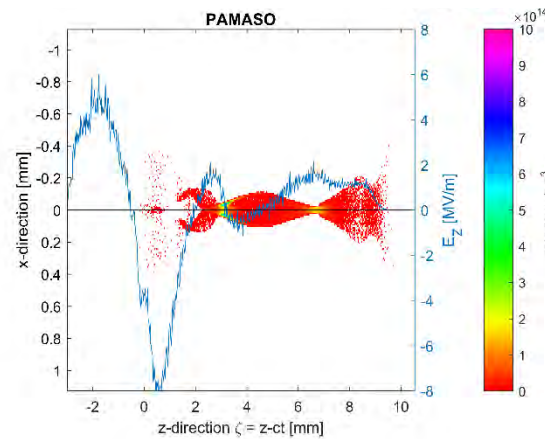
Erion Gjonaj

High order DGTD methods (PAMASO)

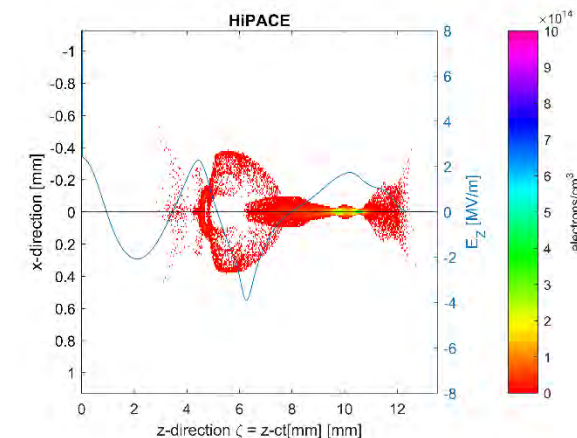
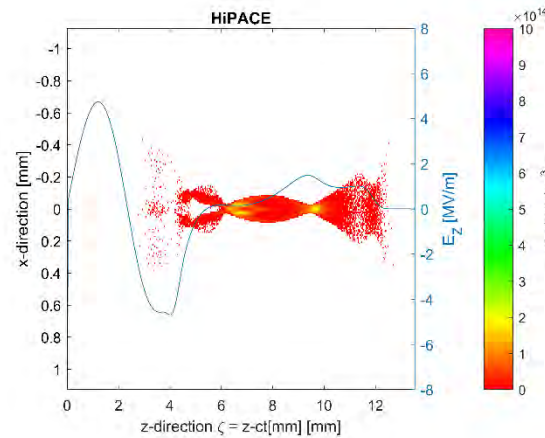
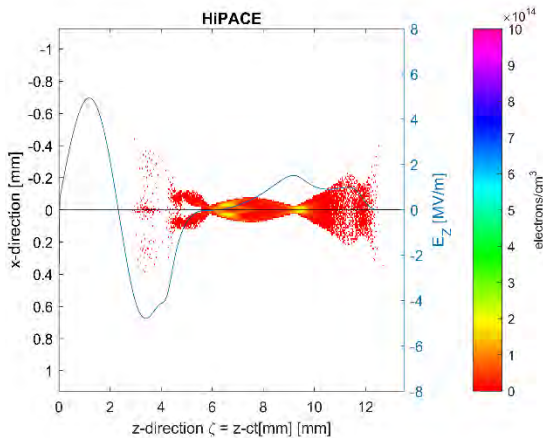
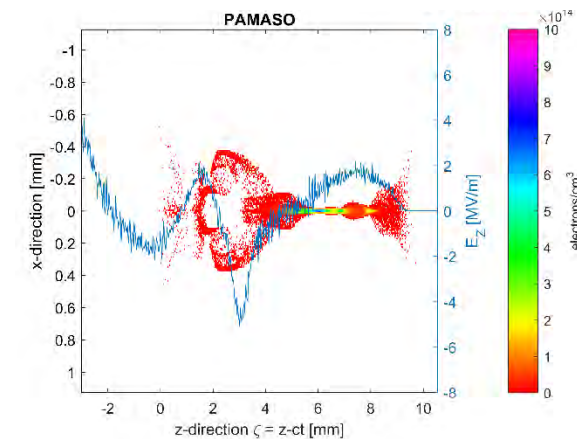
$z = 10\text{mm}$



$z = 16\text{mm}$



$z = 50\text{mm}$



Erion Gjonaj

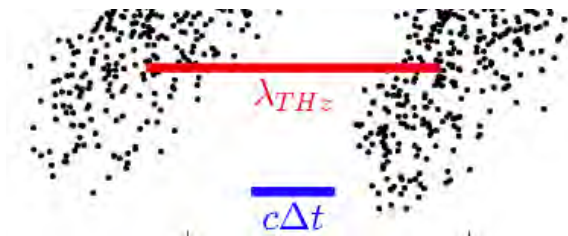
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REPTIL, e.g., tracking

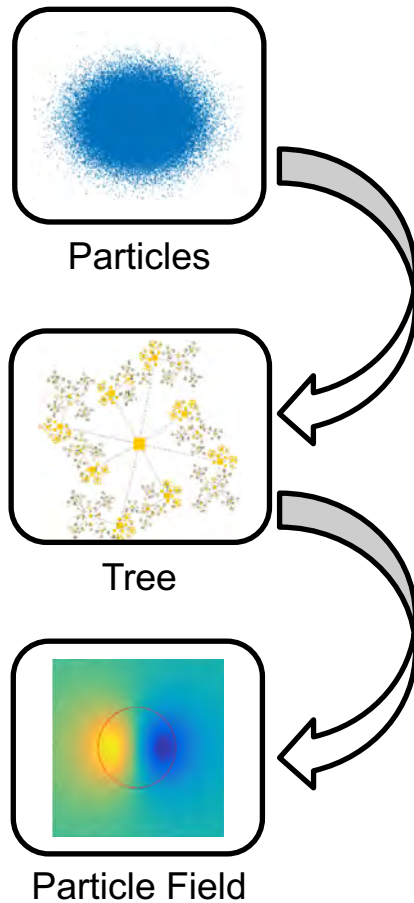
+ space charge

main developer: Erion Gjonaj



Fast Multipole Method Tracking Simulations

Adaptive FMM for sc-dominated, inhomogeneous, and anisotropic beams

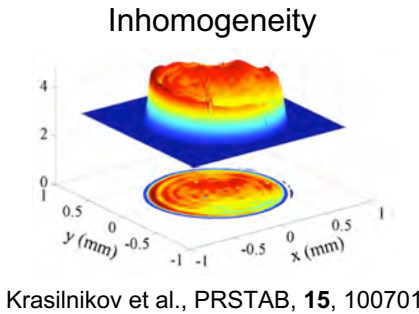


Tree Representation:

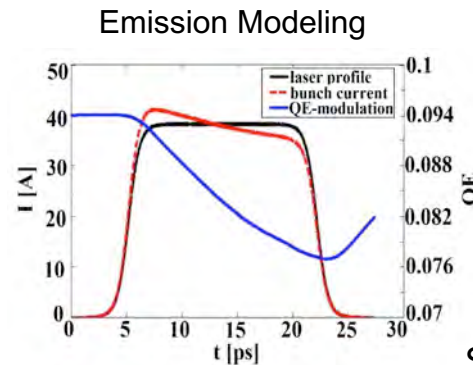
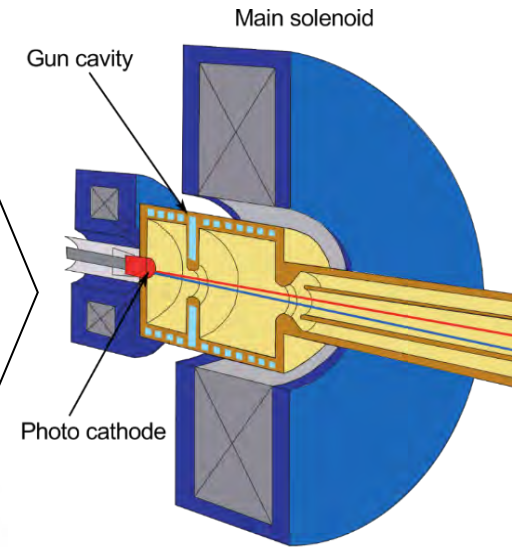
- + adaptive resolution
- + full accuracy
- + shape independent

Hierarchical Approx.:

- + $O(N)$ algorithm
- + near field accuracy
- + field resolution



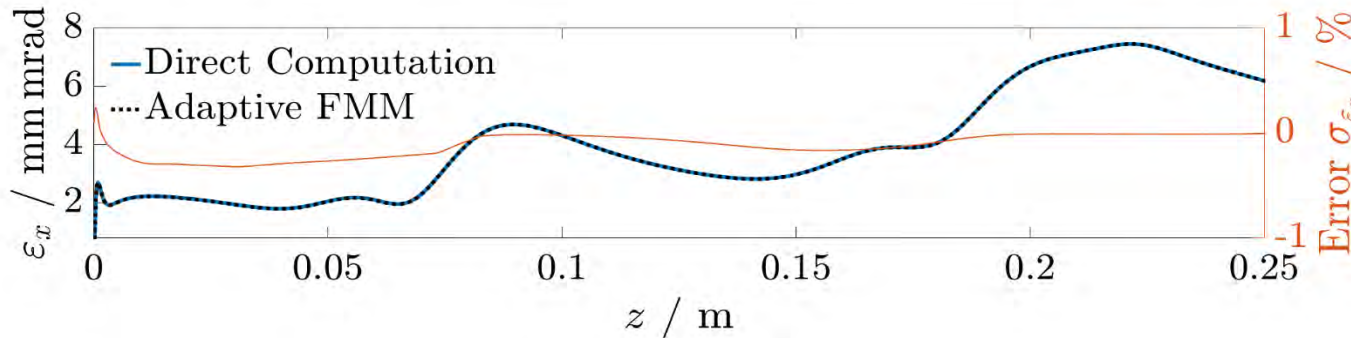
Photogun Simulations



Chen et al., NIMPR A, 889, p. 129-137
Steffen Schmid, Erion Gjonaj

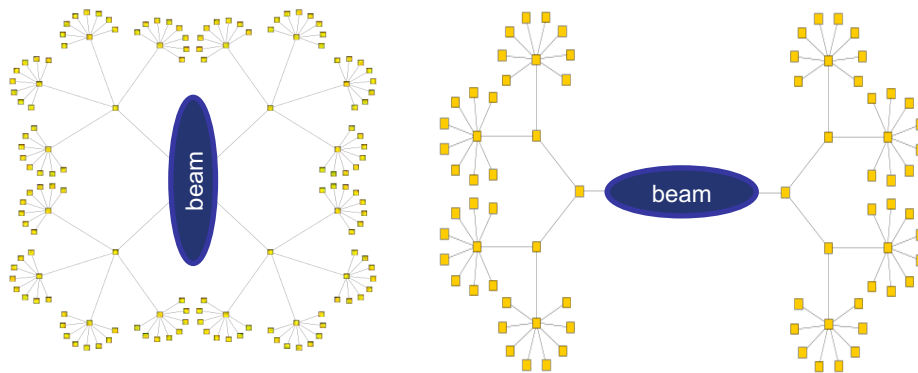
Fast Multipole Method Tracking Simulations

3D FMM Photoinjector Beam Dynamics Simulation



- relativistic, full 3D
- 40 times faster
- deviation $\sigma_{\epsilon_x} \leq 0.5\%$

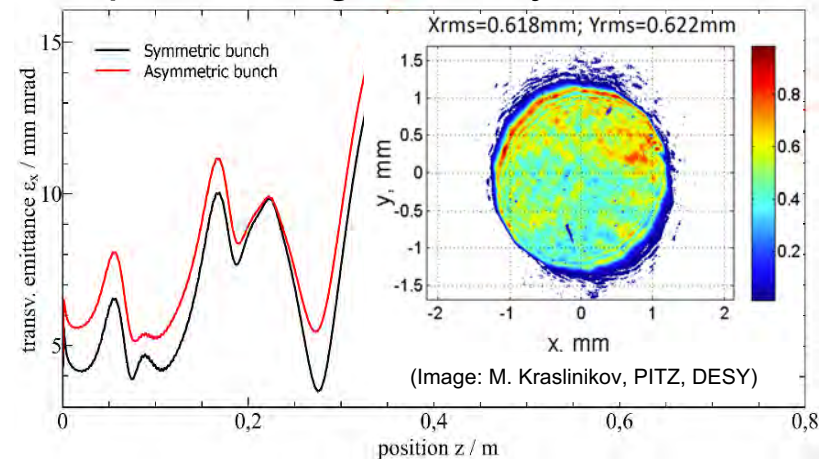
Beam Shape Optimized Tree



cathode ($\gamma \sim 1$)

gun exit ($\gamma \gg 1$)

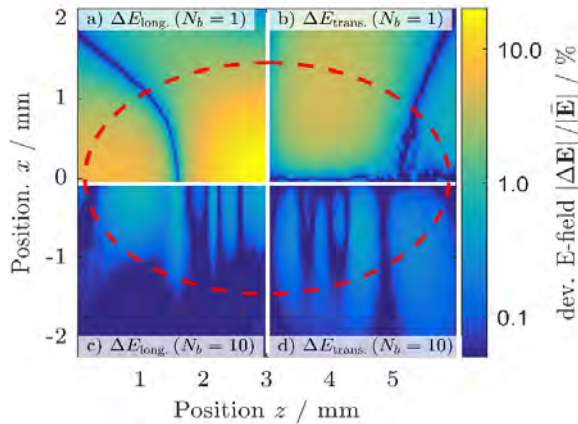
Adaptive Charge Density Resolution



Steffen Schmid, Erion Gjonaj

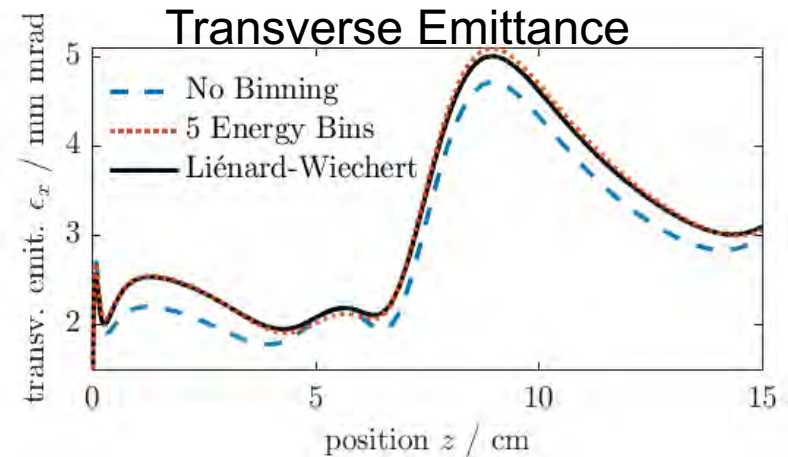
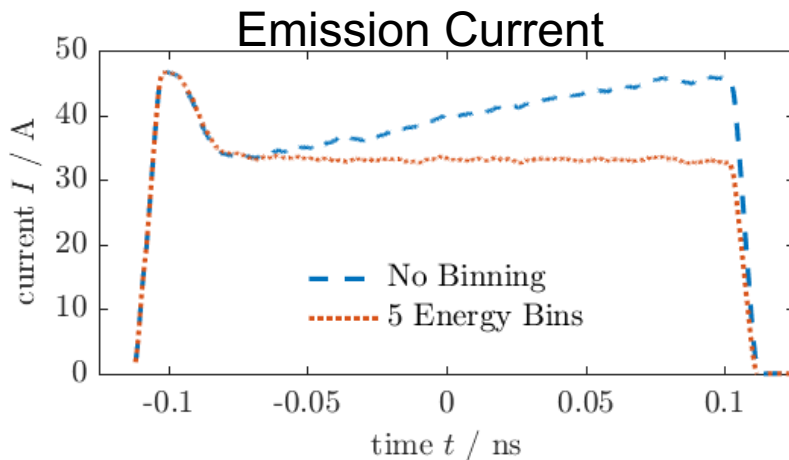
Fast Multipole Method Tracking Simulations

Space Charge Fields of Beams with Large Energy Spread



- no binning approach fields deviate by $\frac{\Delta E}{E} > 10\%$
- using 10 energy bins achieves $\frac{\Delta E}{E} \sim 0.5\%$
- $z - p_z$ phase space correlation supports FMM efficiency

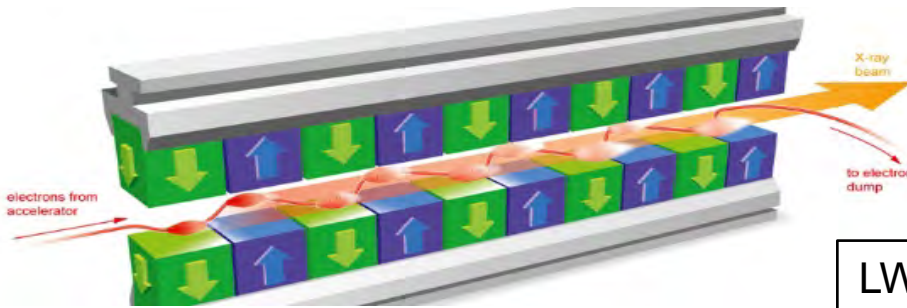
$$t_{FMM,10 \text{ bins}} \approx 2 \times t_{FMM,1 \text{ bin}}$$



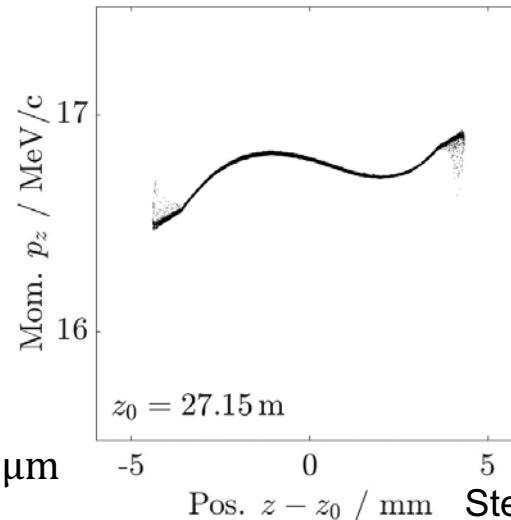
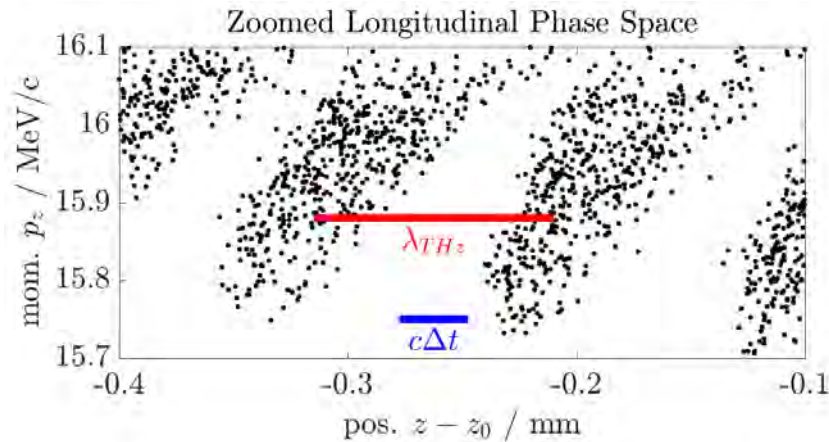
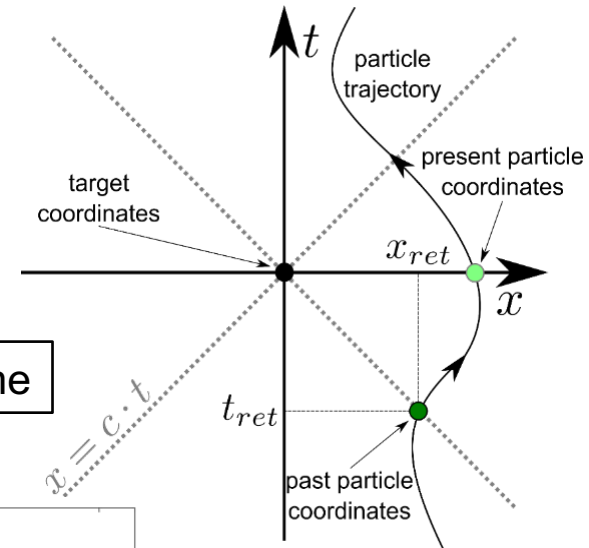
Steffen Schmid, Erion Gjonaj

Lienard-Wiechert model for radiation fields

Simulations for DESY-PITZ THz SASE-FEL



LW-Simulation scheme



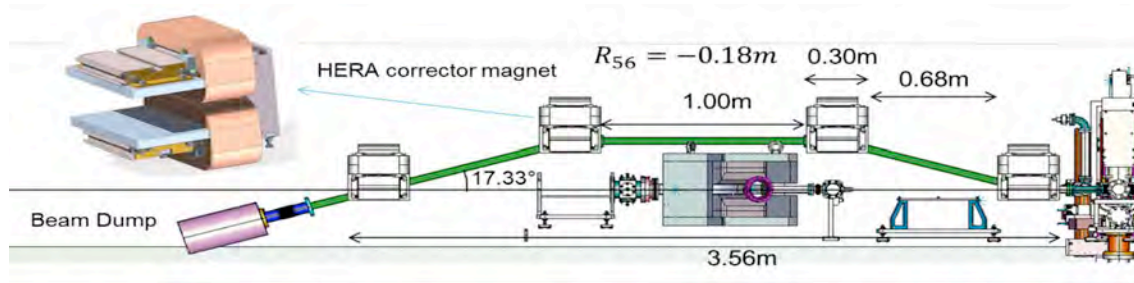
4 nC bunch
16.7 MeV energy
3.6 m undulator

Micro-bunching: $\lambda_{THz} = \frac{\lambda_U}{2\gamma^2} \left(1 + \frac{K^2}{2}\right) \approx 105 \mu\text{m}$

Steffen Schmid, Erion Gjonaj

Lienard-Wiechert model for radiation fields

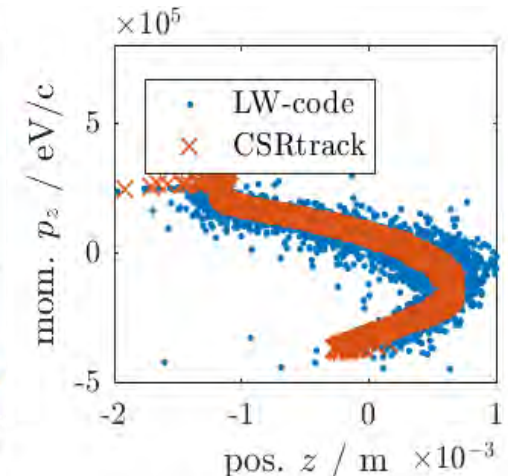
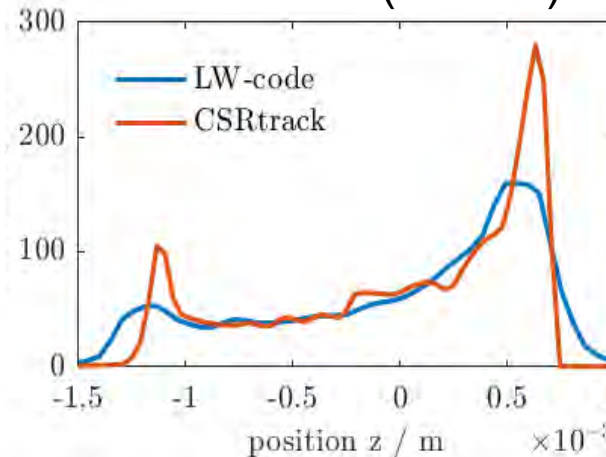
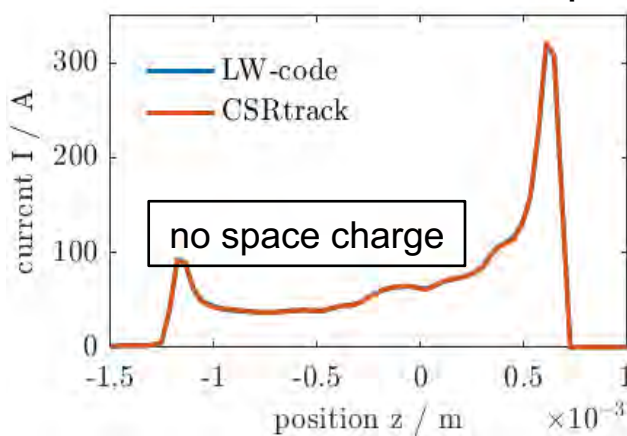
Bunch Compressor for DESY-PITZ THZ FEL



Shaker et al., FEL2019, TUP003

- $I_{peak} \approx 200A$
- $R_{56} = -0.18 m$
- $B_{dipole} \sim 50 mT$

Comparison with CSRTrack (Dohlus)

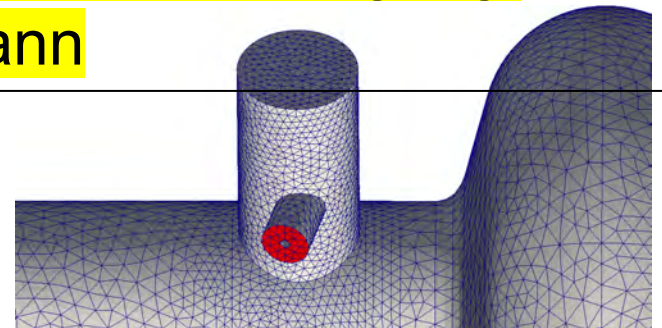


Steffen Schmid, Erion Gjonaj

Categorisation : EM Field Simulation

- volumetric meshes
 - structured (hexahedra)
 - unstructured (tetrahedra, possibly +pyramids +bricks)
 - meshless
- volumetric discretisation
 - finite-difference time-domain (FDTD), finite-integration technique (FIT)
 - finite-element methods (FE)
 - discontinuous Galerkin
 - particle-particle models
- discretisation in time
 - time domain
 - frequency domain
 - eigenmodes

CEM3D, e.g., cavity simulation
main developer: Wolfgang
Ackermann



3D FE Eigenmode Solver (CEM3D)

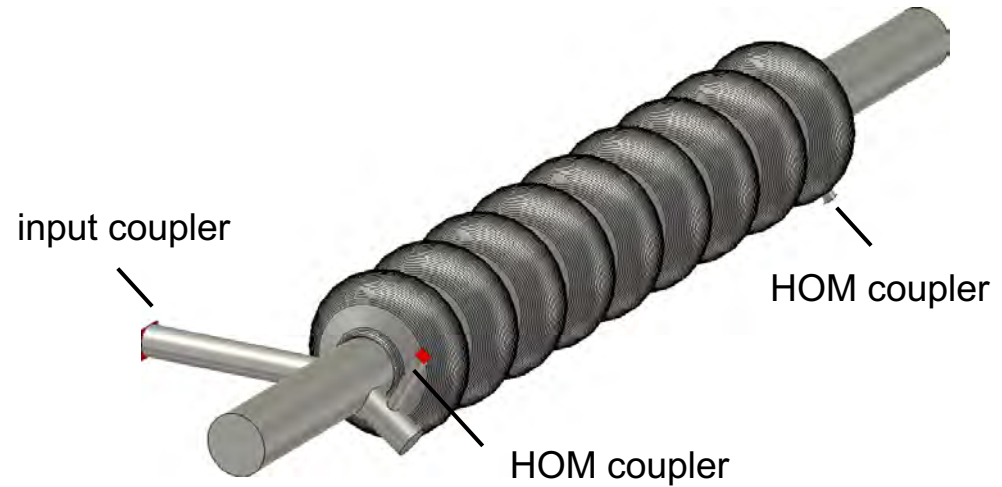
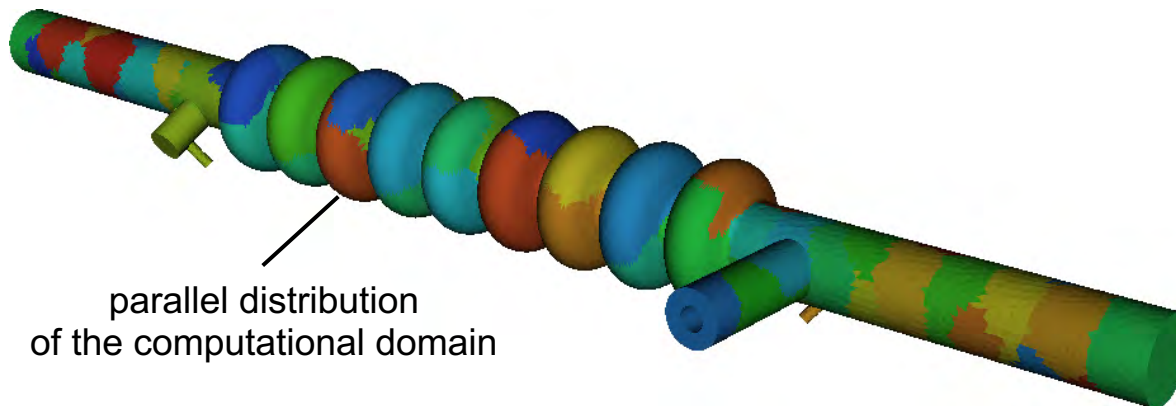
formulation

$$\text{curl } 1/\mu_r \text{ curl } \vec{E} = \left(\frac{\omega}{c_0}\right)^2 \epsilon_r \vec{E} \Big|_{\vec{r} \in \Omega}$$

continuous eigenvalue problem

$$A\vec{\alpha} + j\frac{\omega}{c_0}C\vec{\alpha} + \left(j\frac{\omega}{c_0}\right)^2B\vec{\alpha} = 0$$

discrete eigenvalue problem



domain #1 →
domain #2 →
⋮
domain #n →

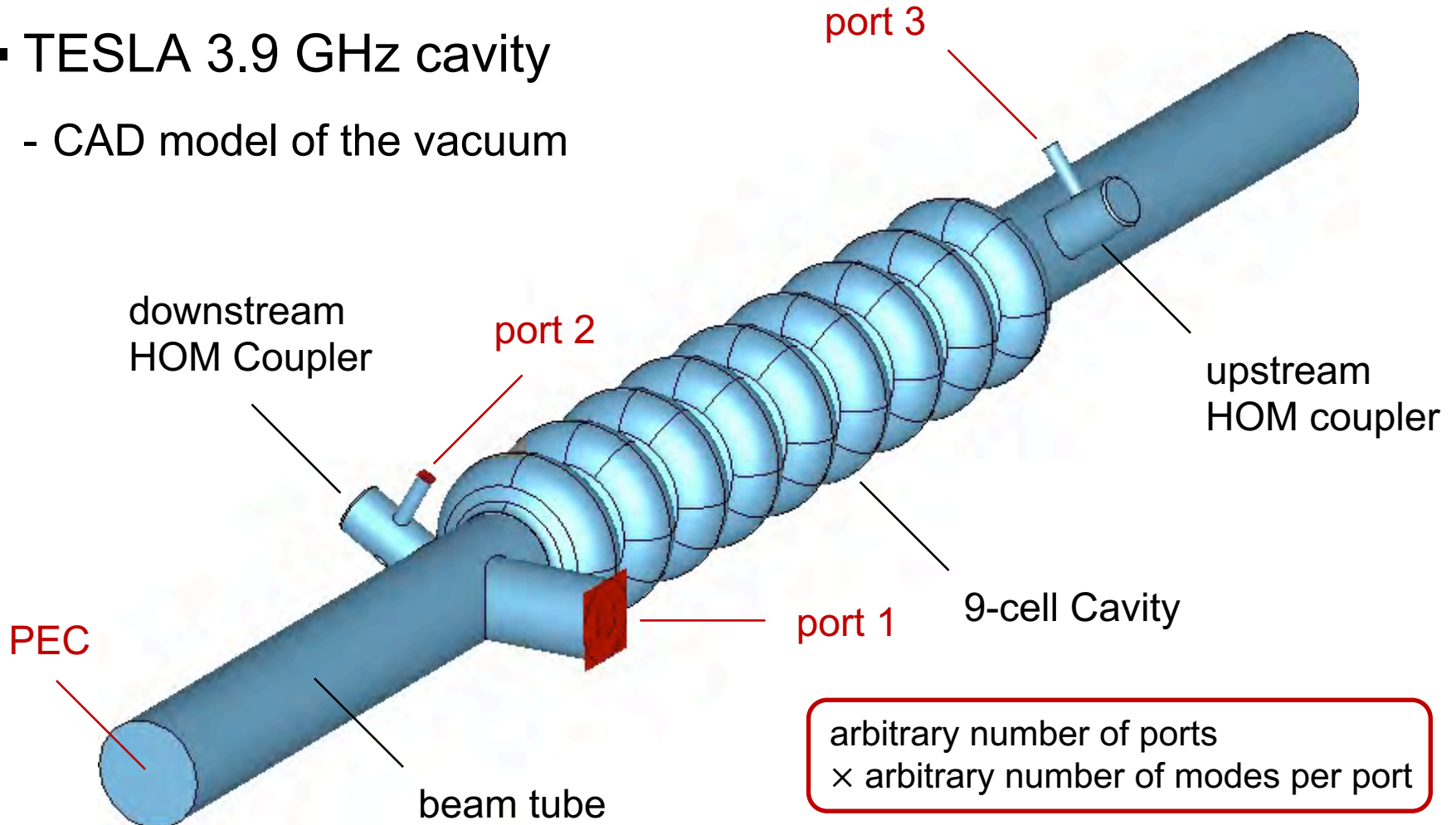


parallel computing

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TESLA Resonators

- TESLA 3.9 GHz cavity
 - CAD model of the vacuum

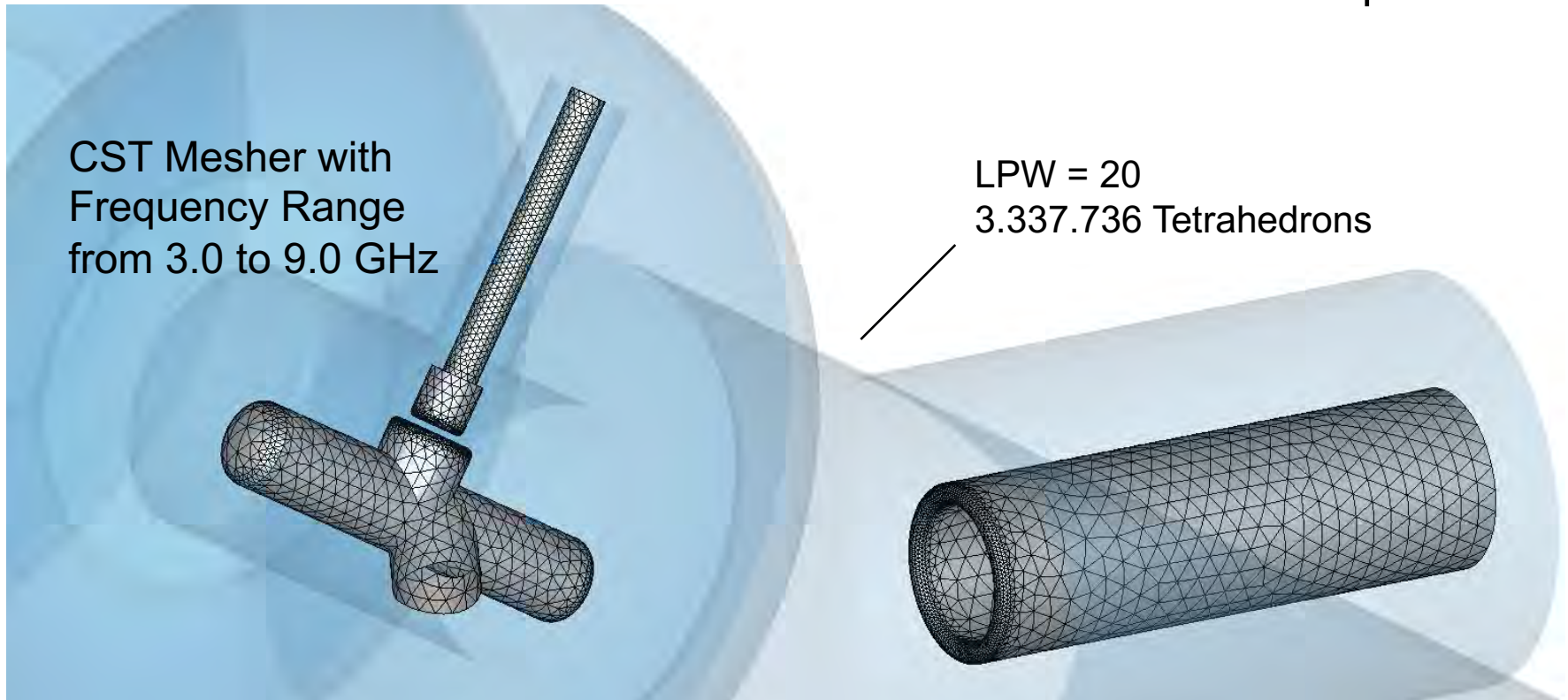


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TESLA Resonators

- TESLA 3.9 GHz Cavity

- CAD Model of the Vacuum with surface mesh on the PEC couplers



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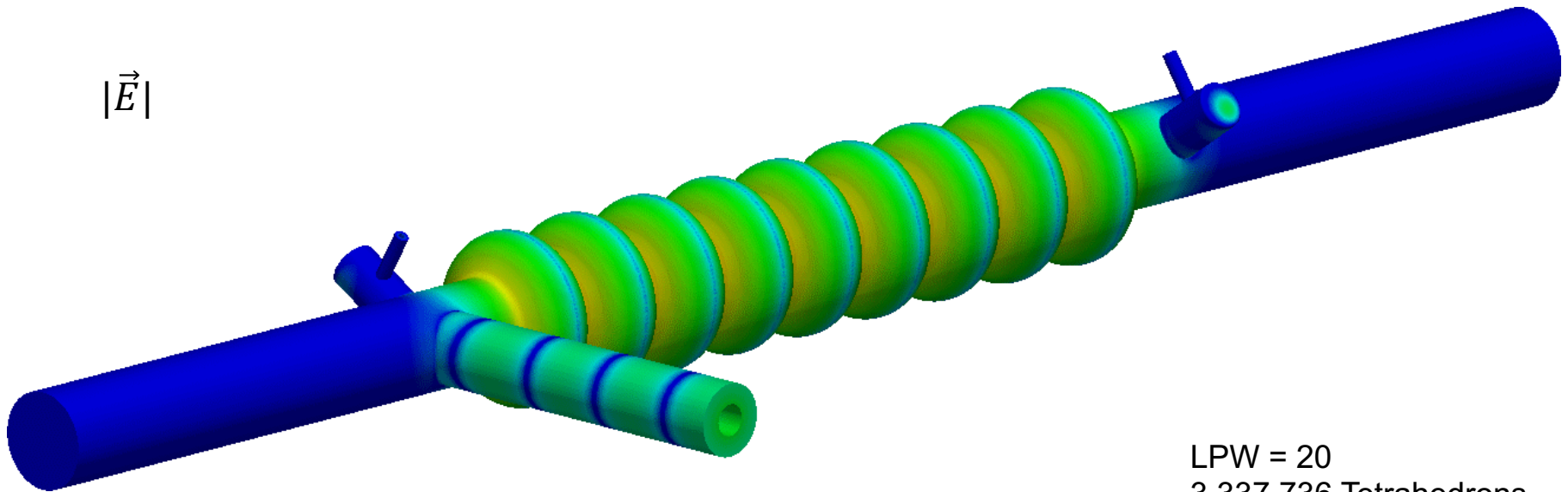
TESLA Resonators

- TESLA 3.9 GHz Cavity

- Fundamental mode

Absolute value of the electric field strength

$|\vec{E}|$



LPW = 20
3.337.736 Tetrahedrons

Logarithmic scale from 1e4 to 1e7 V/m

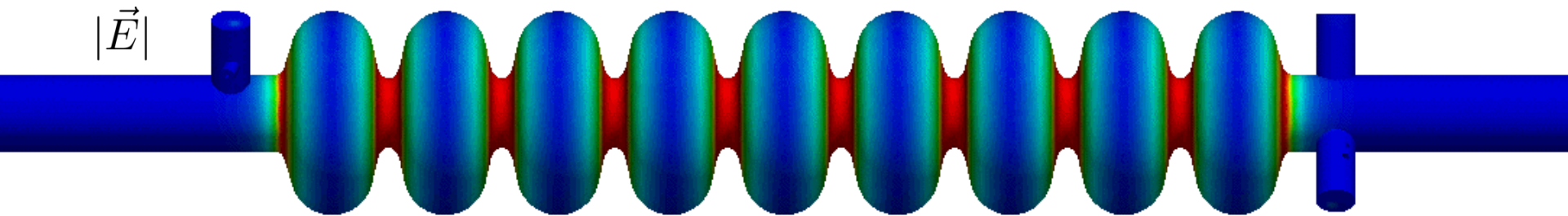
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TESLA Resonators

Simulation results

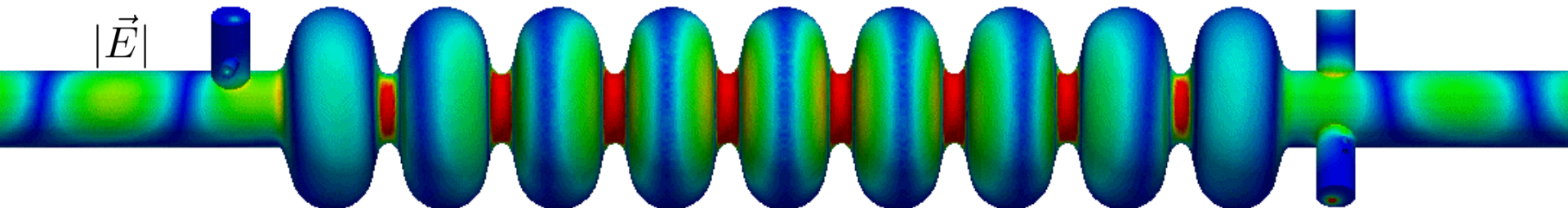
- Accelerating mode (monopole #9)

$$f_{\text{res}} = 1.300 \text{ GHz}$$
$$Q_{\text{ext}} = 2.8 \cdot 10^6$$



- Higher-order mode (dipole #37)

$$f_{\text{res}} = 2.476 \text{ GHz}$$
$$Q_{\text{ext}} = 1.8 \cdot 10^3$$

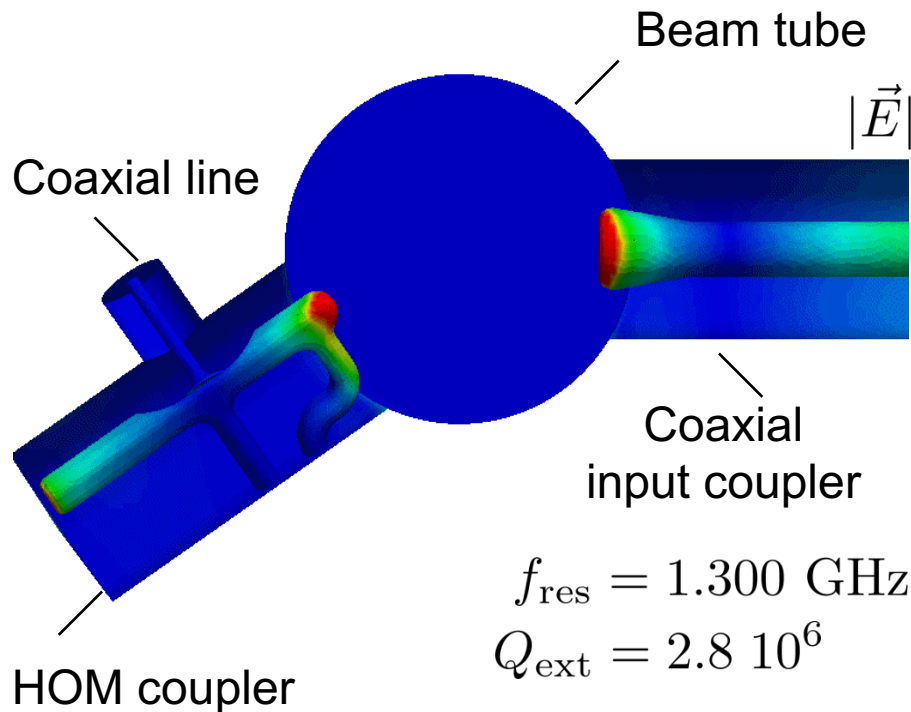


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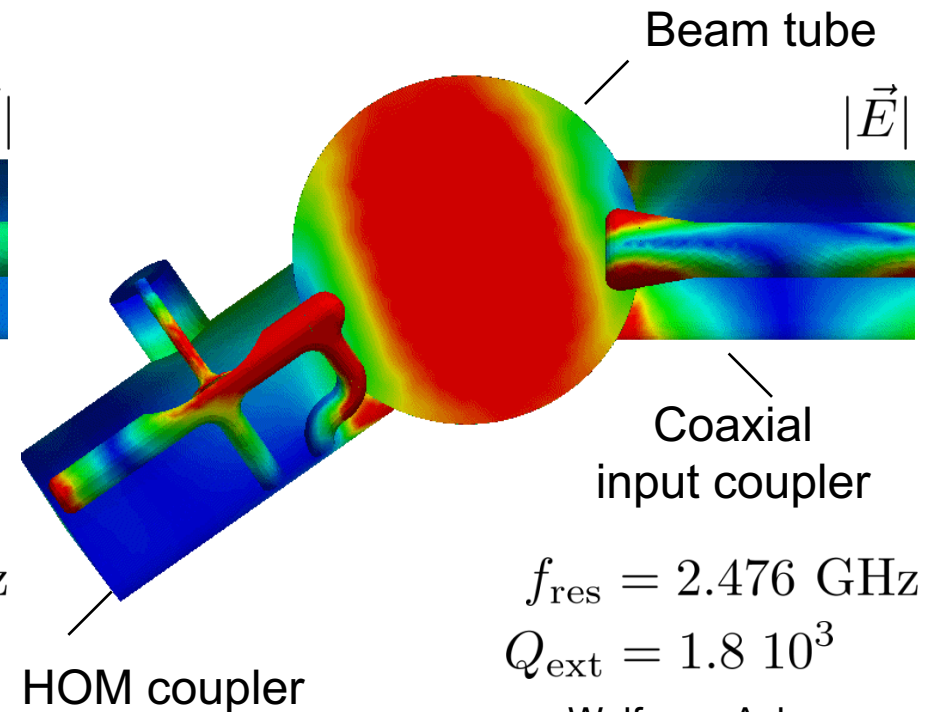
TESLA Resonators

Simulation results

Accelerating mode
(monopole #9)



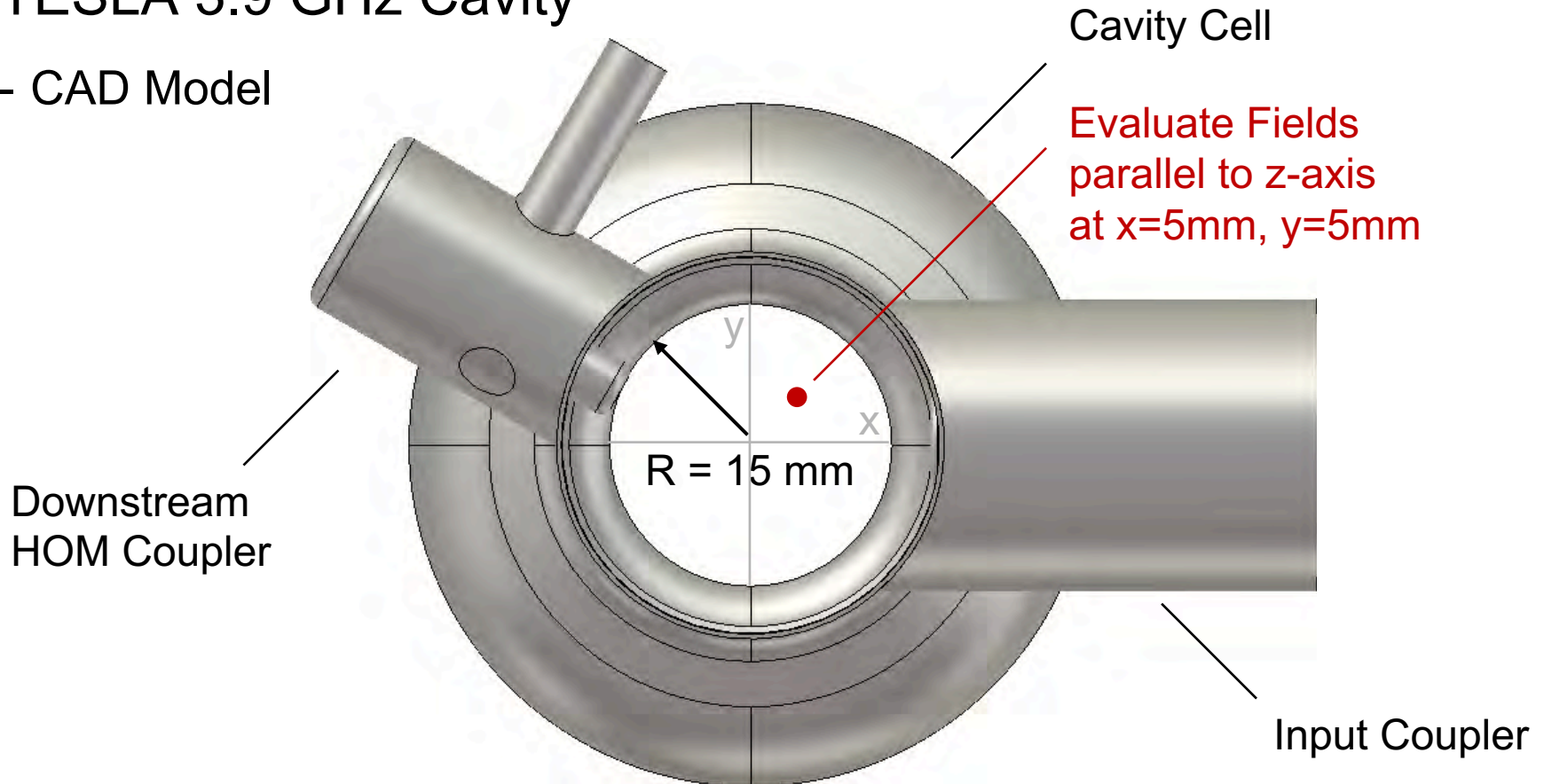
Higher-order mode
(dipole #37)



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Simulation Results

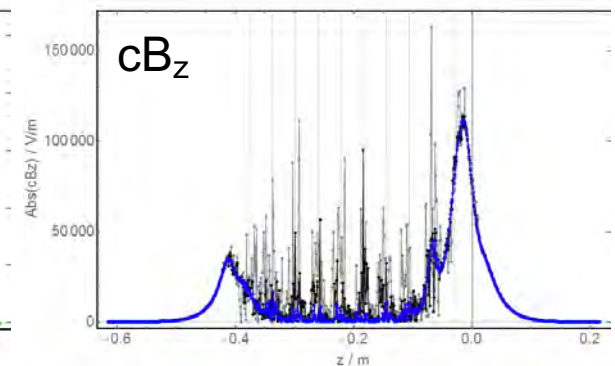
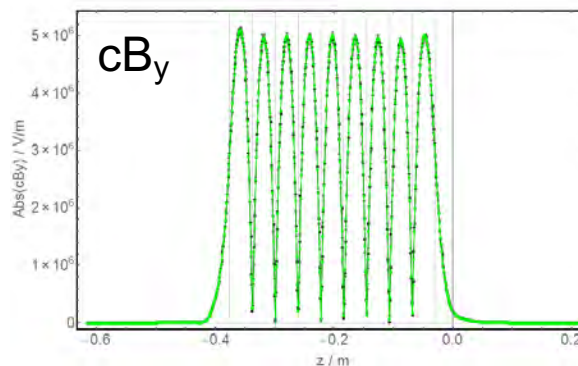
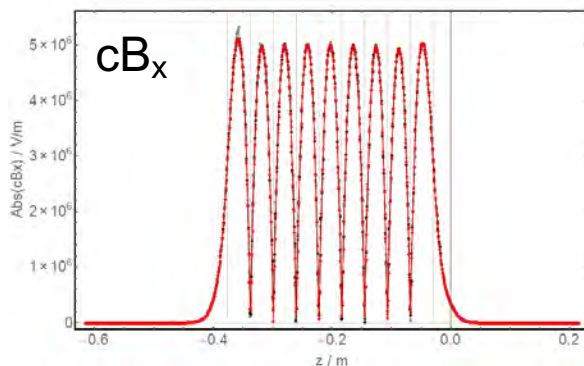
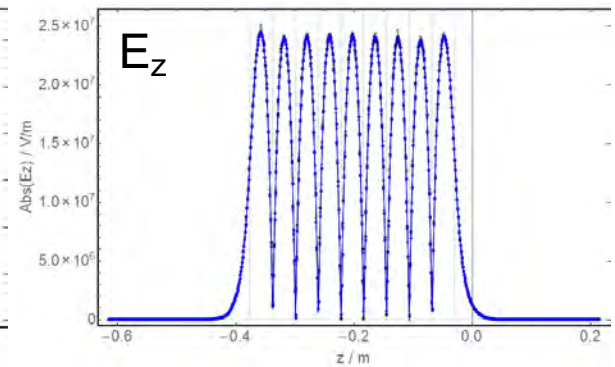
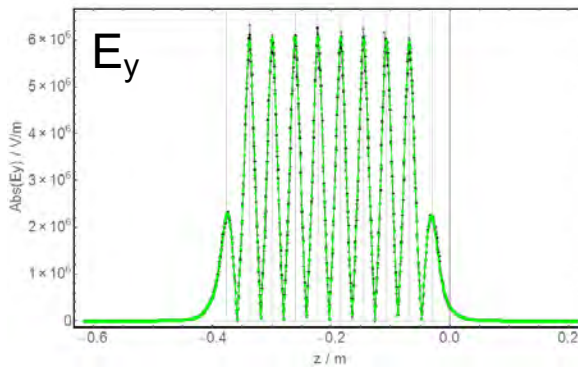
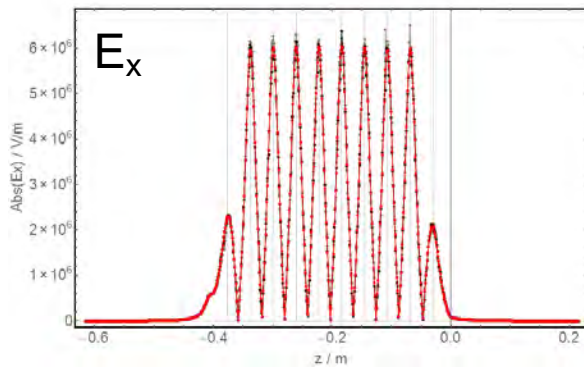
- TESLA 3.9 GHz Cavity
 - CAD Model



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Simulation Results

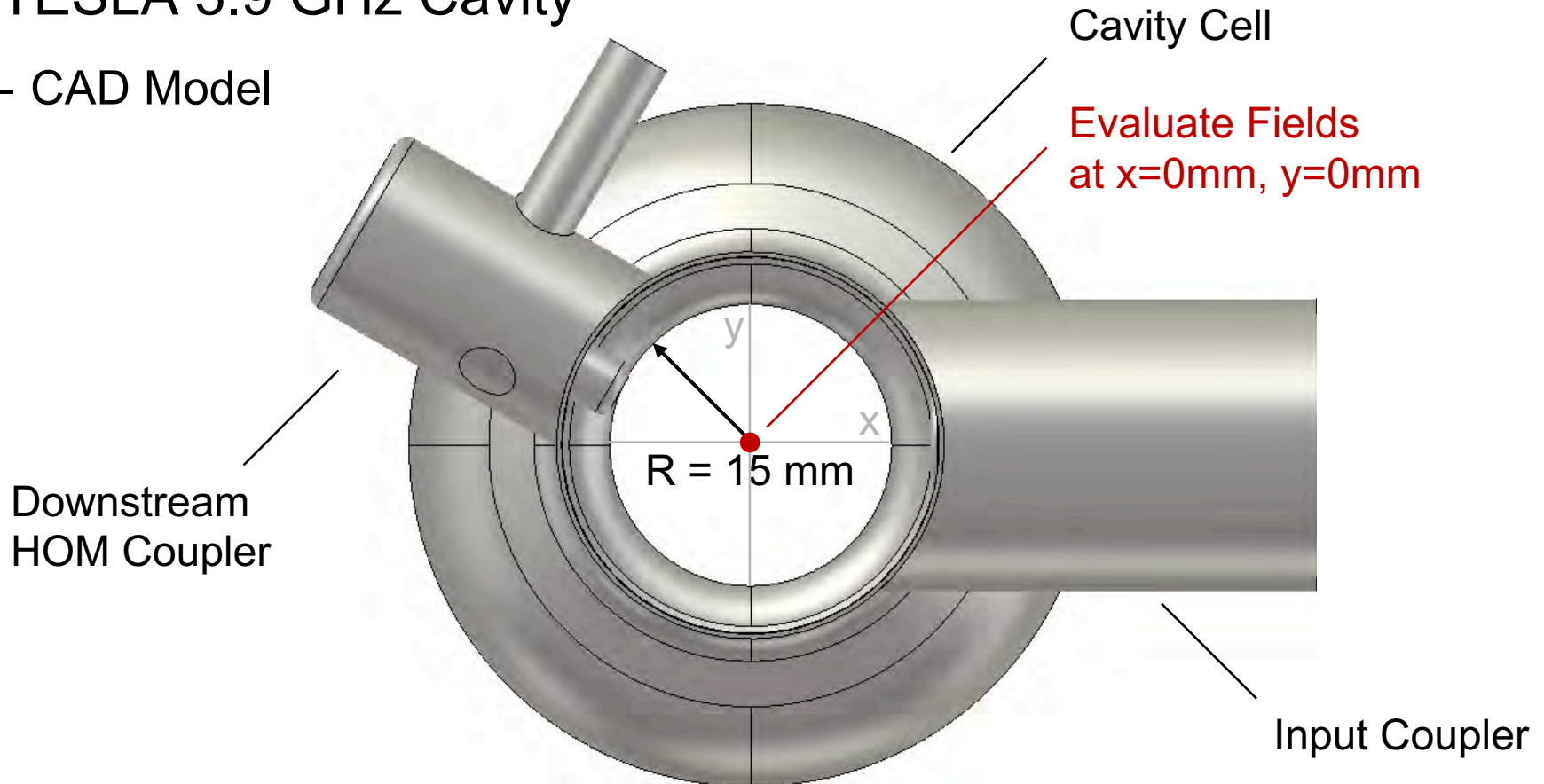
- Field components parallel to the cavity axis (LPW 4,8,16)
 - Transversal offset at $x_0 = 5 \text{ mm}$, $y_0 = 5 \text{ mm}$



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Simulation Results

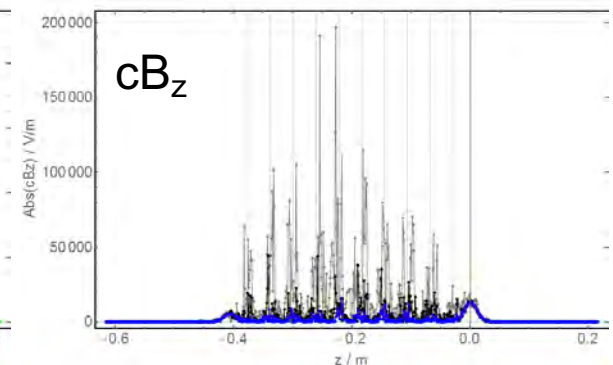
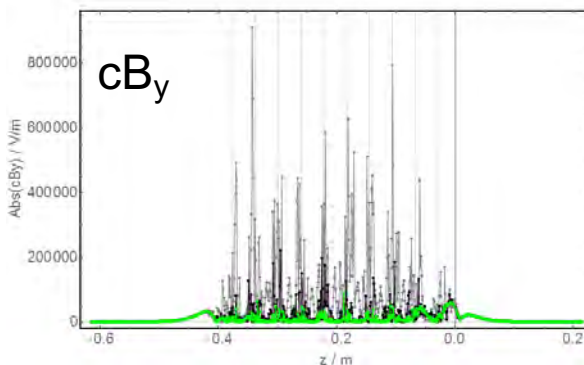
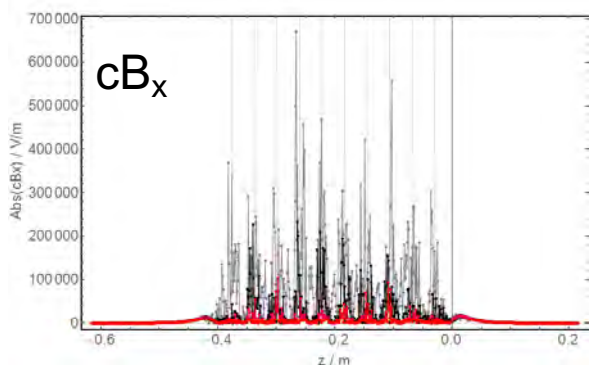
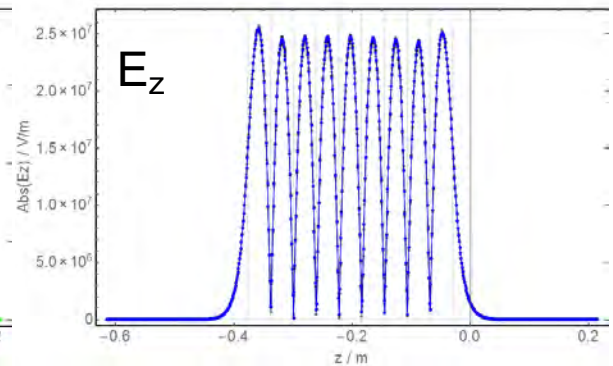
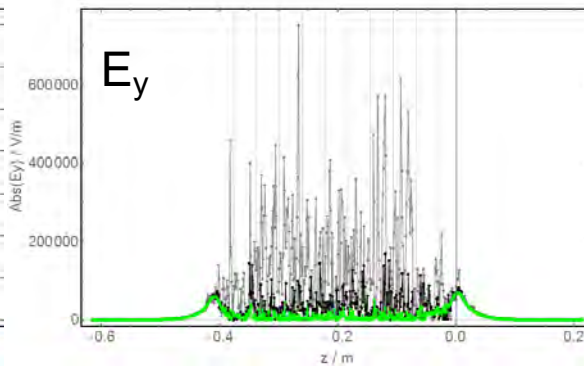
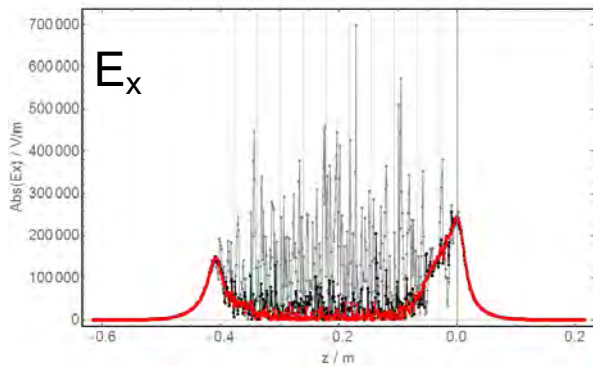
- TESLA 3.9 GHz Cavity
- CAD Model



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Simulation Results

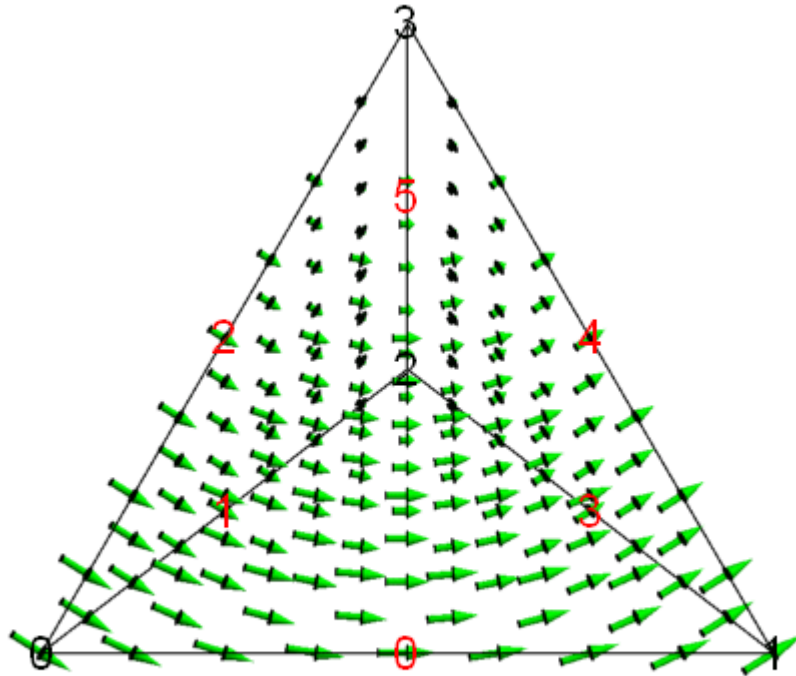
- Field components parallel to the cavity axis (LPW 4,8,16)
 - Transversal offset at $x_0 = 0$ mm, $y_0 = 0$ mm



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Simulation Results

- Field Representation in the Finite Element Method
 - Vector Basis Funktion $\vec{w}_0(\vec{r})$



Example:
Equilateral tetrahedron

Point	x	y	z
0	0	0	0
1	1	0	0
2	$\frac{1}{2}$	$\frac{1}{2}\sqrt{3}$	0
3	$\frac{1}{2}$	$\frac{1}{2\sqrt{3}}$	$\sqrt{2/3}$

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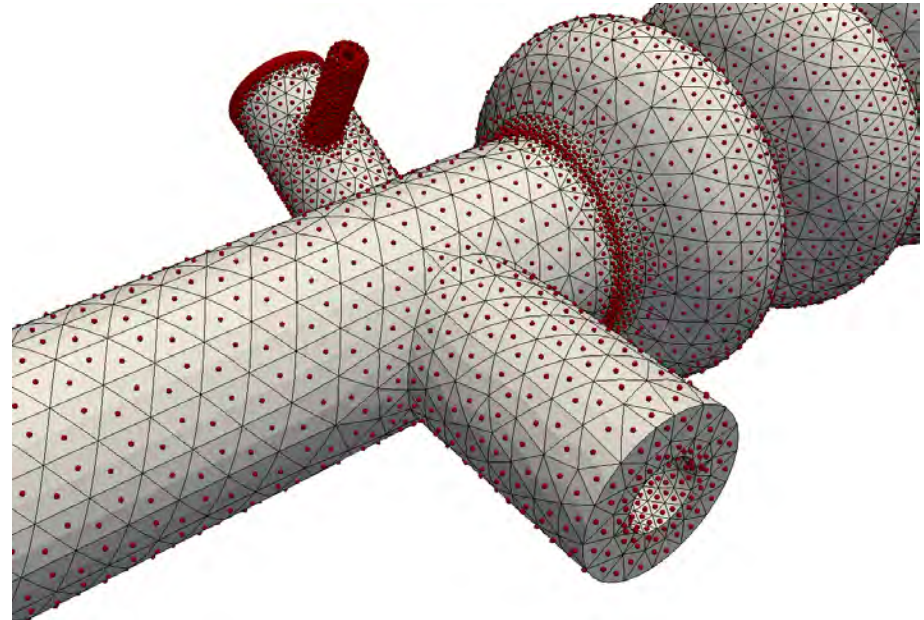
Simulation Results

▪ Field reconstruction using the Kirchhoff integral

- Field values inside a closed surface can be determined once the surface field components are available

- Kirchhoff integral

$$G = \frac{e^{-ik|\vec{r}-\vec{r}'|}}{4\pi|\vec{r}-\vec{r}'|} \quad k = \frac{2\pi f}{c_0}$$

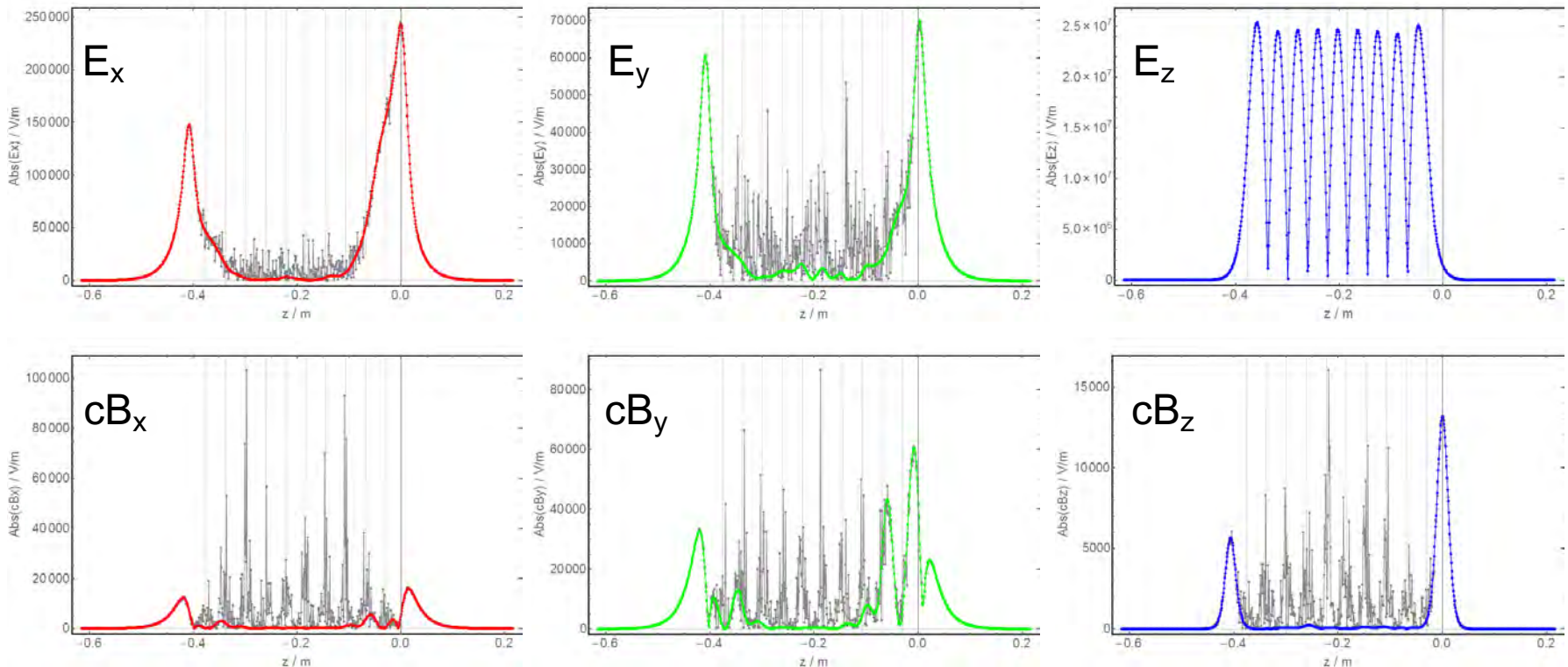


$$\vec{E}(\vec{r}) = \int \left(k(\vec{n}' \times ic_0\vec{B}') G - (\vec{n}' \times \vec{E}') \times \nabla G - (\vec{n}' \cdot \vec{E}') \nabla G \right) dA'$$
$$ic_0\vec{B}(\vec{r}) = \int \left(k(\vec{n}' \times \vec{E}') G - (\vec{n}' \times ic_0\vec{B}') \times \nabla G - (\vec{n}' \cdot ic_0\vec{B}') \nabla G \right) dA'$$

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Simulation Results

- Field components parallel to the cavity axis (LPW 16)
 - Transversal offset at $x_0 = 0$ mm, $y_0 = 0$ mm

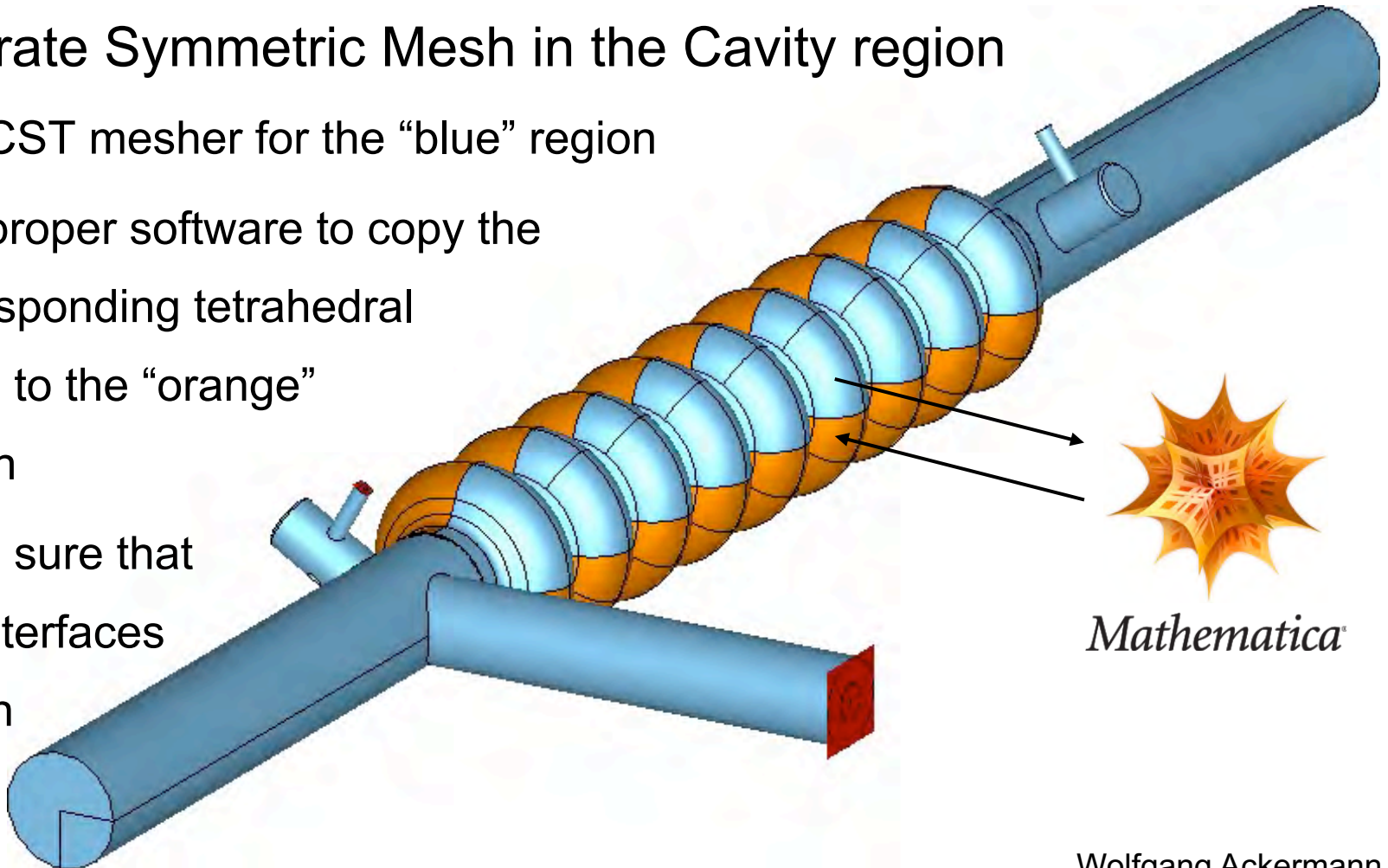


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Simulation Results

- Generate Symmetric Mesh in the Cavity region

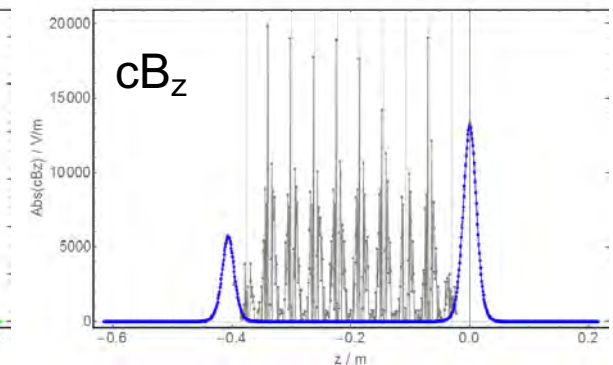
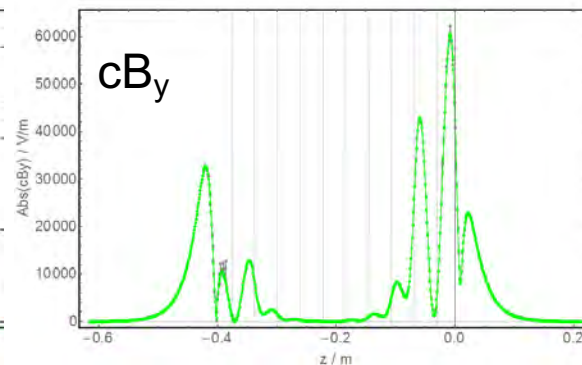
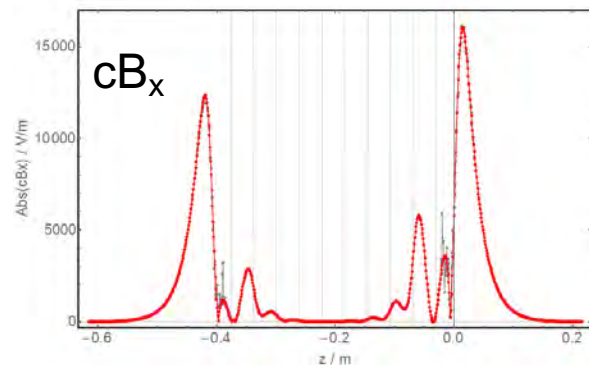
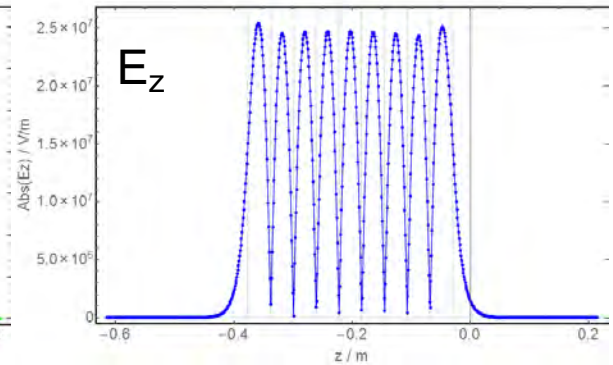
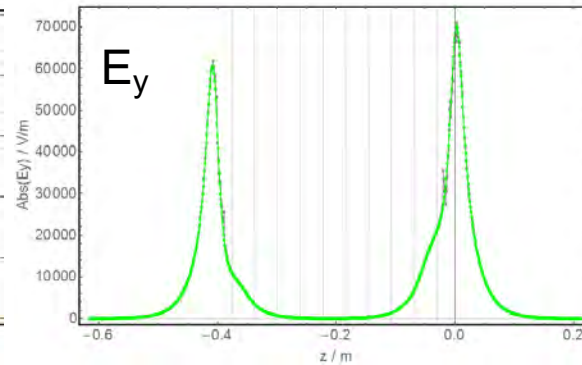
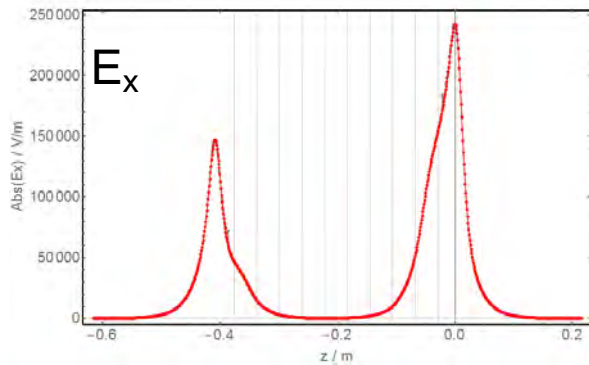
- Use CST mesher for the “blue” region
- Use proper software to copy the corresponding tetrahedral mesh to the “orange” region
- Make sure that the interfaces match



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Simulation Results

- Field components parallel to the cavity axis (LPW 16)
 - Transversal offset at $x_0 = 0$ mm, $y_0 = 0$ mm



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Categorisation : EM Field Simulation

CEM3D

PBCI

FD

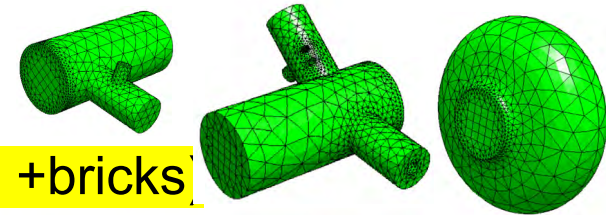
CSR DG

PAMASO

REPTIL

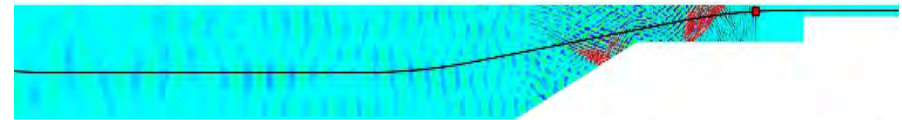
- volumetric meshes

- structured (hexahedra)
- unstructured (tetrahedra, possibly +pyramids +bricks)
- meshless



- volumetric discretisation

- finite-difference time-domain (FDTD), finite-integration technique (FIT)
- finite-element methods (FE)
- discontinuous Galerkin
- particle-particle models



- discretisation in time

- time domain
- frequency domain
- eigenmodes

