

Development of a detector setup to determine the 2s – hyperfine transition of $^{209}\text{Bi}^{80+}$ at the Experimental Storage Ring at GSI

Denis Anielski
Westfälische Wilhelms-Universität Münster
28.01.2011

- Motivation for physics of highly charged Ions
- Hyper fine structure
- Laser spectroscopy ESR
- Monte-Carlo-Simulation
- “Old” mirror system
- Parabolic mirror system

The status of QED in the low field regime

„Quantum electrodynamics (QED) is the most precise theory in physics“

- g-factor of the free electron
- Lamb-Shift
- HFS of hydrogen
- ...

Example: g-factor of the free electron $\vec{\mu}_s = g_s \mu_B \frac{\vec{s}}{\hbar}$

$$g/2 = 1.001\,159\,652\,180\,85\,(76)$$

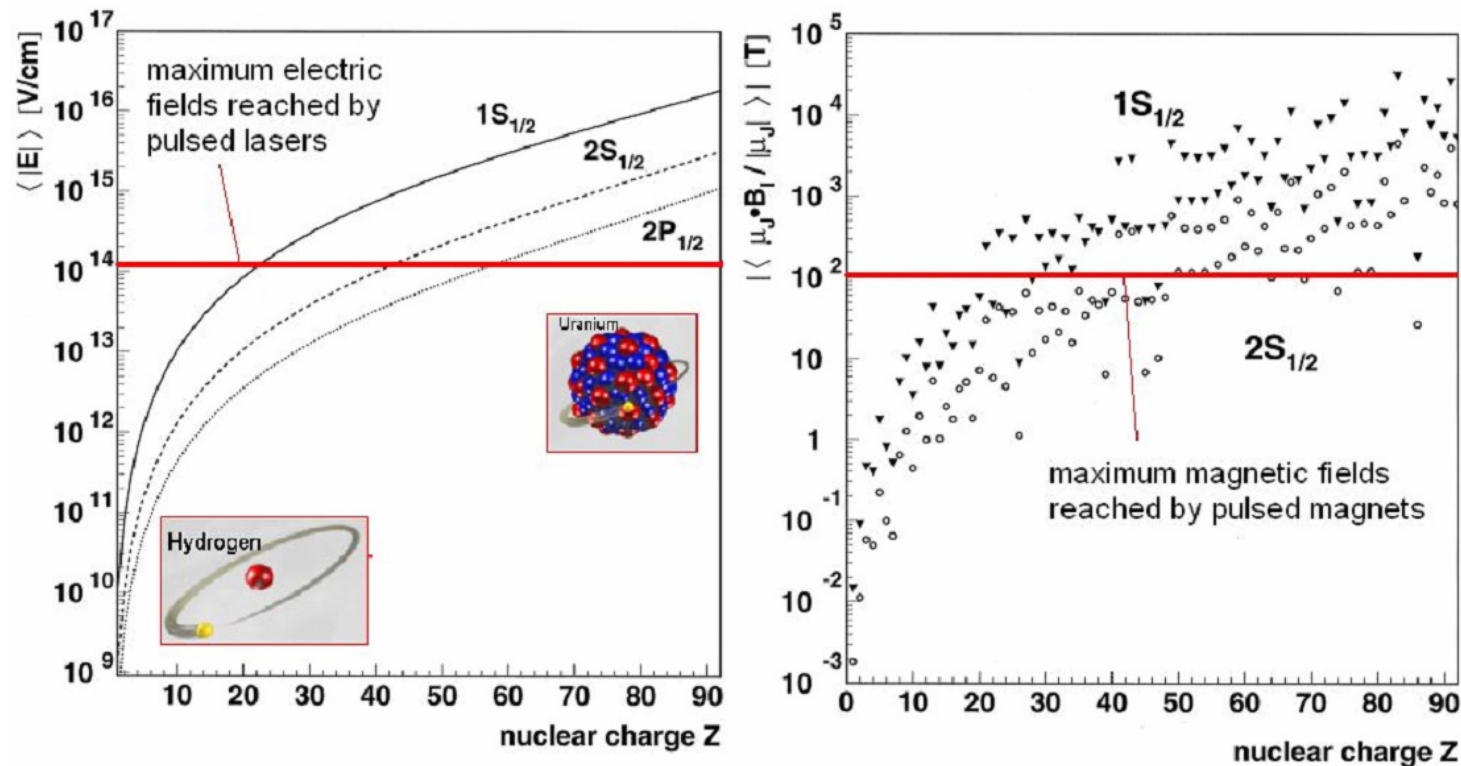
Experiment [1]

$$g/2 = 1.001\,159\,652\,180\,86\,(10)(26)(848)$$

Theory [2]

[1] Kinoshita et al., PRD 73(1), 013003-27 (2006)

[2] Odom et al., PRL 97, 030801 (2006)



- Extremely high electromagnetic fields near the nucleus
 - $Z\alpha \approx 10^{-2} \longrightarrow Z\alpha \approx 1 \longrightarrow$ non-perturbative calculations
- \longrightarrow Test of QED in heavy H-like Ions

Hyperfine structure

$$\Delta E'_{\text{HFS}} = \alpha g_I \frac{m_e}{m_p} \frac{F(F+1) - I(I+1) - j(j+1)}{2j(j+1)} m_e c^2 \frac{(Z\alpha)^3}{n^3(2l+1)}$$

H	H-like →	$^{207}\text{Pb}^{81+}$	$^{209}\text{Bi}^{82+}$
$\lambda = 21 \text{ cm}$	$\sim \Delta E^{-1} \sim Z^{-3}$ →	$\lambda = 1020 \text{ nm}$	$\lambda = 244 \text{ nm}$
$\tau = 1.1 \cdot 10^7 \text{ a}$	$\sim \Delta E^{-3} \sim Z^{-9}$ →	$\tau = 52 \text{ ms}$	$\tau = 0.4 \text{ ms}$

Full description including rel. effects, nuclear structure and QED contributions

$$\Delta E_{\text{HFS}} = \Delta E'_{\text{HFS}} \cdot \mathcal{M} \left(A(Z\alpha)(1-\delta)(1-\epsilon) + \frac{\alpha}{\pi} \Delta\epsilon_{\text{QED}} \right)$$

Finite mass
of nucleus

Relativistic
Effects

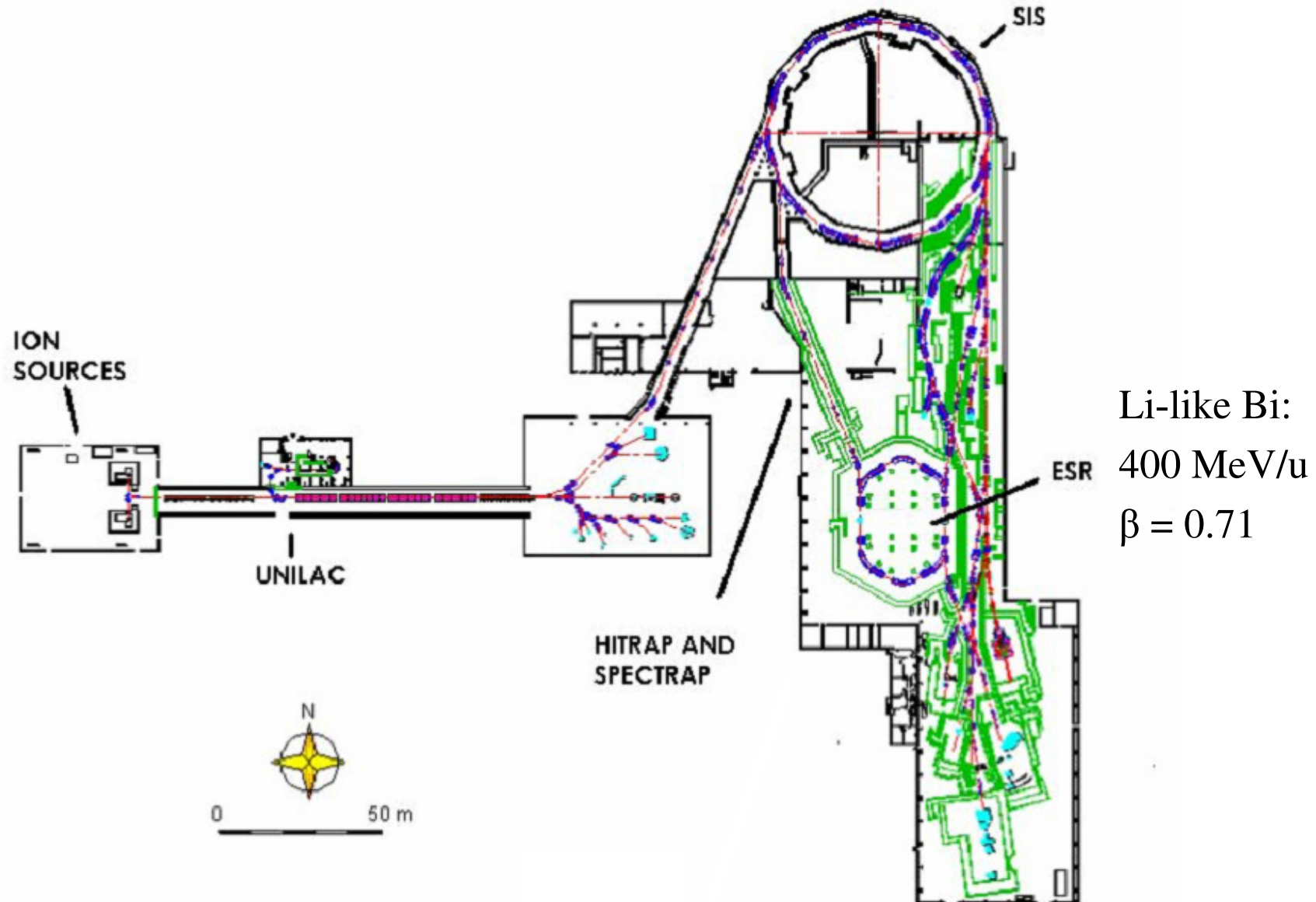
Breit-Rosenthal-
Effect

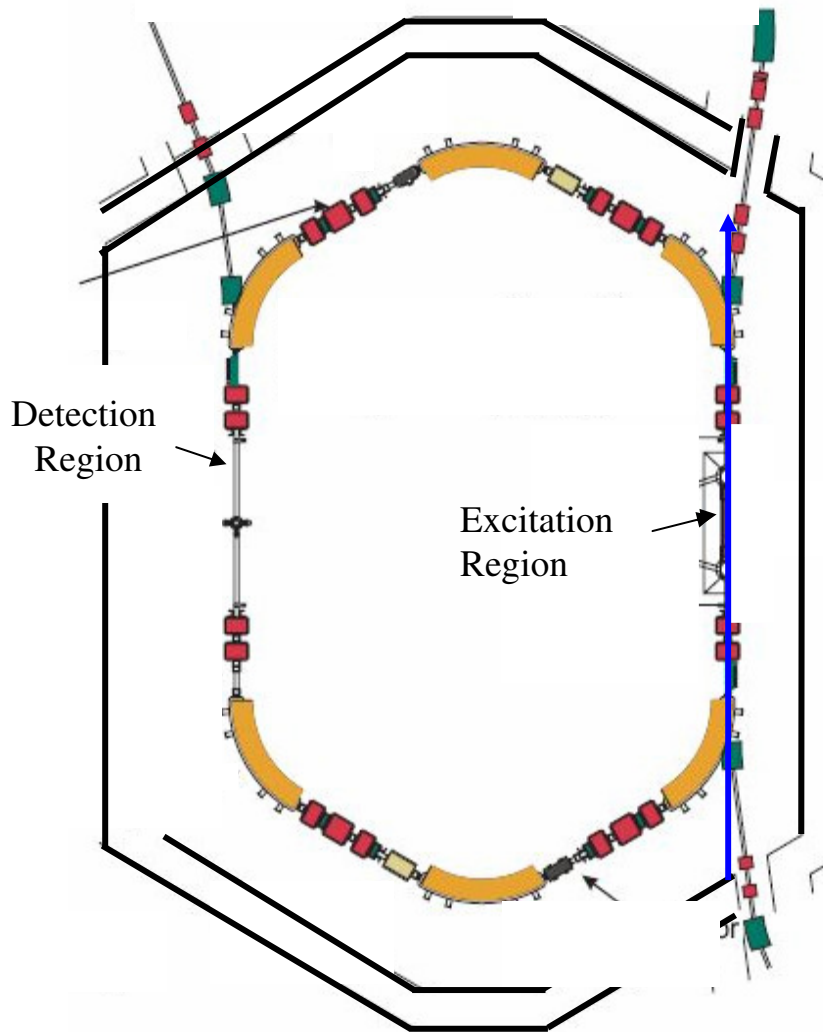
Bohr-Weisskopf-
Effect

QED-
Contribution



The Accelerator Facility at GSI





- Relativistic Doppler effect

$$\lambda_{\downarrow\uparrow} = \lambda' \gamma (1 - \beta)$$

$${}^{209}\text{Bi}^{80+}: \lambda_0 = 1555 \text{ nm}$$

$$\beta = 0.71 \text{ (400 MeV/u)}$$

$$\lambda_{\text{Lab}} = 640 \text{ nm}$$

- Change wavelength of laser

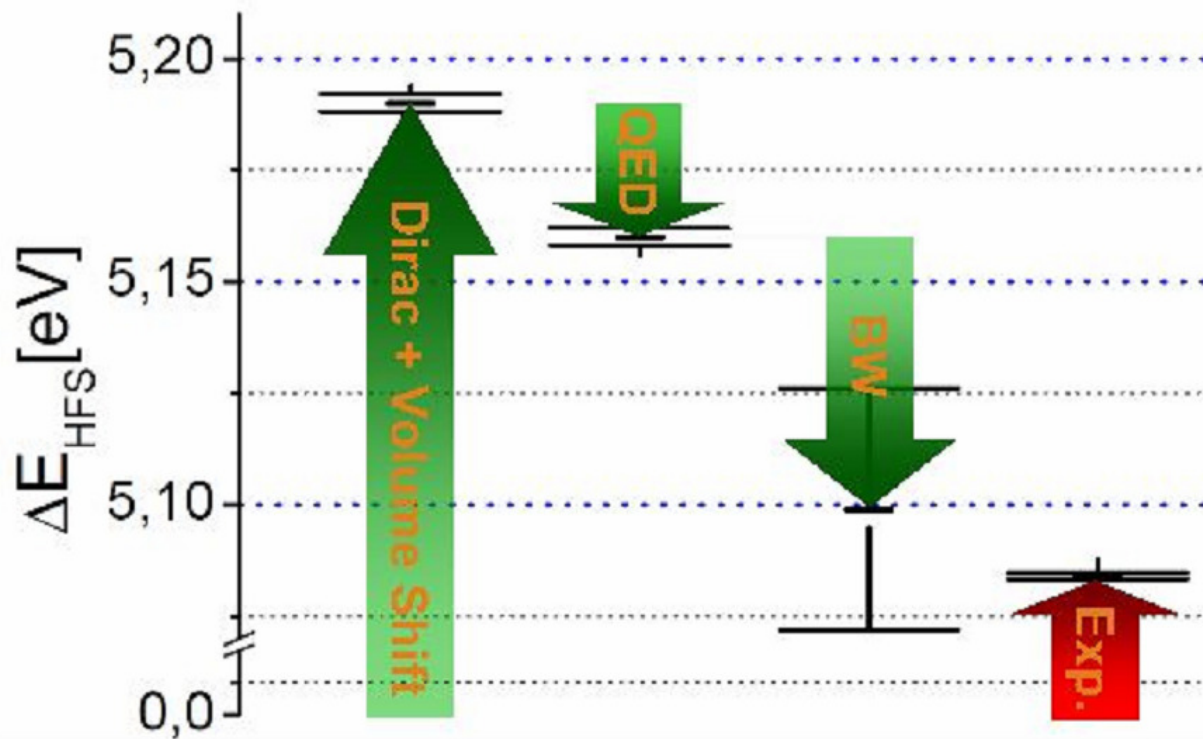
$$\longrightarrow E_{\text{HFS}}$$

- Reduced Background:
 - Signal- und Reference-bunch
 - Small window for DAQ

Results for H-like HCl

$$^{207}\text{Pb}^{81+} \quad \lambda=1019.7 (2) \text{ nm} \quad \Delta E_{\text{HFS}}=1.2159 (2) \text{ eV} \quad [1]$$

$$^{209}\text{Bi}^{82+} \quad \lambda=243.87 (4) \text{ nm} \quad \Delta E_{\text{HFS}}=5.0841 (4) \text{ eV} \quad [2]$$



Experimental uncertainties are very small!

Theoretical uncertainties of BW-Effect are very high!

Test of QED not possible!

[1] Seelig, Dissertation Uni Mainz (1999)

[2] Klaft et al., PRL 73, 2425-2427 (1994)

Disentangling QED and nuclear structure

$$\text{HFS}_{\text{H-like}} \quad \Delta E^{(1s)} = \Delta E_{\text{Dirac}}^{(1s)} (1 - \epsilon^{(1s)}) + E_{\text{QED}}^{(1s)}$$

$$\text{HFS}_{\text{Li-like}} \quad \Delta E^{(2s)} = \Delta E_{\text{Dirac}}^{(2s)} (1 - \epsilon^{(2s)}) + \Delta E_{\text{int}} (1 - \epsilon^{(\text{int})}) + \Delta E_{\text{QED}}^{(2s)} + \Delta E_{\text{int-QED}}$$

The specific difference

$$\Delta E' = \Delta E^{(2s)} - \xi \Delta E^{(1s)} \quad \text{with}$$

$$\xi = f(\alpha Z) \frac{\Delta E_{\text{Dirac}}^{(2s)} + f_{\text{int}}(\alpha Z) \Delta E_{\text{int}}}{\Delta E_{\text{Dirac}}^{(1s)}} \quad \frac{\epsilon^{(2s)}}{\epsilon^{(1s)}} \equiv f(\alpha Z) \quad \frac{\epsilon^{(\text{int})}}{\epsilon^{(2s)}} \equiv f_{\text{int}}(\alpha Z)$$

is independent of the BW-effect and can be calculated to rather high accuracy!

$$\Delta E' = \Delta E'_{\text{non-QED}} + \Delta E'_{\text{QED}} = (61.25 \pm 0.04) \text{ meV}$$

Solution: Measurement of HFS of H- and Li-like Ion of the same Isotope!

Isotope		Wavelength [nm]	Life time [ms]
$^{207}\text{Pb}^{81+}$	(H-like)	1020	52
$^{209}\text{Bi}^{82+}$	(H-like)	244	0.4
$^{209}\text{Bi}^{80+}$	(Li-like)	≈ 1555	82

2x without success \longrightarrow Monte-Carlo Simulation

HFS_{Li-Bi} between 1500 nm and 1590 nm

Measurement time is the relevant value to decide
if signal rate is too low or not

$$\Delta x = \sqrt{X + Y}$$

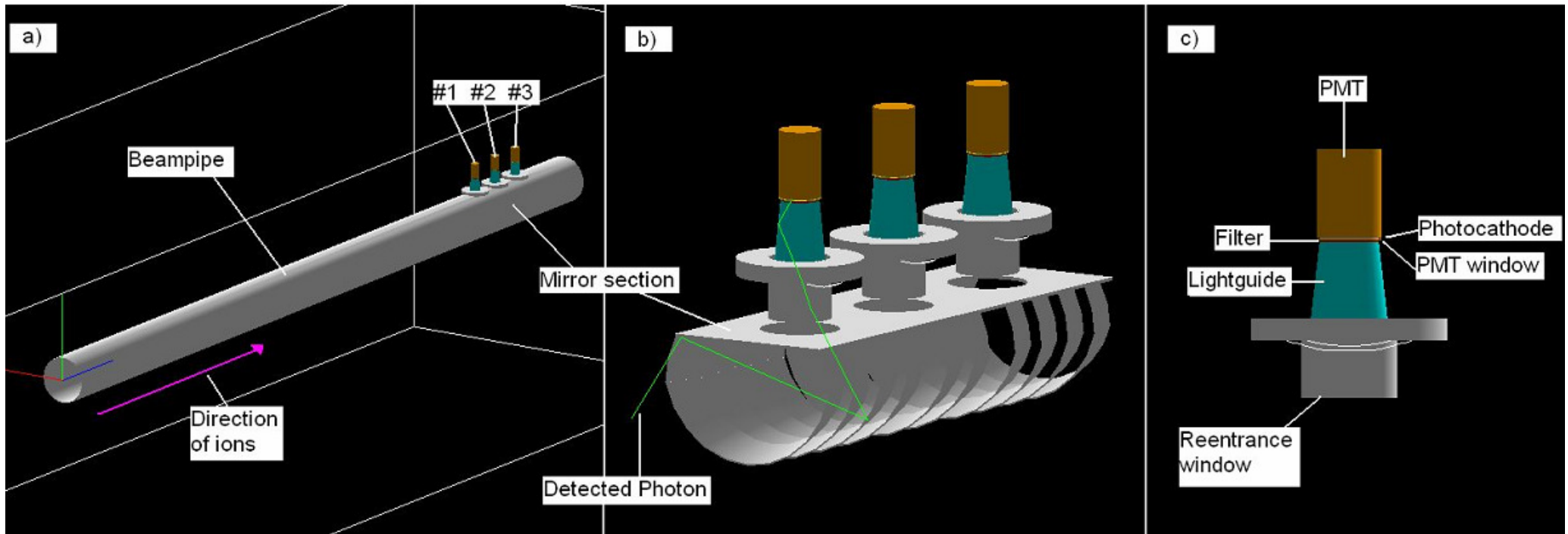
$$\Delta x \approx \sqrt{2 \cdot X}$$

$$S \cdot t \geq n \cdot \sqrt{2 \cdot (U_{ESR} + D) \cdot t}$$

$$\Leftrightarrow t = \frac{2 \cdot n^2 \cdot (U_{ESR} + D)}{S^2} \quad n = 3$$

Seven days beam time

→ at most 10 s to 12 s measurement time per wavelength



Check with measurement of HFS of H-like Pb:

Measured: $S = (416 \pm 1) \text{ cps}$

Simulated: $S = (423 \pm 4) \text{ cps}$

Signal rate of Li-like bismuth at mirror section

$S = (14 \pm 1) \text{ cps}$ (Simulation)

$U = (772 \pm 2) \text{ cps}$ (2003 measured)

$t_{n=3} = (71 \pm 1) \text{ s}$

$t_{n=2} = (31 \pm 1) \text{ s}$ Probably the reason, why Signal has not been found

Optimizations:

- Different detectors
- Larger window ($\varnothing 60 \text{ mm}$ \longrightarrow $\varnothing 70 \text{ mm}$)
- Lightguide

No significant change

\longrightarrow **Development of a new detector setup!**

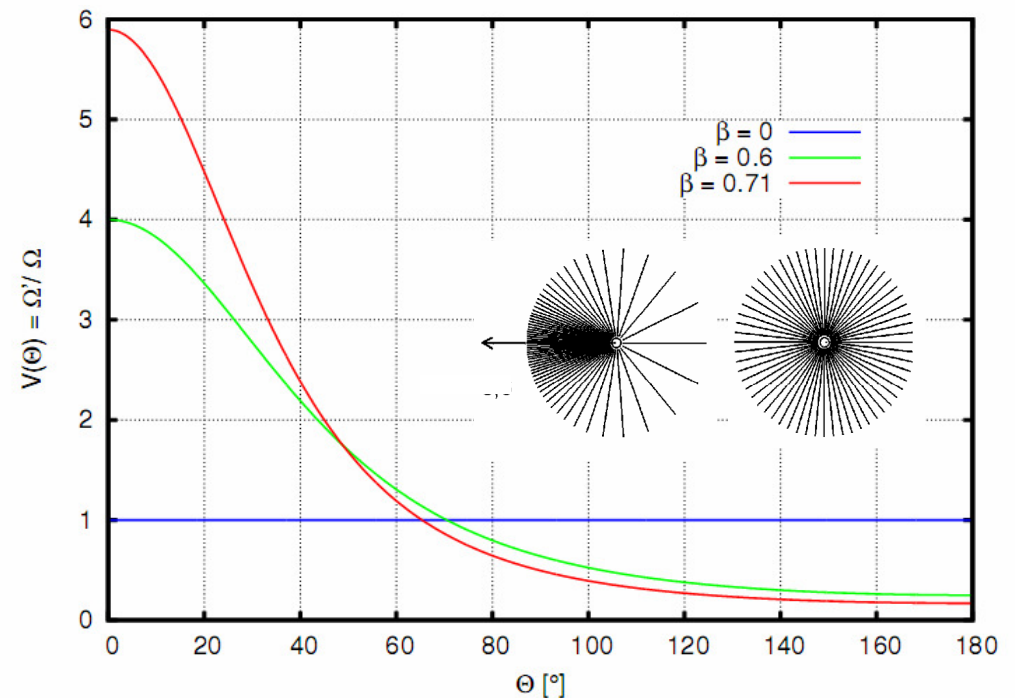
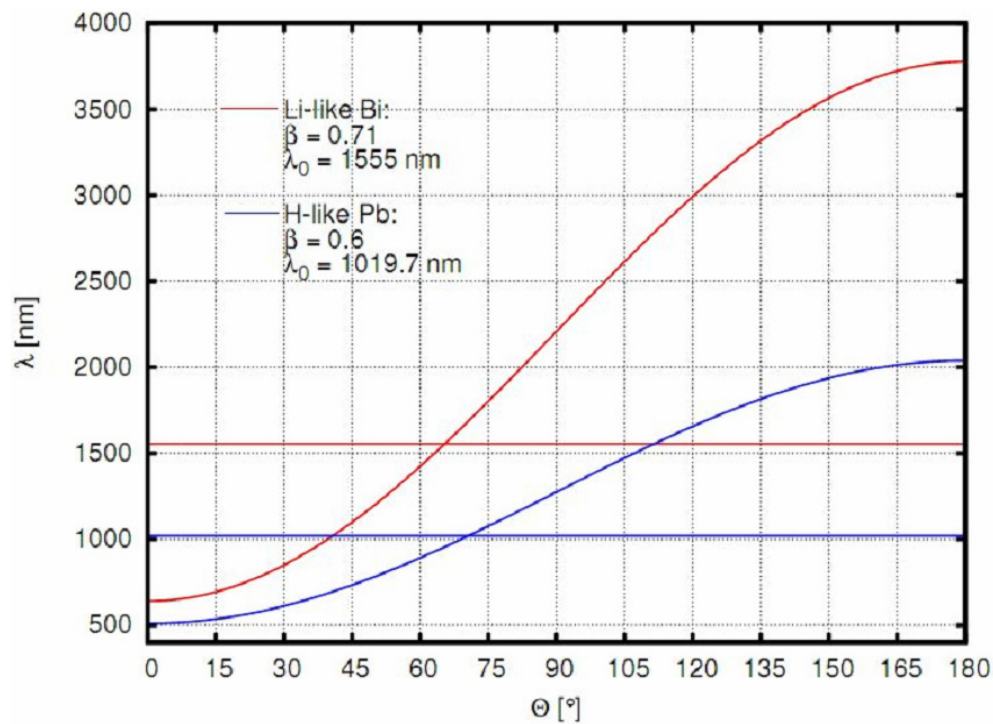
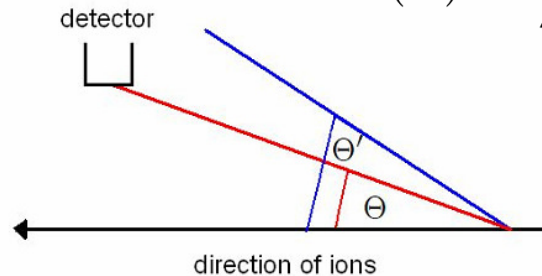
Rel. Doppler effect:

$$\lambda = \lambda' \cdot \gamma(1 - \beta \cos(\Theta))$$

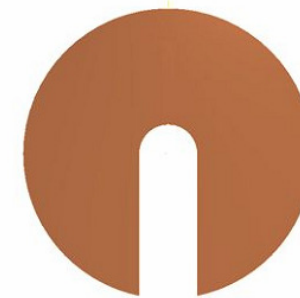
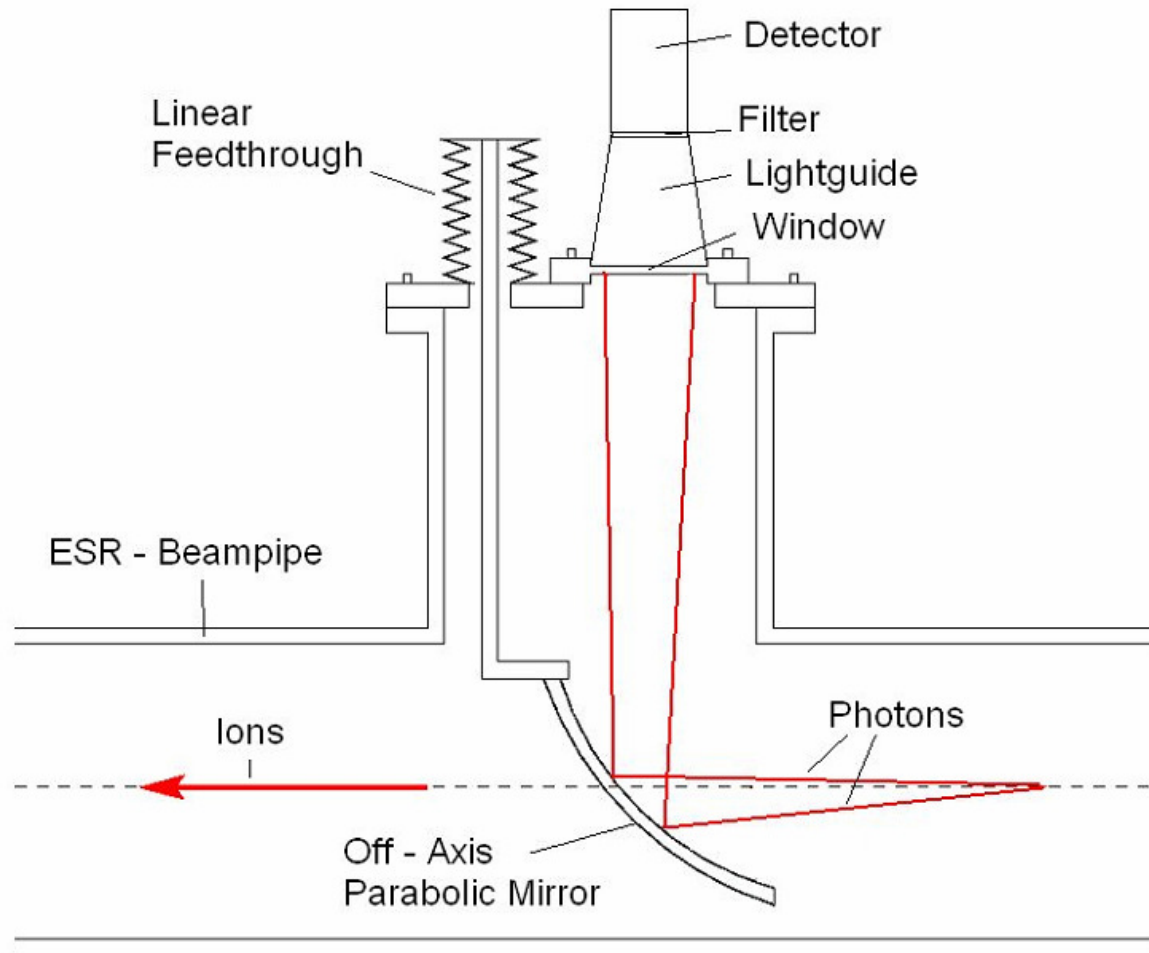
$$(25^\circ \triangleq 800 \text{ nm})$$

Rel. Boost:

$$V(\Theta) = \frac{\Delta\Omega'}{\Delta\Omega} = \frac{\sin \Theta' d\Theta'}{\sin \Theta d\Theta} = \frac{1 - \beta^2}{(1 - \beta \cos(\Theta))^2}$$



Parabolic mirror system

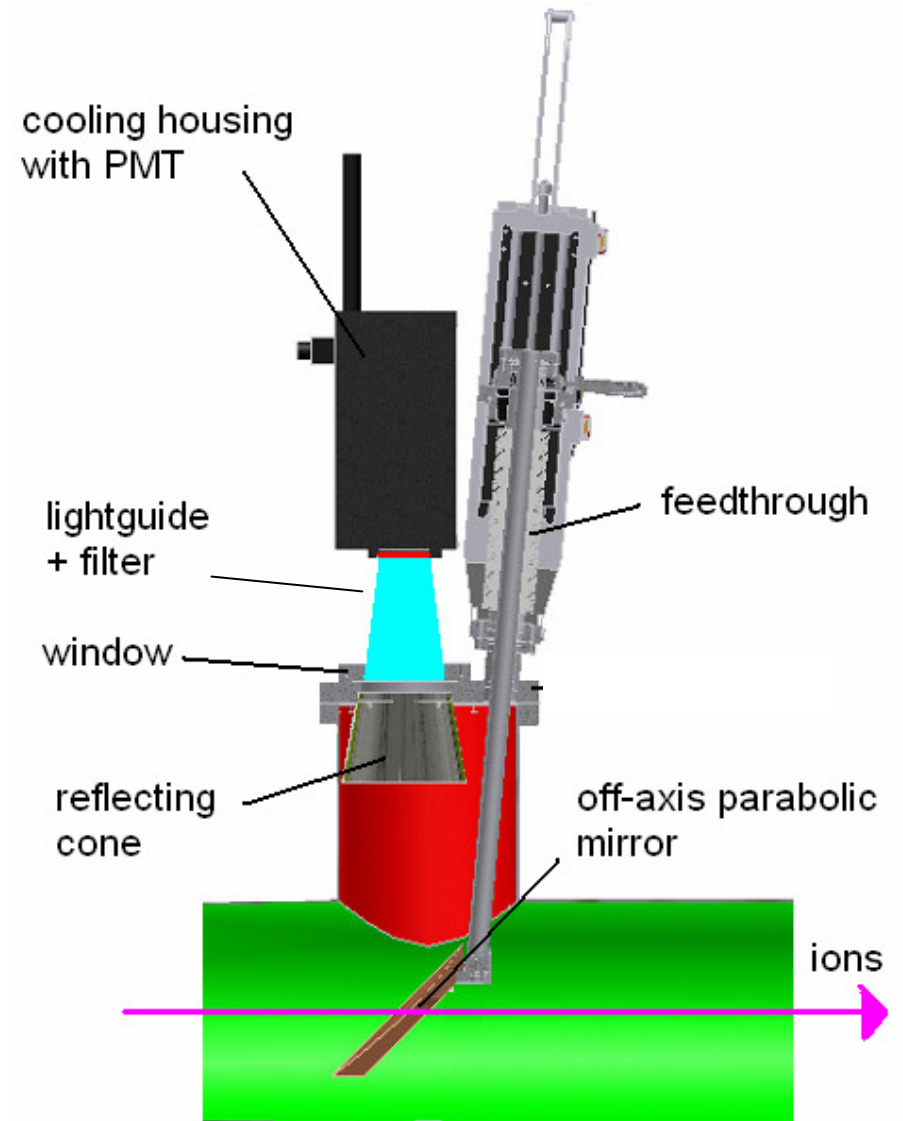


Mirror as seen by ions

Moveable off-axis-
parabolic mirror ± 100 mm \updownarrow

Optimization of parabolic mirror system

1. 1-flange-option vs. 2-flange-option
2. Reentrance window vs. "cone"
3. Shape of mirror
4. Detector
5. Size of window
6. Lightguide
7. "Extreme" wavelength



Results parabolic mirror system

Parabolic mirror:

$$S = (60 \pm 1) \text{ cps}$$

$$U = (427 \pm 9) \text{ cps} \quad t = (2.1 \pm 0.1) \text{ s}$$

Old mirror:

$$S = (14 \pm 1) \text{ cps}$$

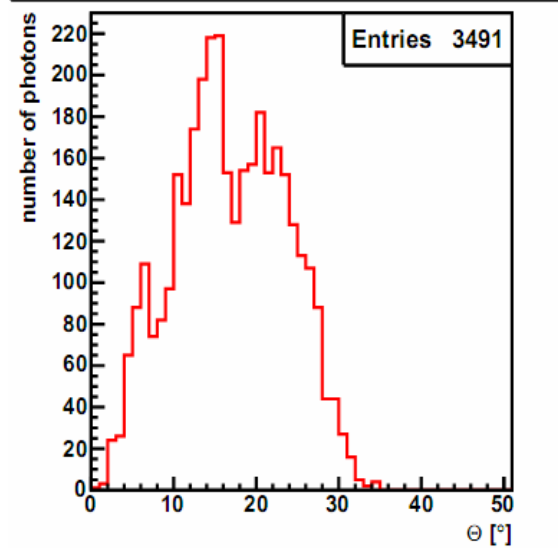
$$U = (772 \pm 1) \text{ cps} \quad t = (70.5 \pm 1) \text{ s}$$

$t < 10 \text{ s}!!!$

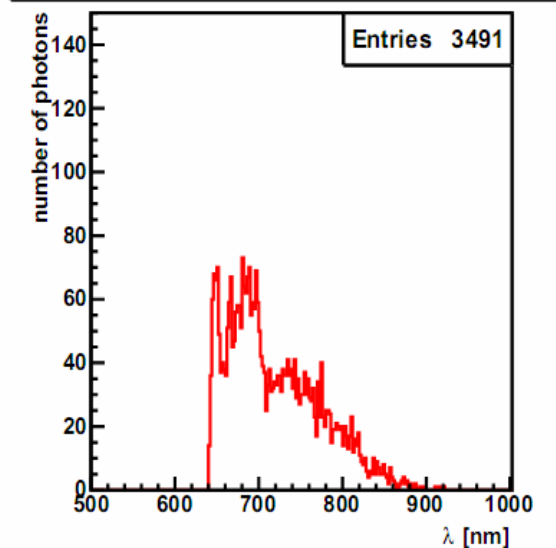
33 times better!

Detected photons

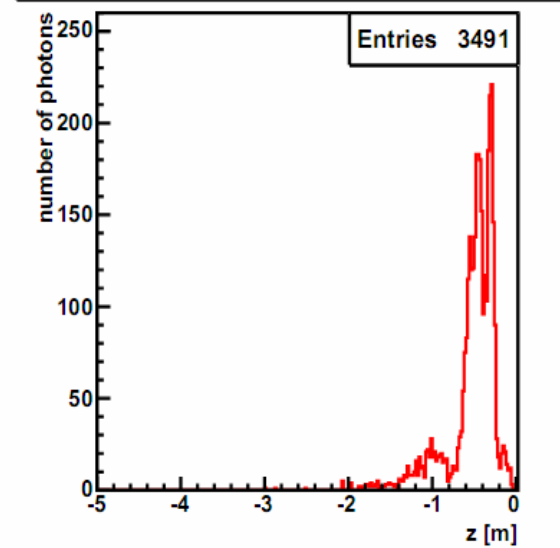
observed angle of detected photons - window2



observed wavelength of detected photons - window2

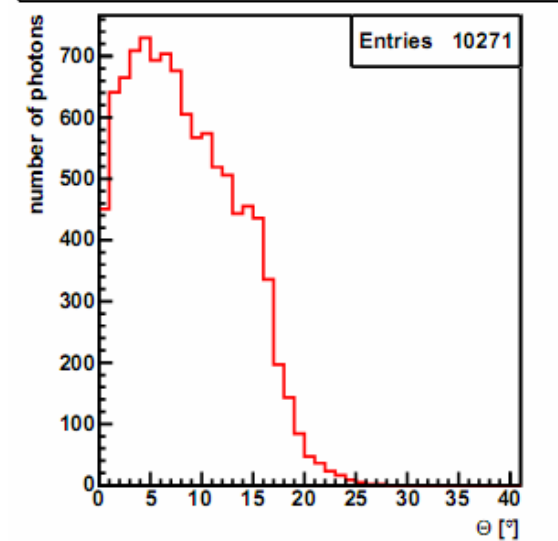


z-coordinates of detected photons - window2

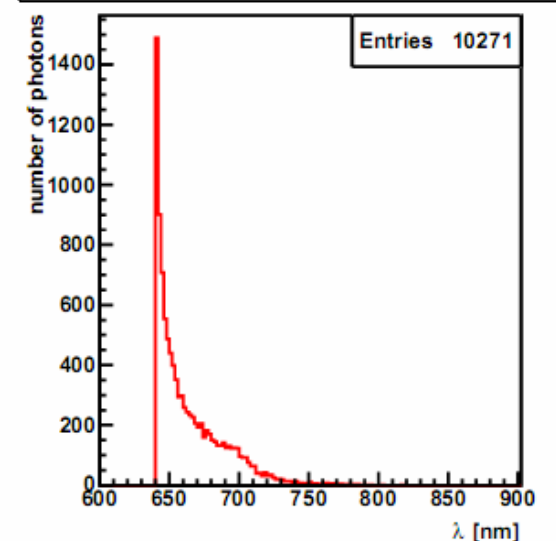


Mirror
section

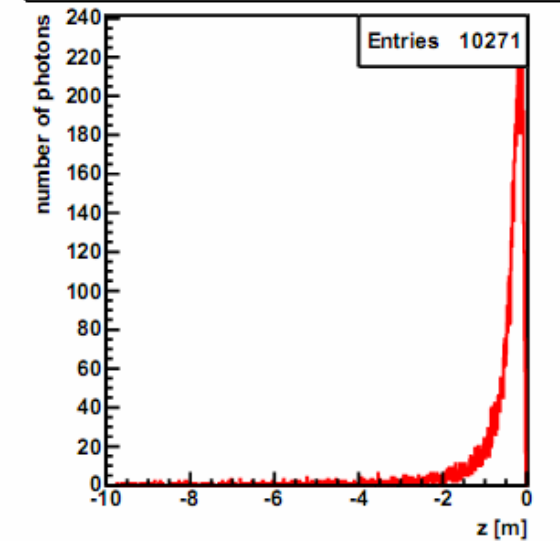
polar angle (lab) of detected photons



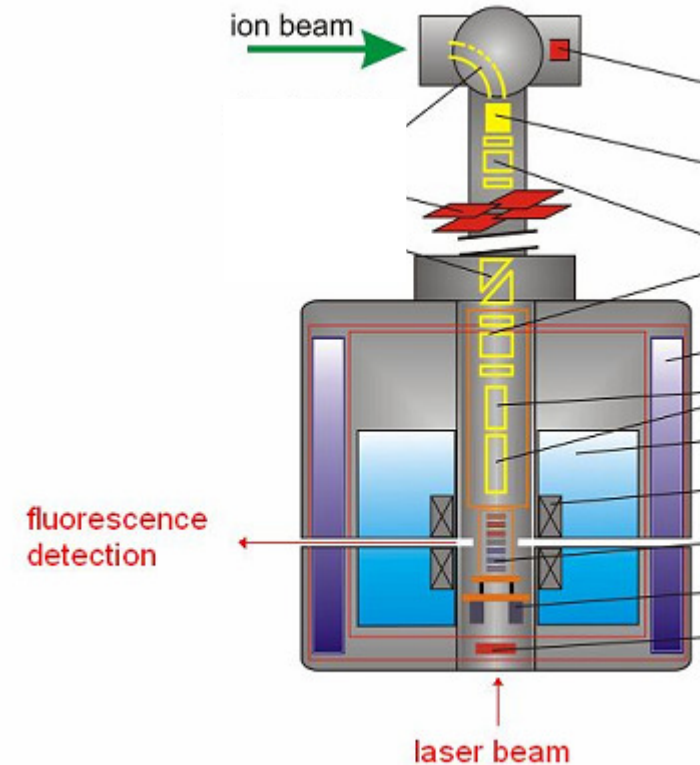
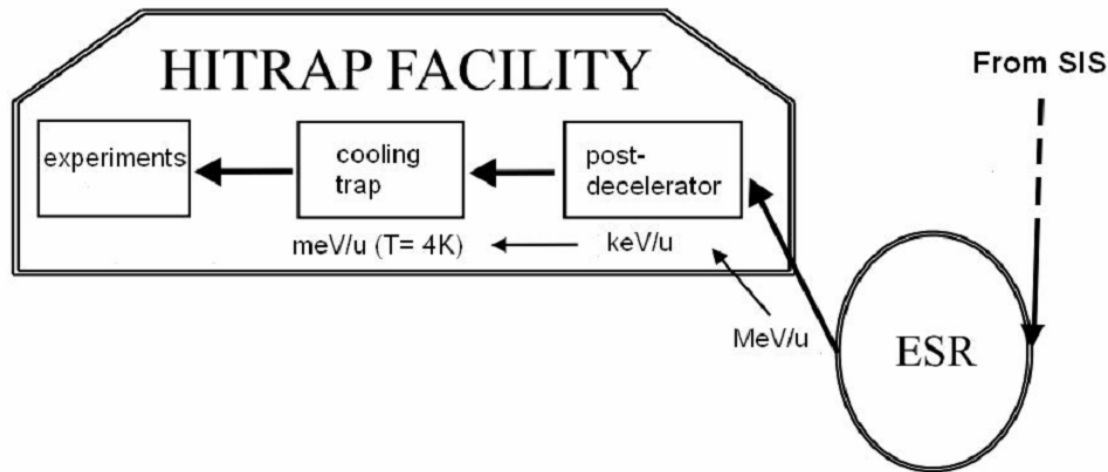
wavelength (lab) of detected photons



z-coordinates of detected photons



Parabolic
mirror



ESR: $\Delta\lambda/\lambda = 10^{-4}$

Spectrap: $\Delta\lambda/\lambda = 10^{-7}$ \longrightarrow Test of QED of a few per cent

Determination of HFS at ESR is required before measuring with Spectrap!



Setup in photographic laboratory

Characterization of PMT and CPM

- Single Photon Plateaus
- Sensitivity in B-field
- Jitter
- Dark counting rate (cooled)
- Test at ESR
- Detection of single photons
- Determination of QE

- Testing QED with laser spectroscopy at highly charged ions
- HFS of $^{209}\text{Bi}^{82+}$ determined, $^{209}\text{Bi}^{80+}$ under investigation
- Old mirror system not appropriate
- Development of new detector setup with off-axis parabolic mirror
- parabolic mirror successfully tested at ESR
- Development of new laser system and new DAQ at GSI
- Measurement spring 2011