

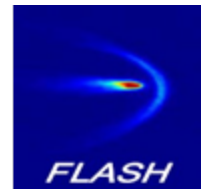
# Spurious Dispersion Effects at FLASH

Eduard Prat

Disputation – July 16, 2009



Universität Hamburg



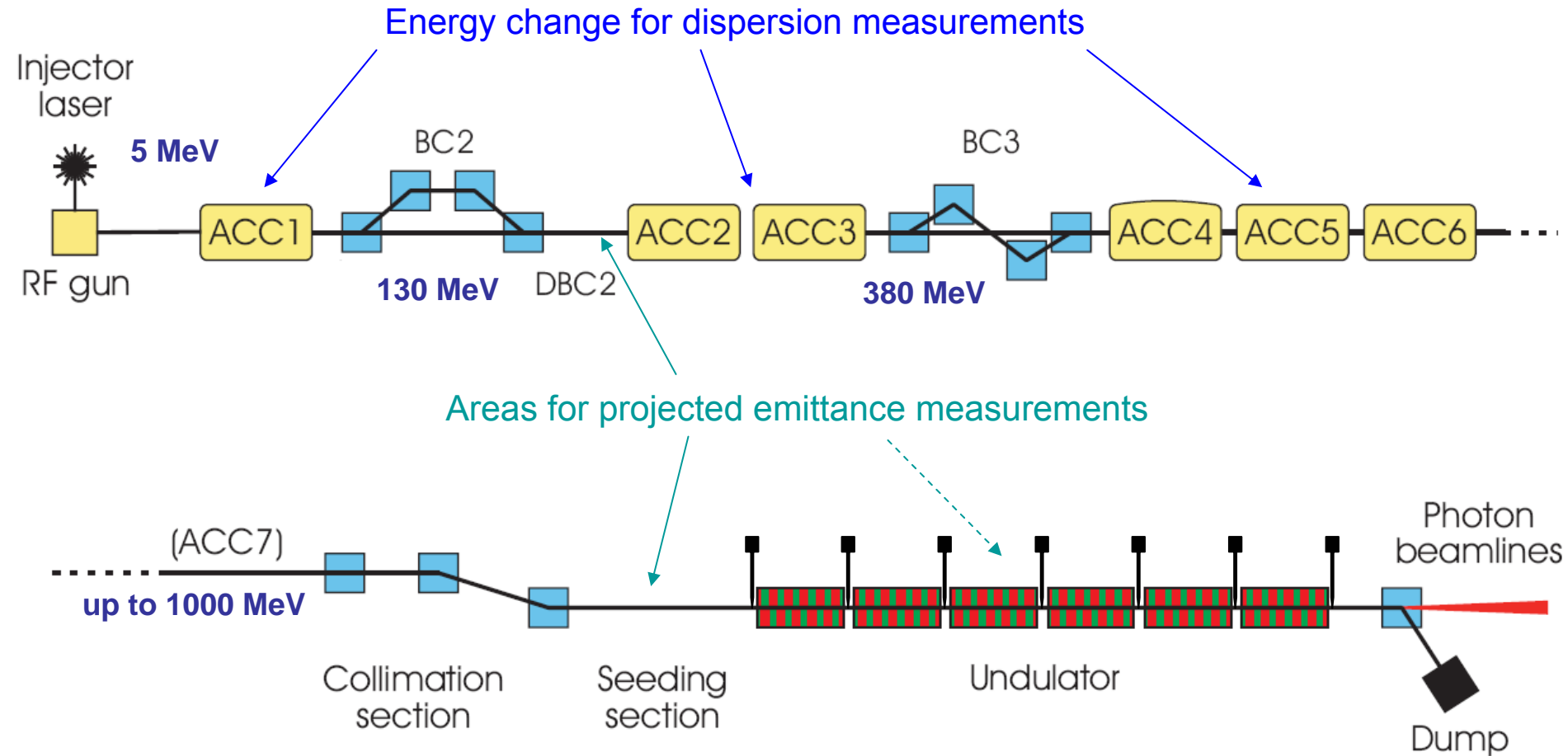
# Overview

- Introduction
- Generation mechanisms of dispersion
- Measurement and correction
- Effects on transverse beam quality at FLASH
- Effects on FEL performance at FLASH
- Conclusion

- **Introduction**
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# FLASH

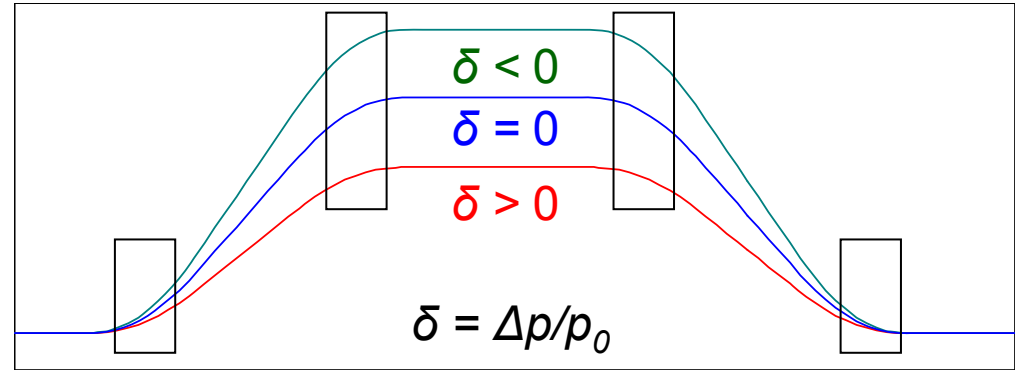
## Free-electron LASer in Hamburg



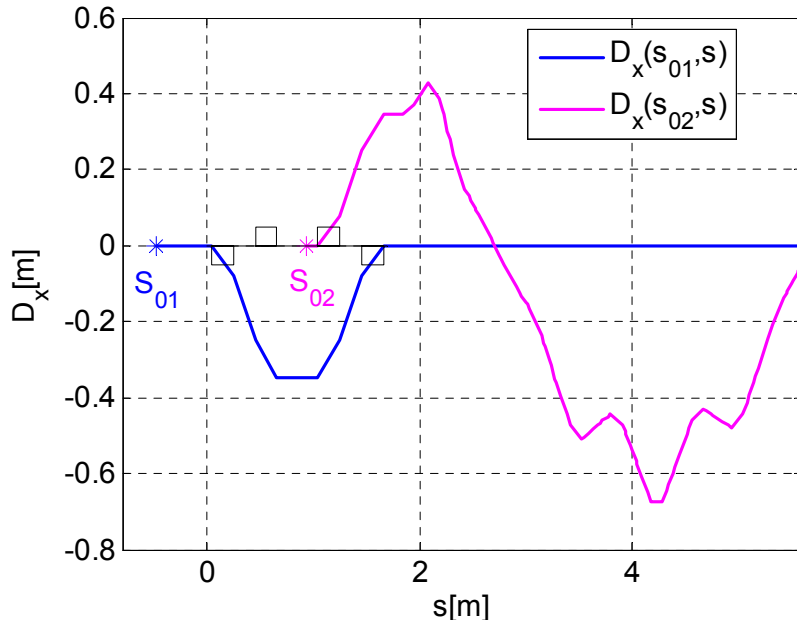
# Dispersion in linacs

Dispersion is the momentum dependence of charged particle deflections in a magnetic field

$$\frac{1}{\rho} = \frac{eB}{p}$$



The dispersion functions  $D_x(s_0, s)$  and  $D_y(s_0, s)$  describe the change in transverse phase-space coordinates at  $s$  due to a momentum change at  $s_0$ . They depend on the point where the momentum changes.



Effects to a single particle  
Beam offsets and angles

$$\Delta x_D(s) = D_x(s_0, s) \cdot \delta(s_0) + D_{xx}(s_0, s) \cdot \delta^2(s_0) + \dots$$

$$\Delta x'_D(s) = D'_x(s_0, s) \cdot \delta(s_0) + D'_{xx}(s_0, s) \cdot \delta^2(s_0) + \dots$$

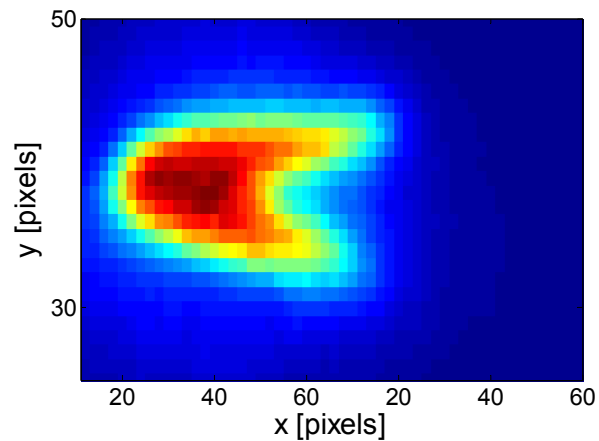
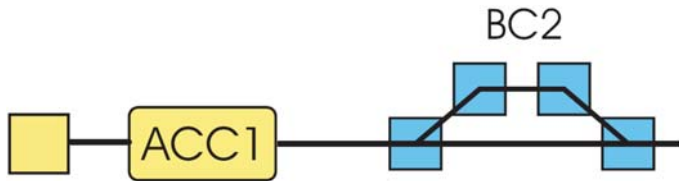
# Effects on the electron beam distribution

Circular accelerators  $\rightarrow$  moments of energy distribution = constant

Linacs  $\rightarrow$  moments of energy distribution  $\neq$  constant

The impact of dispersion depends on the position of the dispersion sources

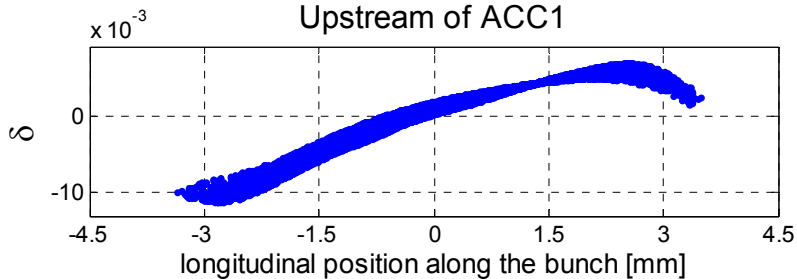
Example: c-shape effect  
at BC2 (FLASH)



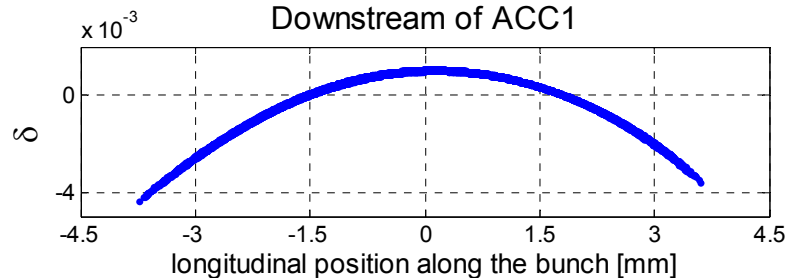
Measured beam  
image at BC2  
( $D_x = -35$  cm)

Momentum distributions

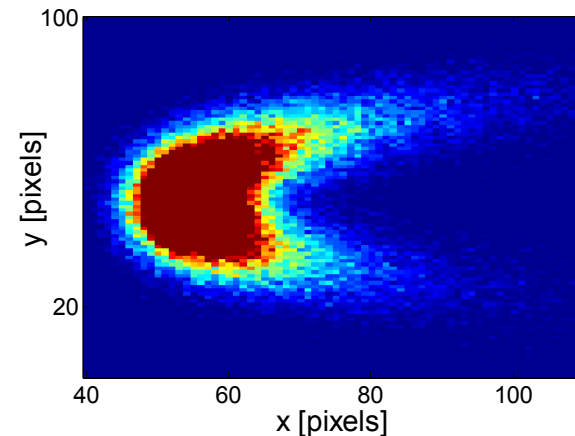
Upstream of ACC1



Downstream of ACC1



Simulated beam image at BC2  
(vertical dispersion source upstream of ACC1)



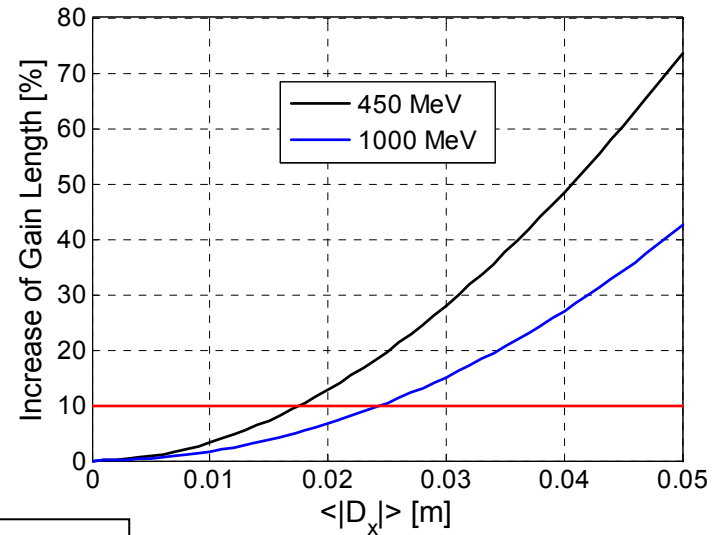
# Effects on the FEL process

1) Dispersion causes FEL power jitter due to electron energy fluctuations

2)  $D \rightarrow \sigma \uparrow \rightarrow \text{gain length} \uparrow, \text{power} \downarrow$

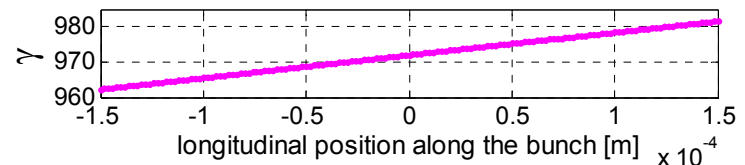
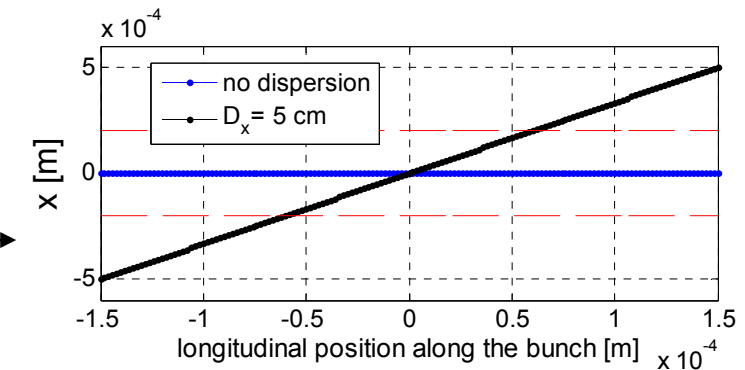
Increase of gain length for  
FLASH design parameters

$D < 1.8 \text{ cm} \rightarrow \text{Increase of gain length} < 10\%$



3)  $D \rightarrow \text{Intrabunch trajectory deviations} \rightarrow \text{power} \downarrow$

Example of offset along the  
bunch with and without dispersion

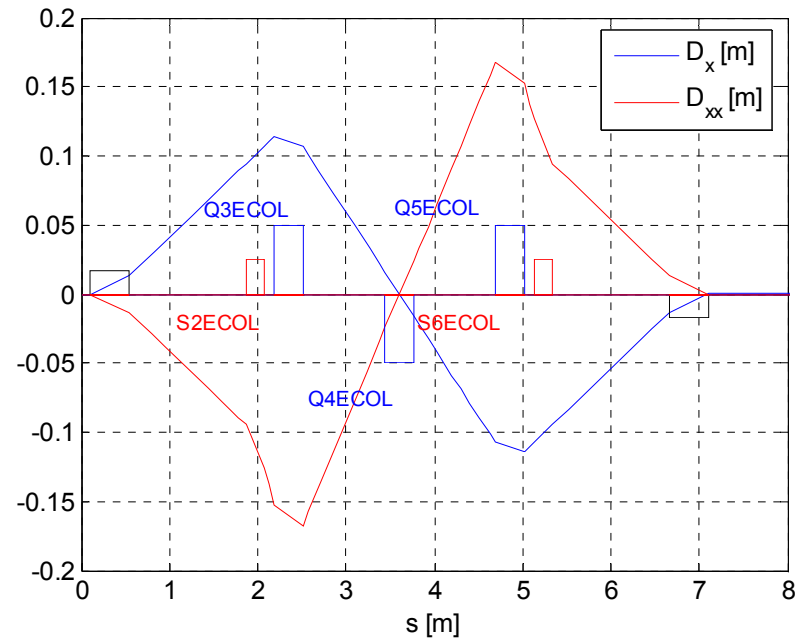
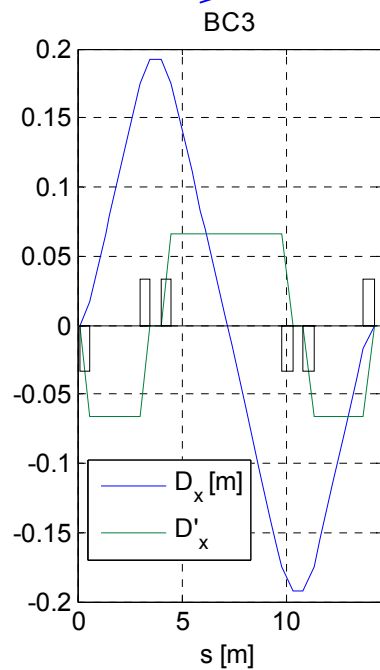
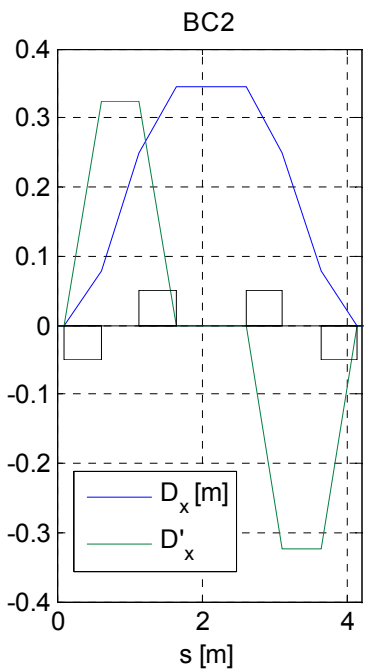
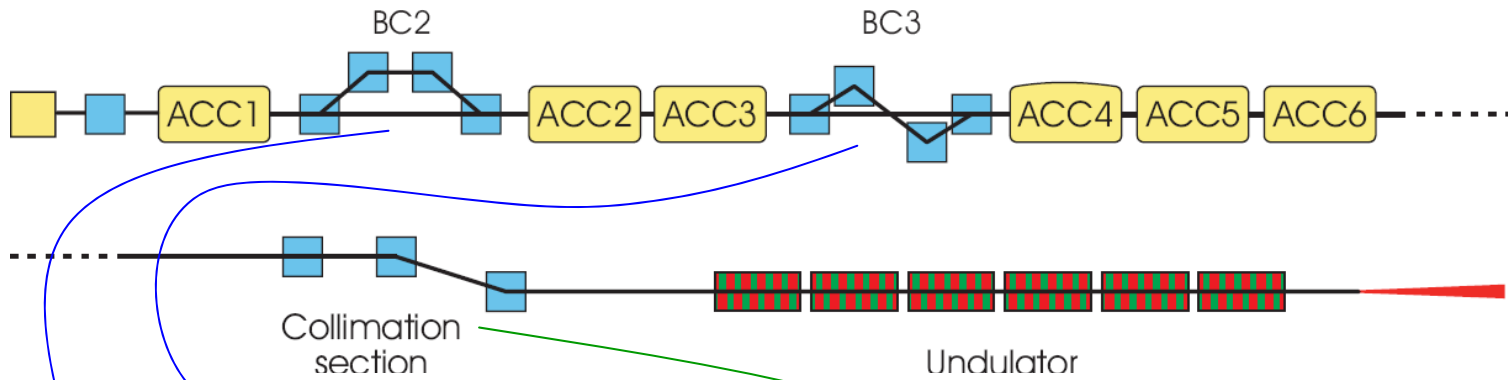


- Introduction
- **Generation mechanisms of dispersion**
- Measurement and correction
- Effects on transverse beam quality at FLASH
- Effects on FEL performance at FLASH
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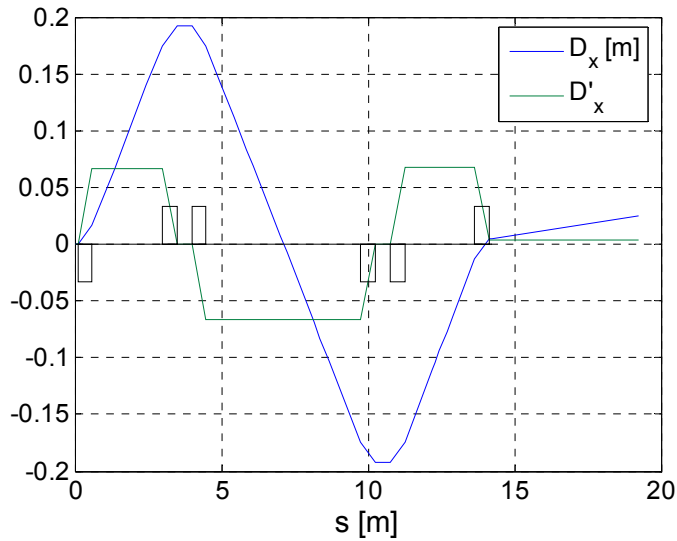
# Dispersive sections in FELs

## Bunch compressors and collimator sections

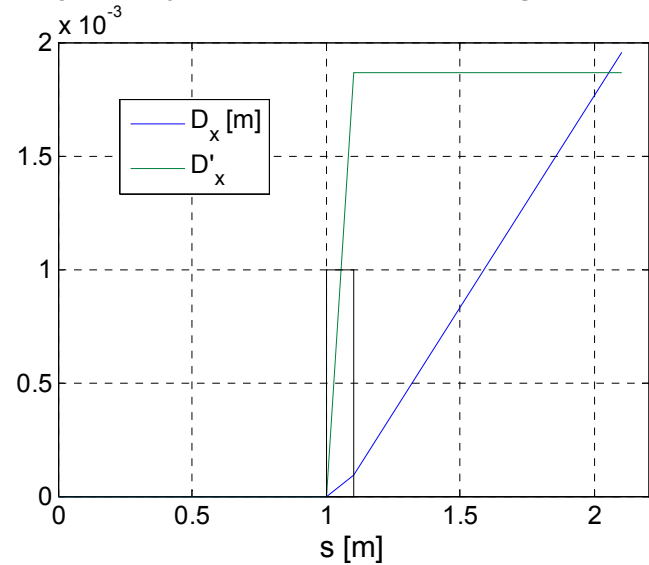


# Spurious dispersion sources

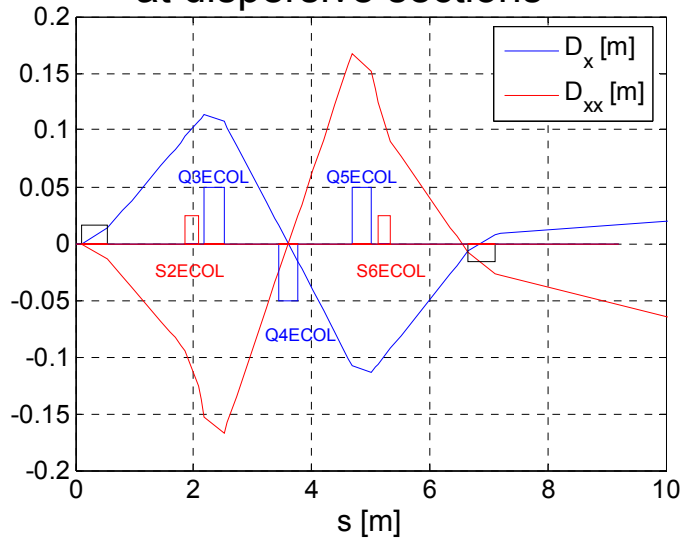
## Dipole field errors



## Trajectory errors and misalignments



## Quadrupole and sextupole field errors at dispersive sections



Other sources:

- any additional dipole field (e.g. coupler kicks)
- any additional quadrupole (and sextupole) field in dispersive sections

# Sensitivities for FLASH

Required amount of error to generate 10 mm of dispersion in the undulator (RMS)  
No orbit correction is performed  
(average results over 200 seeds)

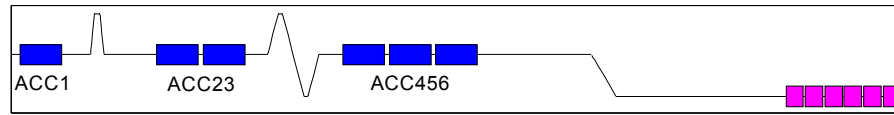
Error type	Required amount
<i>Quadrupole misalignment</i>	x: 17 $\mu\text{m}$ y: 18 $\mu\text{m}$
<i>Quadrupole field error</i>	1.31 %
<i>Quadrupole component in dipoles</i>	$4.1 \cdot 10^{-3} \text{ m}^{-2}$
<i>Vertical dipole misalignment</i>	215 $\mu\text{m}$
<i>Dipole field error</i>	0.13 %
<i>Cavity misalignment</i>	x: 2.0 mm y: 1.8 mm

**Quadrupole misalignments** are the most important dispersion sources  
**Collimator** is a critical area

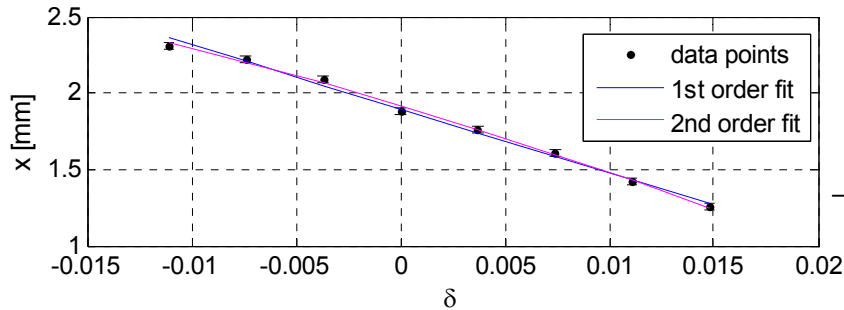
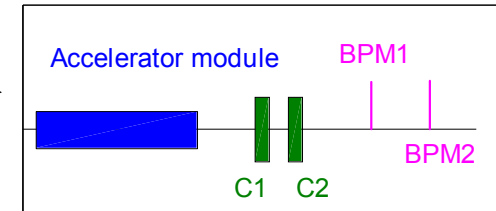
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# Dispersion measurement

It is based on measuring the orbit for different beam energies

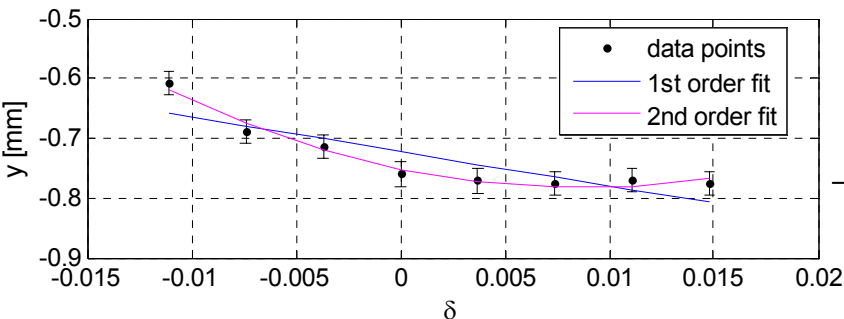


1. Change RF gradient of the module
2. Apply orbit correction to compensate RF steering effect
3. Read BPM positions downstream last correction BPM



$$x(s) = x_0 + D_x(s_0, s) \cdot \delta(s_0) + D_{xx}(s_0, s) \cdot \delta^2(s_0)$$

Dispersion



$$y(s) = y_0 + D_y(s_0, s) \cdot \delta(s_0) + D_{yy}(s_0, s) \cdot \delta^2(s_0)$$

# Dispersion measurement errors

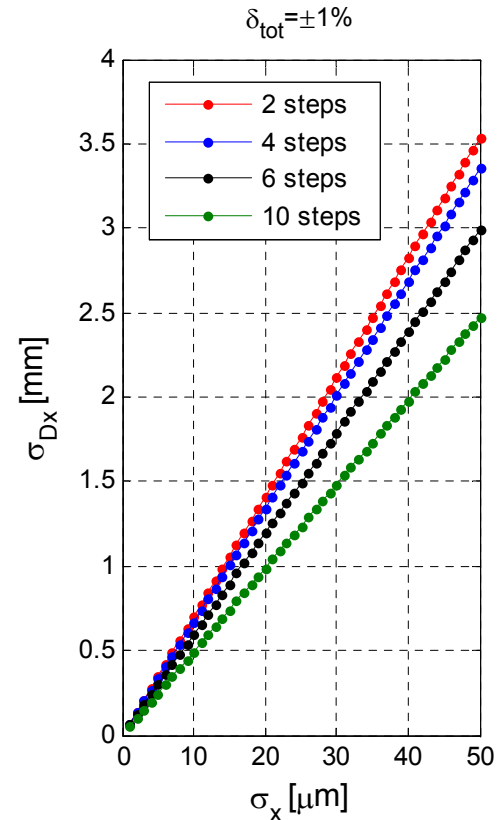
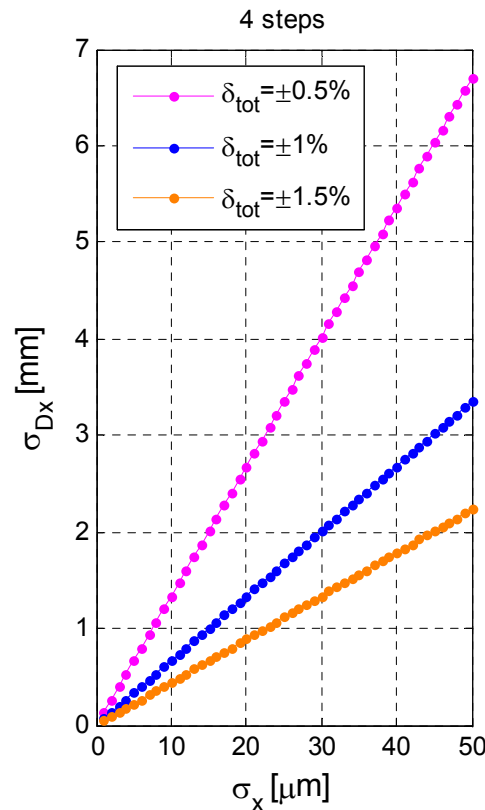
- Statistical errors

$$\sigma_{D_x} = \sqrt{\frac{\sum_i \frac{1}{\sigma_{x_i}^2}}{\sum_i \frac{1}{\sigma_{x_i}^2} \cdot \sum_i \frac{\delta_i^2}{\sigma_{x_i}^2} - \left(\sum_i \frac{\delta_i}{\sigma_{x_i}^2}\right)^2}}$$

$$\left. \begin{array}{l} \sigma_x = 20 : 50 \mu\text{m} \\ \delta_{\text{tot}} \approx \pm 1\% \\ 3 - 4 \text{ steps} \end{array} \right\} \rightarrow \sigma_{D_x} = 1 : 3 \text{ mm}$$

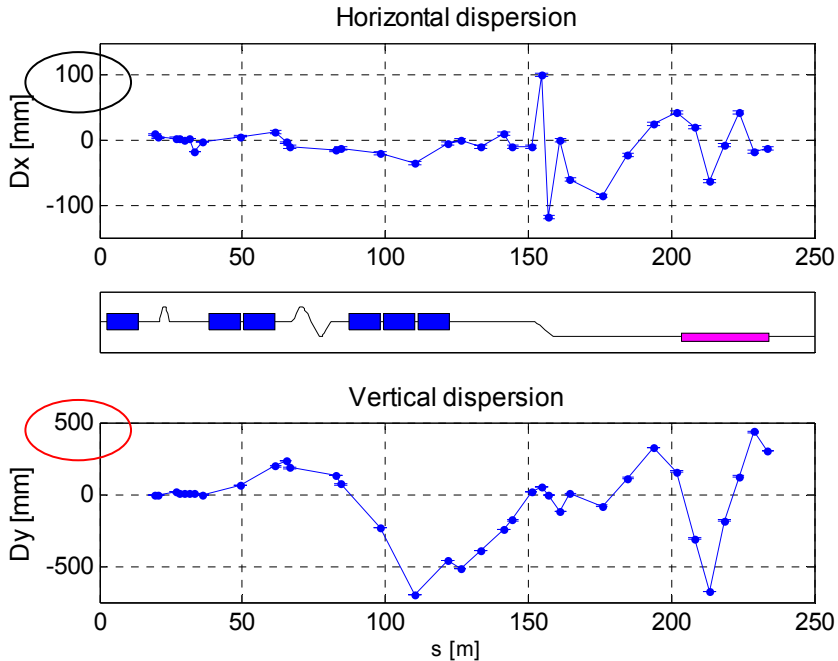
- Systematic errors:

- RF steering: corrected
- Calibration errors for  $\delta$ :  $< 0.3\%$
- BPM calibration errors:  $\sim 5\%$
- BPM nonlinearities: negligible if  $D = \pm 10 \text{ cm}$  (assuming no BPM off-set and  $\delta_{\text{tot}} = \pm 1\%$ )
- Drifts (negligible because of the short measurement time)

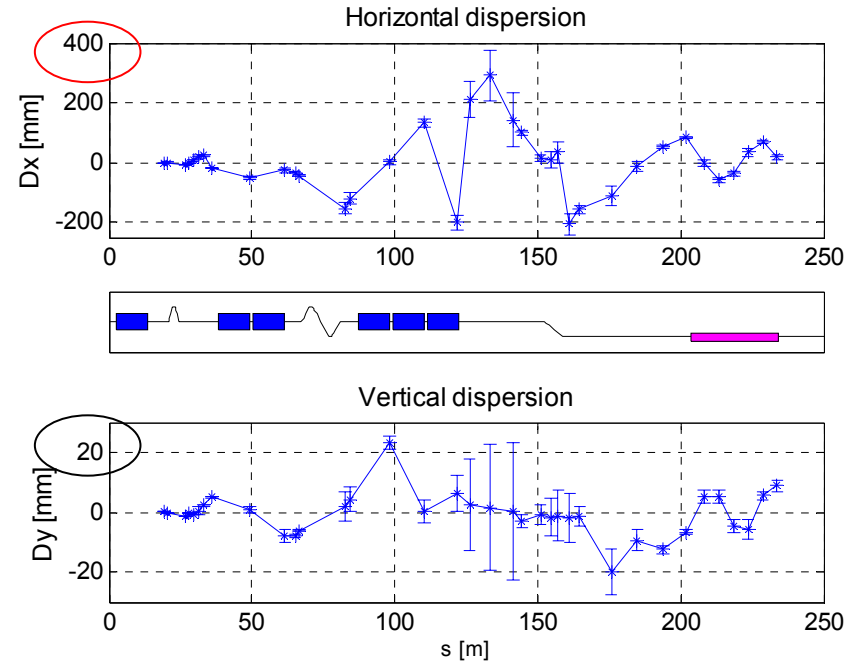


# Examples of measurements at FLASH

Day 1



Day 2 (SASE conditions)



Different errors change the spurious dispersion depending on the actual operating conditions of the accelerator, so dispersion must be measured and controlled frequently.

# Dispersion correction algorithm

It corrects both **orbit** and **dispersion**, using dipole magnets and quadrupole movers.

The optimal settings are calculated using the **orbit** and **dispersion** response matrices.

➤ Orbit response term  $O_{i,j} = \frac{\Delta x_i}{\Delta \theta_j}$       ➤ Dispersion response term  $\Delta_{i,j} = \frac{\Delta D_i}{\Delta \theta_j}$

$\Delta x_i / \Delta D_i$  -----> change of the orbit / dispersion at the BPM  $i$   
 $\Delta \theta_j$  -----> change of the kick angle of the steerer  $j$

$$\begin{pmatrix} \hat{O} \\ \hat{\Delta} \end{pmatrix} \cdot \Delta \vec{\theta} = \begin{pmatrix} \vec{x}_{ind} \\ \vec{D}_{ind} \end{pmatrix}$$

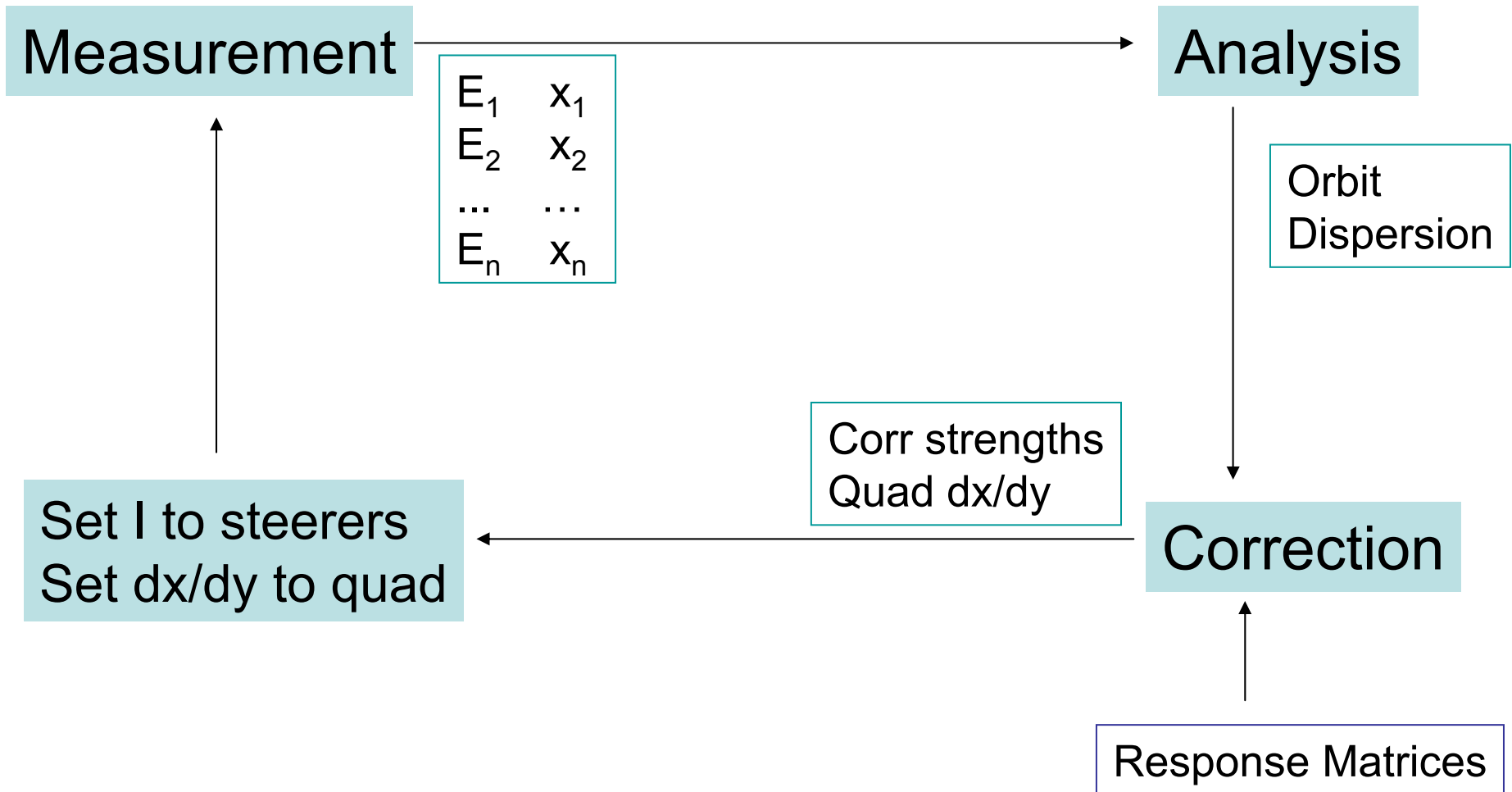
$$(1-w) \left\| \vec{x}_{meas} + \vec{x}_{ind} - \vec{x}_{gold} \right\|^2 + w \left\| \vec{D}_{meas} + \vec{D}_{ind} - \vec{D}_{gold} \right\|^2 = \min$$

*ind* = induced, *meas* = measured, *gold* = golden (target)

*w*: weighting factor ( $w = 0$  only orbit correction,  $w = 1$  only dispersion correction)



# Scheme for dispersion correction procedure



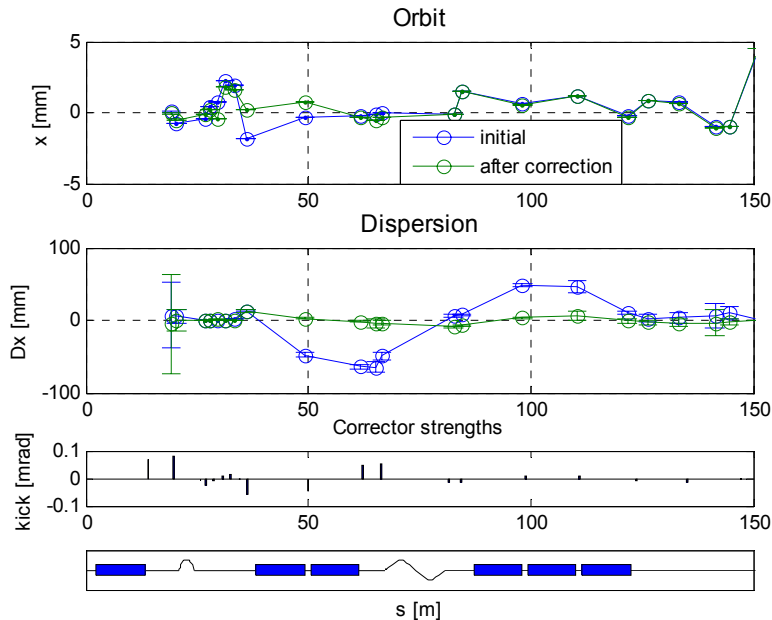
# Dispersion tool at FLASH

The dispersion measured from all accelerator modules can be kept below 5 mm (RMS) in both planes.

## Examples

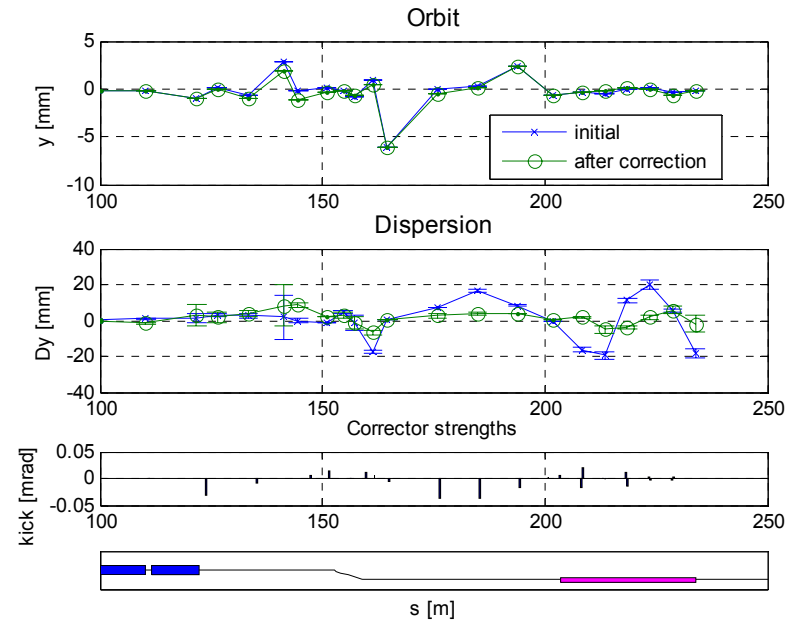
From **ACC1**

$D_x$  corrected from 30 to 5 mm (RMS)



From **ACC456**

$D_y$  corrected from 17 to 4 mm (RMS)

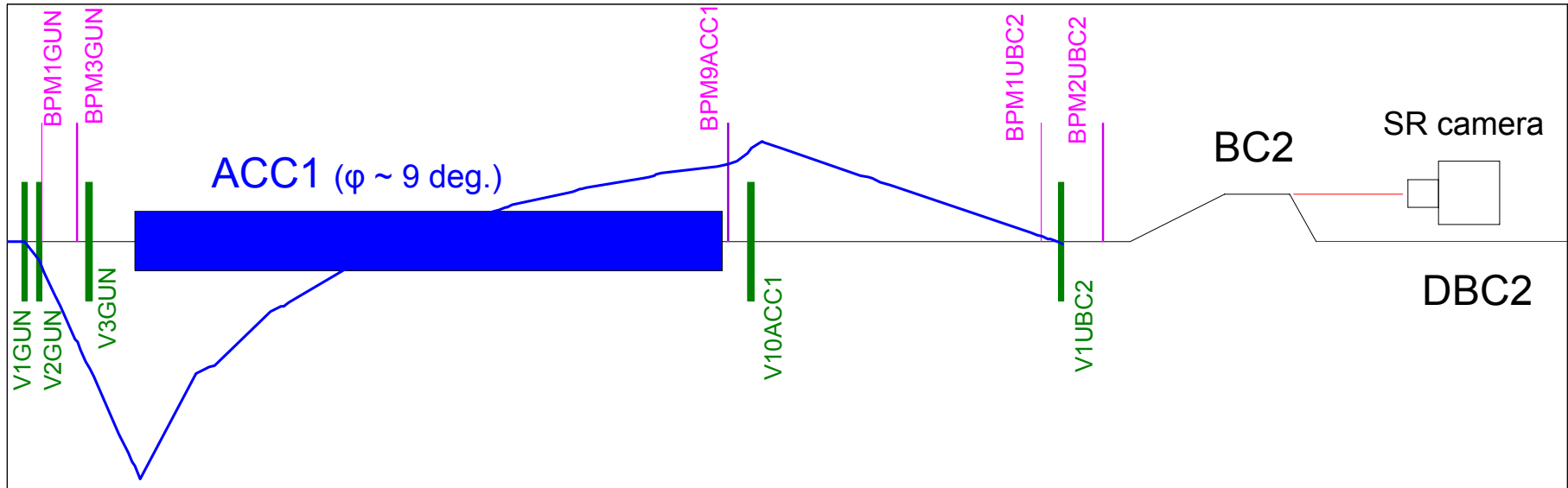


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# Beam tilt experiment

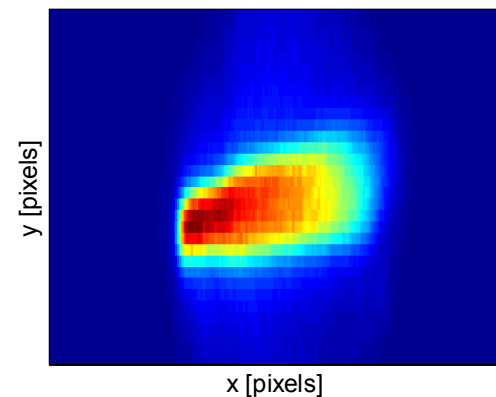
(with C. Gerth and K. Hacker)

Studies on how vertical dispersion tilts the beam at BC2 and causes an increase of the emittance. The dispersion is generated by applying vertical trajectory bumps through ACC1.



Bump	Relative bump amplitude at BMP9ACC1 [mm]
ref. ( $y = -2.8 \text{ mm}$ )	0.0
1	-5.3
2	-3.1
3	-2.0
4	1.7
5	3.5
6	4.6

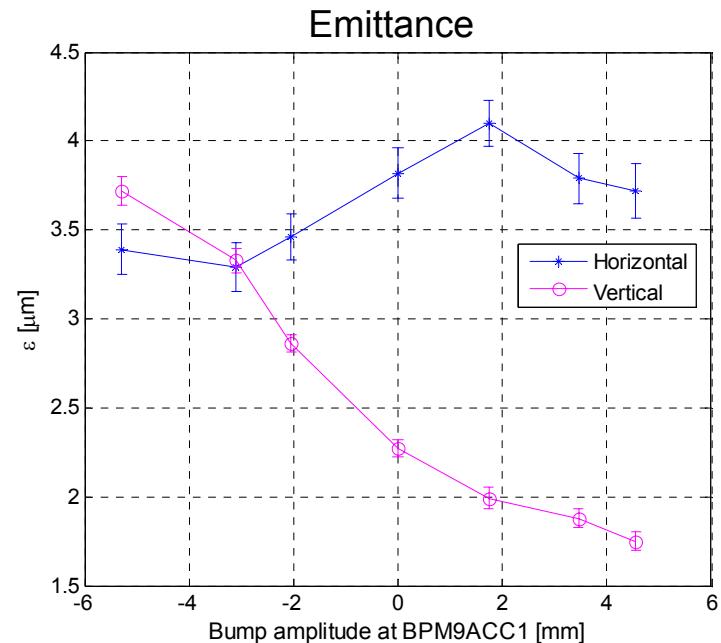
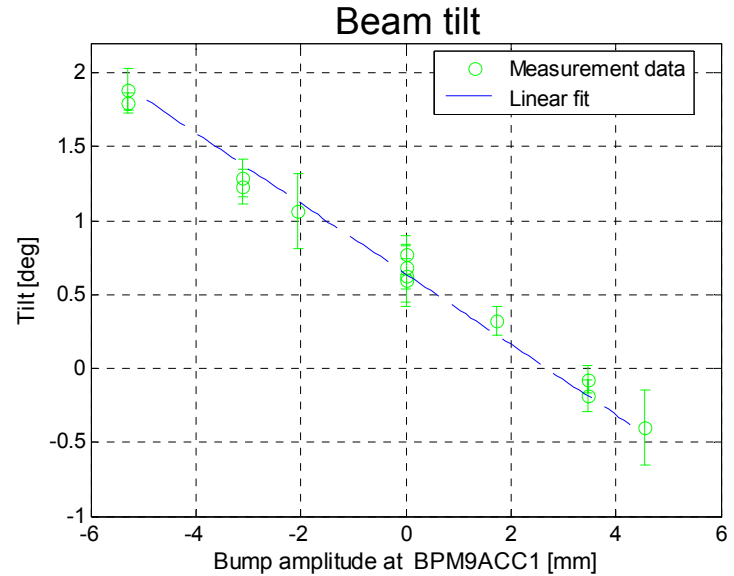
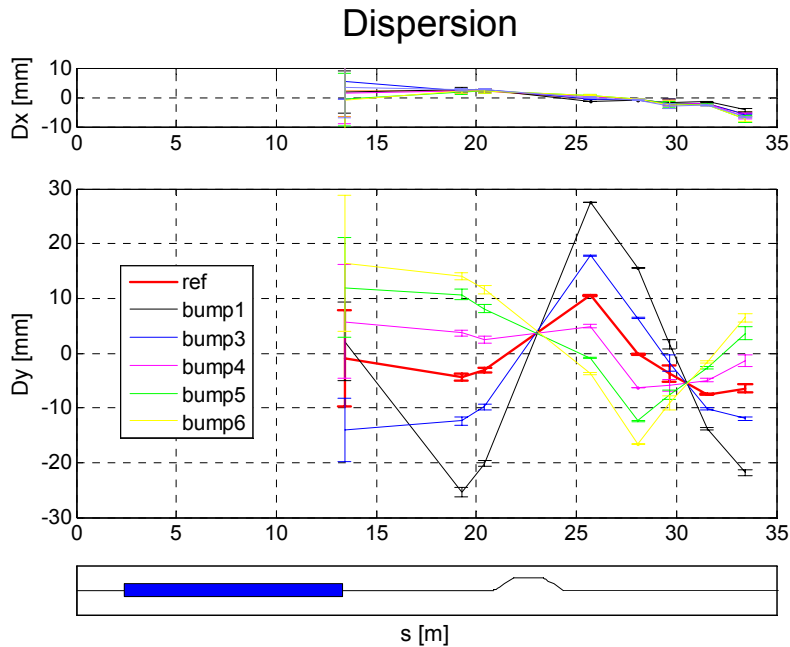
Image with SR camera



# Beam tilt experiment. Measurements.

Measurements per each bump:

1. Dispersion from ACC1
2. Beam tilt at BC2
3. Projected emittance at DBC2

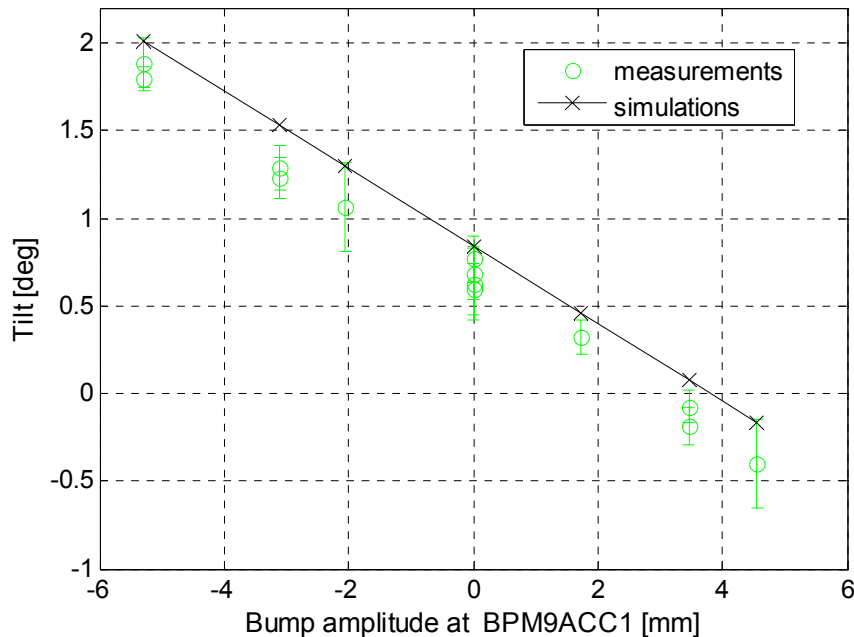


# Beam tilt experiment. Simulations.

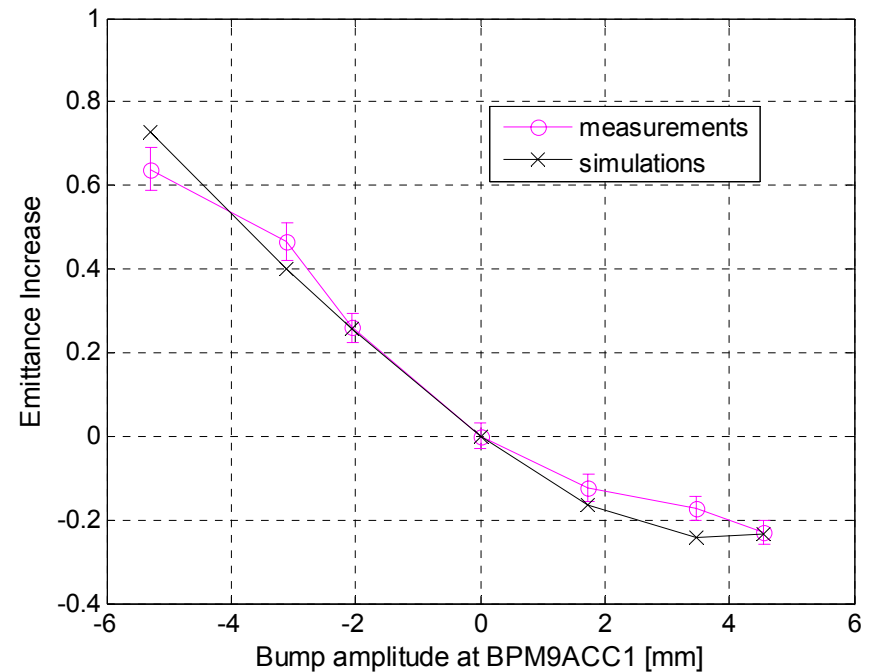
Simulations done with elegant

Initial vertical trajectory offset of 3.0 mm reproduces the measurements  
(orbit, dispersion, beam tilt and emittance)

Beam tilt



Emittance

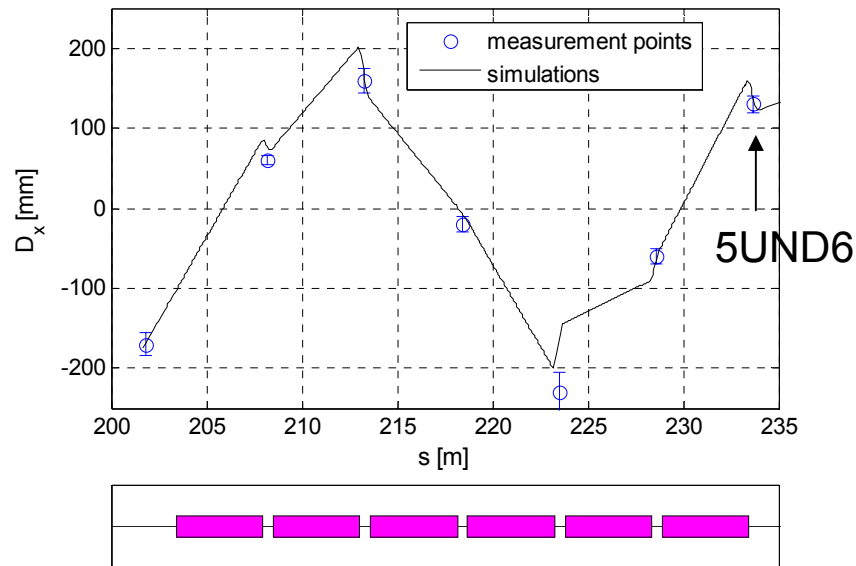


- The required steering to improve the beam quality was counteracting a vertical kick which is in accordance with a relative solenoid misalignment of  $\sim 300 \mu\text{m}$ .

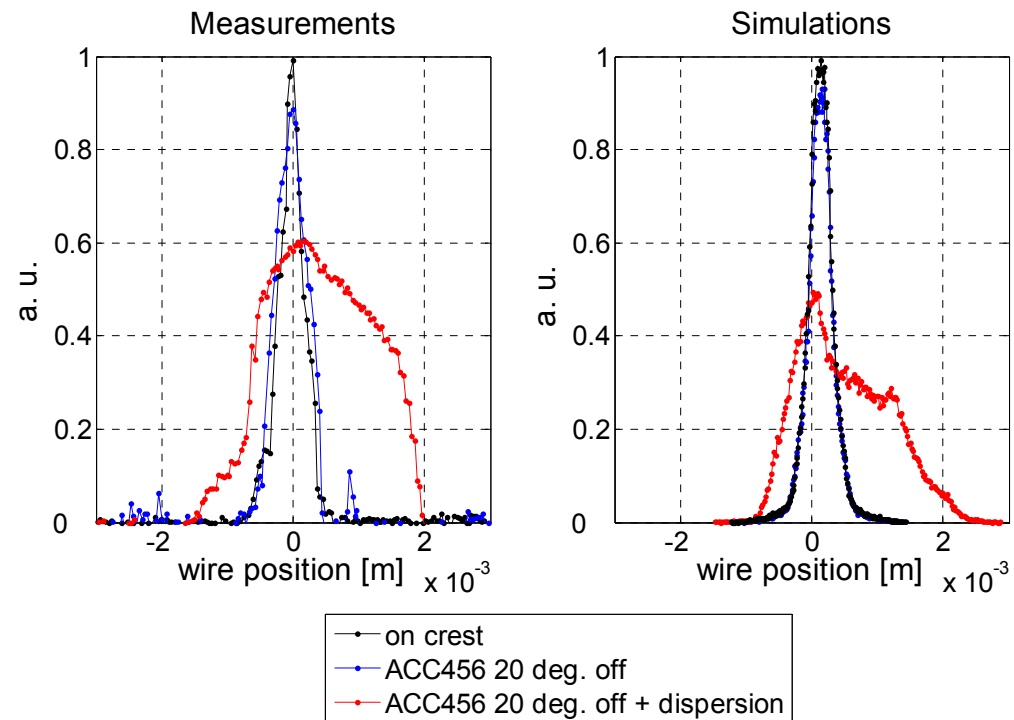
# Dispersion generation in the undulator

Current of Q3/5ECOL was decreased by 10%  $\rightarrow D_x = 140$  mm (RMS)

## Dispersion generation

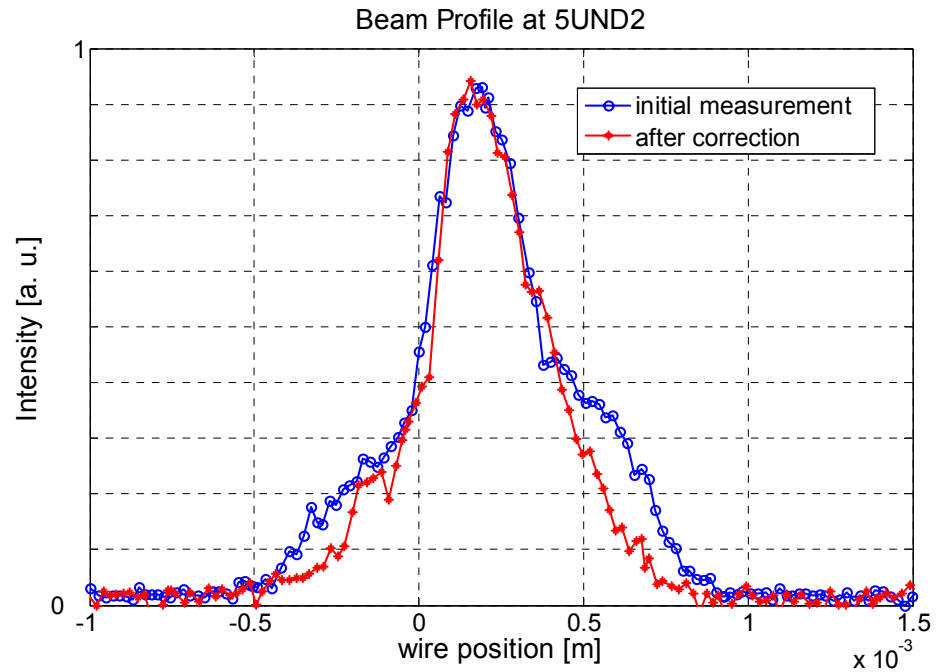
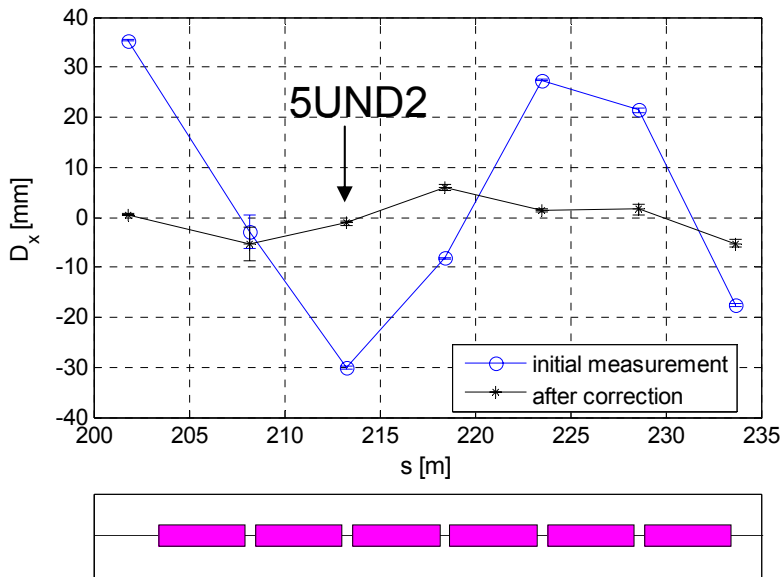


## Profile at 5UND6 (50 $\mu$ m W - wire)



# Dispersion correction in the undulator

Correction of  $D_x$  in the undulator from 22 to 4 mm (RMS)  
Beam emittance reduced by 20% (from 5.8 to 4.7  $\mu\text{m}$ )  
Beam shoulders vanished due to dispersion correction





# Emittance transport

(with F. Loehl and K. Honkavaara)

Results of projected emittance at FLASH for 2 different days after **linac optimization** (i.e. orbit and dispersion correction)

Normalized values for 90% beam intensities

Design emittance is 2  $\mu\text{m}$

Day	17-02-2007		08-09-2007	
Section	$\epsilon_x$ [ $\mu\text{m}$ ]	$\epsilon_y$ [ $\mu\text{m}$ ]	$\epsilon_x$ [ $\mu\text{m}$ ]	$\epsilon_y$ [ $\mu\text{m}$ ]
DBC2	<b>2.4</b>	<b>2.5</b>	<b>2.2</b>	<b>2.1</b>
Seeding	<b>2.0</b>	<b>2.2</b>	<b>1.8</b>	<b>2.3</b>

Statistical measurement errors = 0.1  $\mu\text{m}$

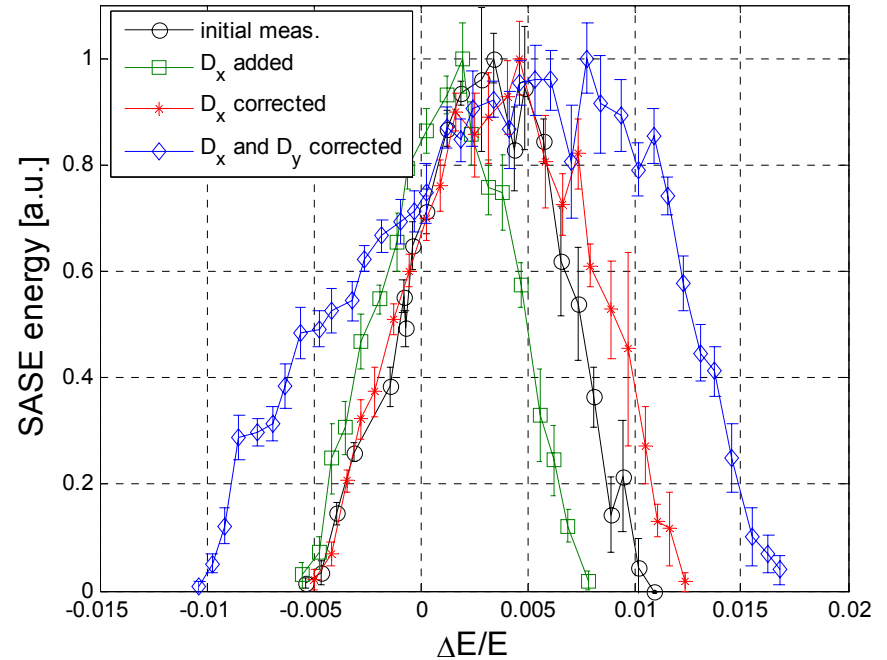
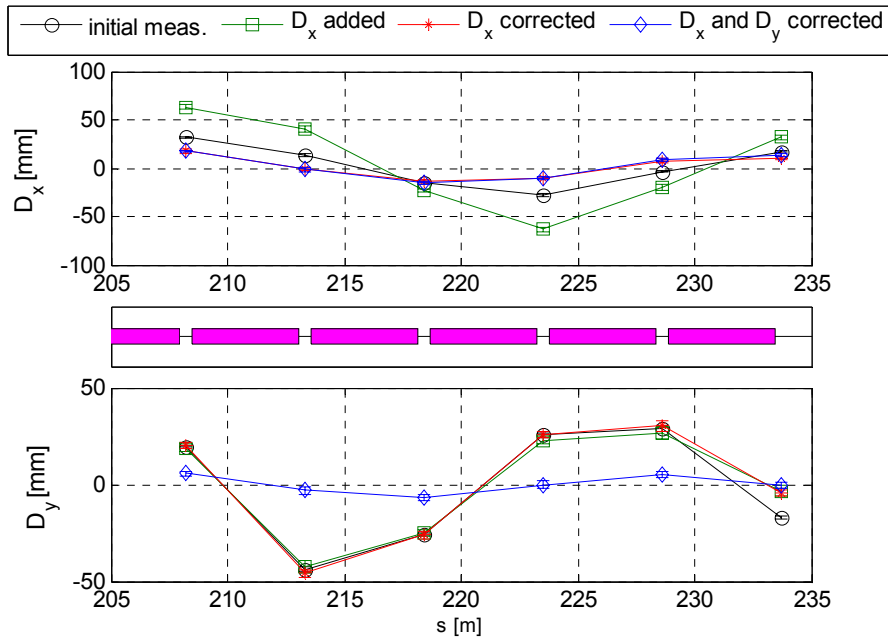
Systematic errors > 0.1  $\mu\text{m}$

Dispersion correction (to less than 10 mm) is necessary for the conservation of the projected emittance

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  - SASE sensitivity to electron beam energy offset
  - Dispersion impact on SASE spectrum
- Conclusion

# SASE sensitivity to electron beam energy offset. Measurements.

Motivation: show that by correcting the dispersion inside the undulator, the SASE power jitter due to electron beam energy fluctuations decreases



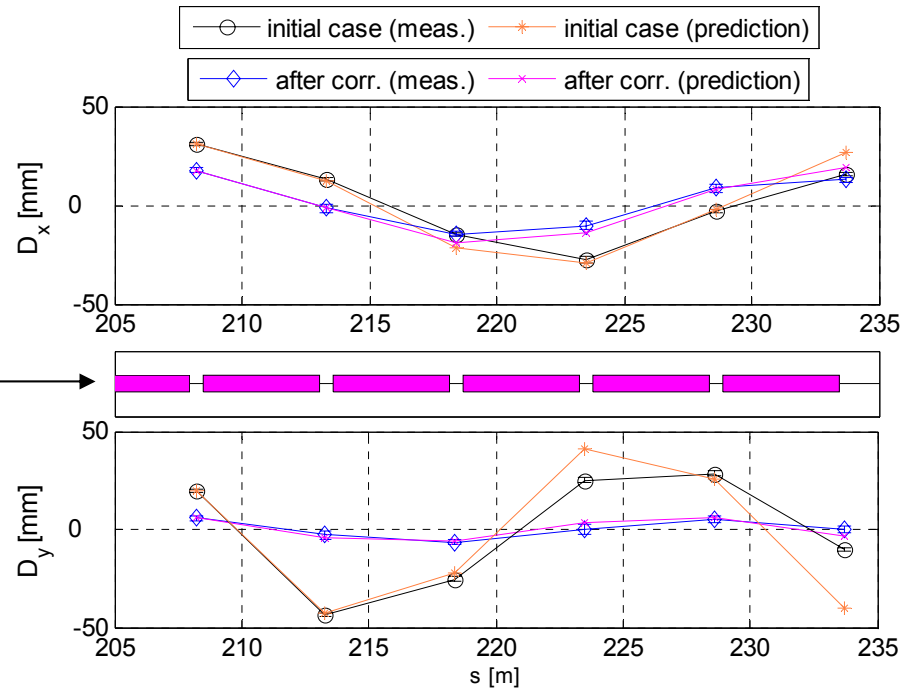
Condition	$D_x$ (RMS)	$D_y$ (RMS)	FWHM in $\Delta E/E$
Initial measurement	22 mm	30 mm	0.82 %
$D_x$ generated	48 mm	28 mm	0.74 %
$D_x$ corrected	12 mm	31 mm	1.06 %
$D_x$ and $D_y$ corrected	11 mm	5 mm	1.72 %

# SASE sensitivity to electron beam energy offset. Simulations.

Simulations done with Genesis 1.3 (only initial and last cases)

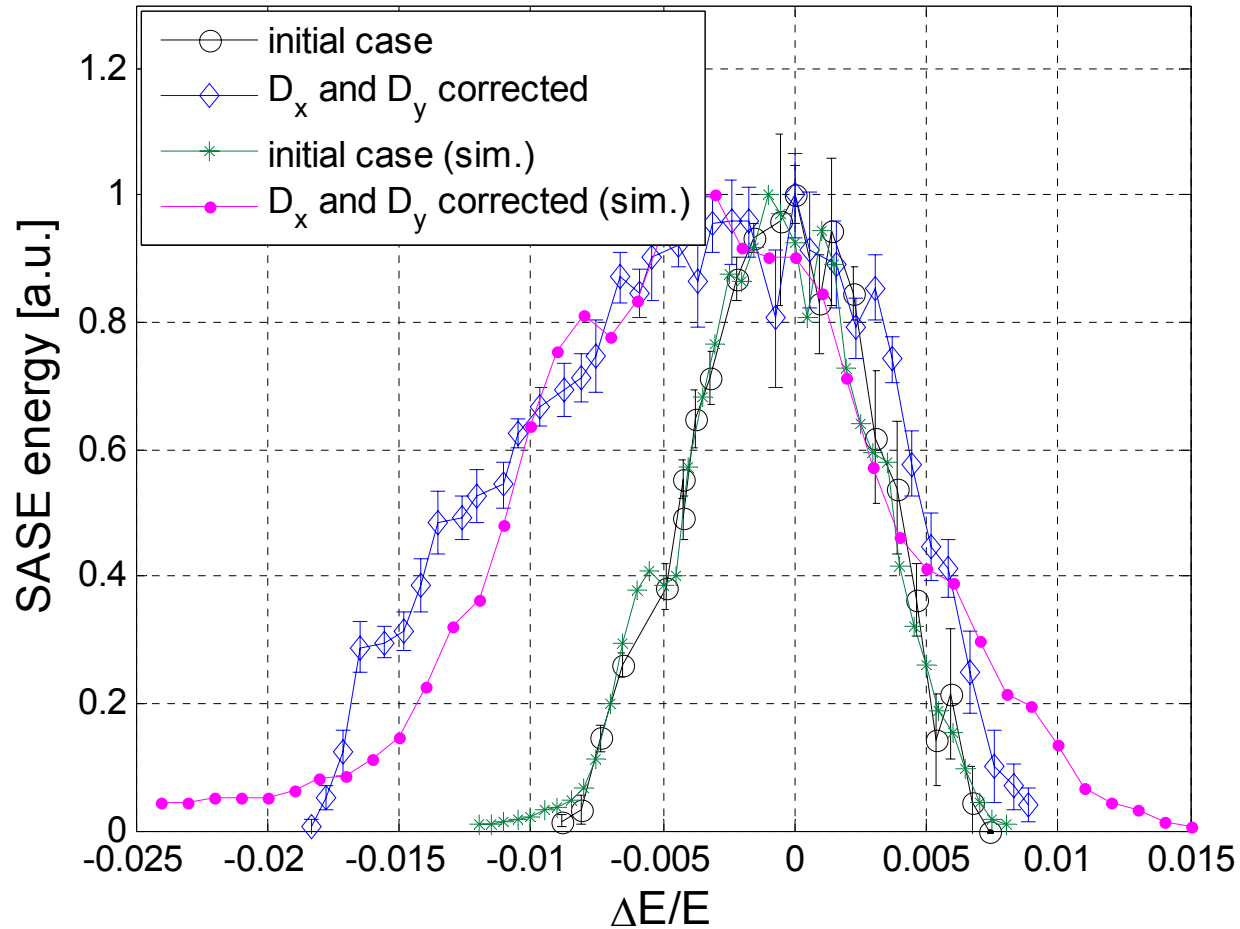
Effects { trajectory changes:  
 $\Delta x, y = D_{x,y} \cdot \delta$   
 $\Delta x', y' = D'_{x,y} \cdot \delta$   
 energy: - optics  
 - undulator field  
 - undulator focusing

Dispersion along the undulator: measurements and predictions according to the dispersion functions at the undulator entrance.

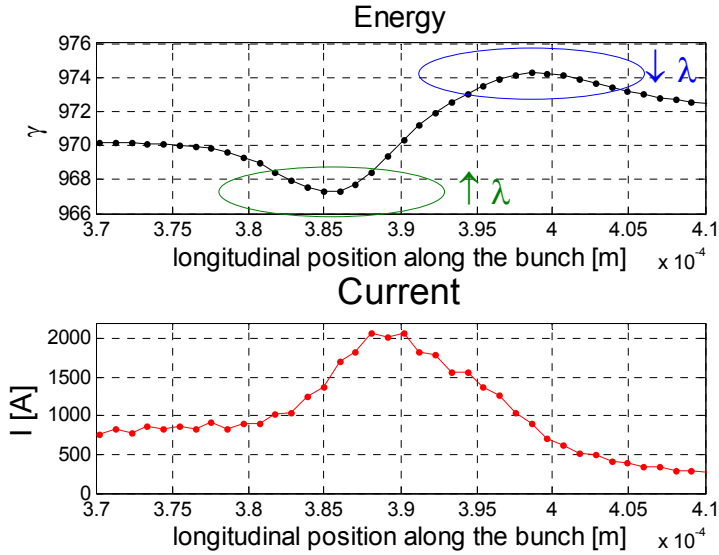


No dispersion is generated inside the undulator

# SASE sensitivity to electron beam energy offset. Measurements and simulations.



# Dispersion impact on the SASE spectrum

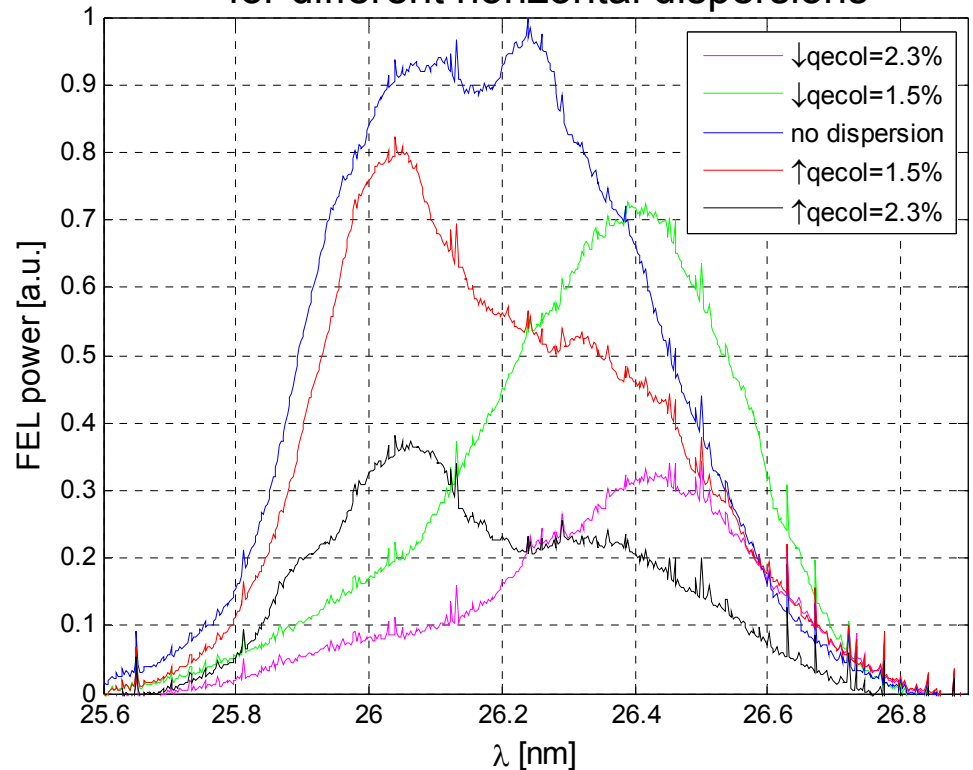


Dispersion deviates off-energy particle trajectories:  
 { FEL power ↓  
 spectrum bandwidth ↓

QECOL\*1.01 →  $D_x = 10$  mm (RMS)

$|D_x| > 0 \rightarrow$  FEL power ↓  
 QECOL ↑ →  $\lambda_c$  ↓  
 QECOL ↓ →  $\lambda_c$  ↑

Measurements of SASE spectrum for different horizontal dispersions



# Dispersion impact on the SASE spectrum. Simulations with a Gaussian electron beam

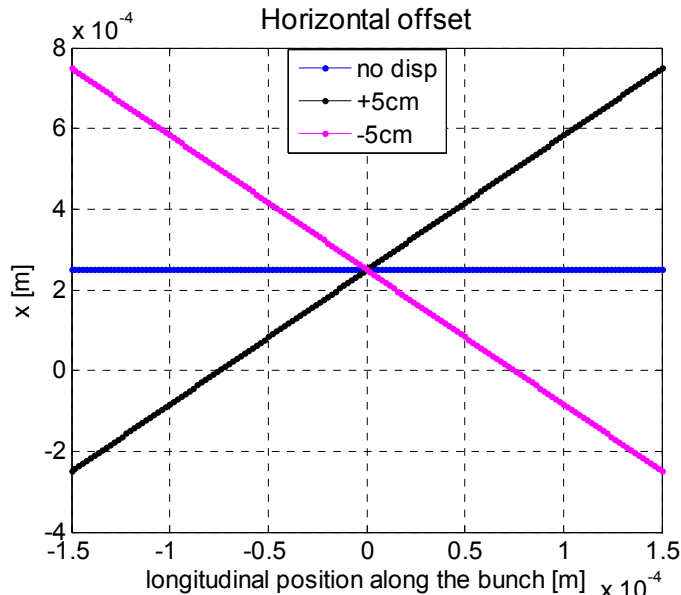
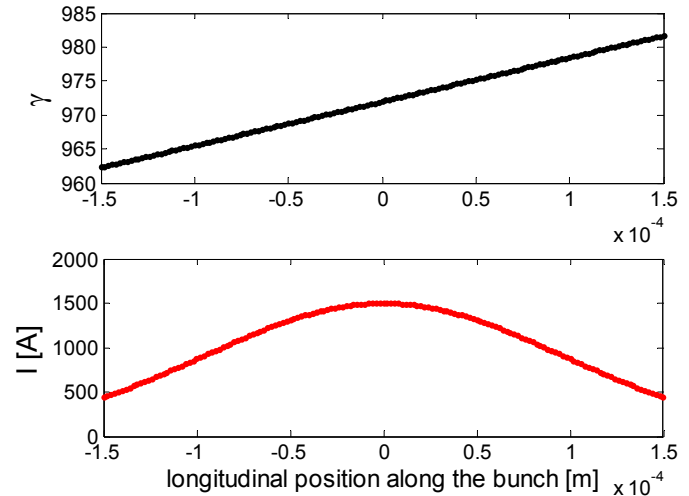
Study restricted to the impact of  $D_x$  and  $x$

3 dispersion scenarios:  $D_x = 0$   
 $D_x = +5 \text{ cm}$   
 $D_x = -5 \text{ cm}$

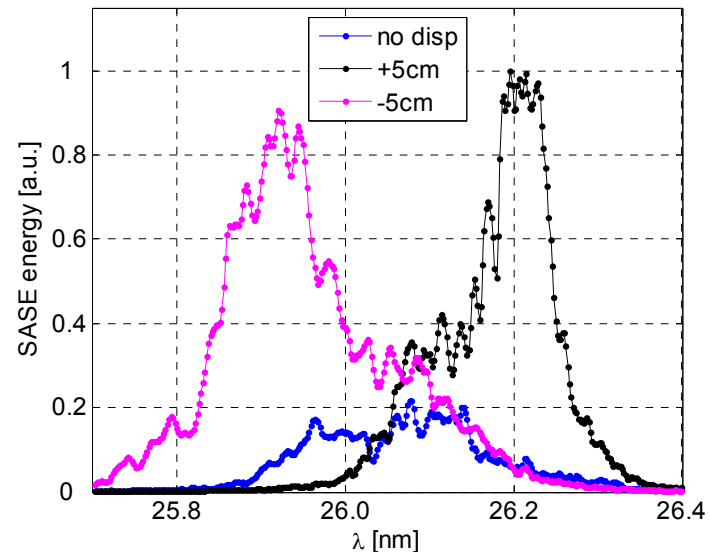
Initial offset distributions:

1. Zero offset along the bunch
2. Non-zero offset along the bunch
3. Quadratic x-energy correlation

Input beam properties



Radiation spectrum



# Dispersion impact on the SASE spectrum. Realistic Simulations

Electron properties obtained from s2e simulations (M. Dohlus)

Considered cases:

- No dispersion
- Changes of QECOL of  $\pm 1.5\%$

Trajectory changes:

$$x(i) = x_0(i) + D_x \cdot \delta(i)$$

$$x'(i) = x'_0(i) + D'_x \cdot \delta(i)$$

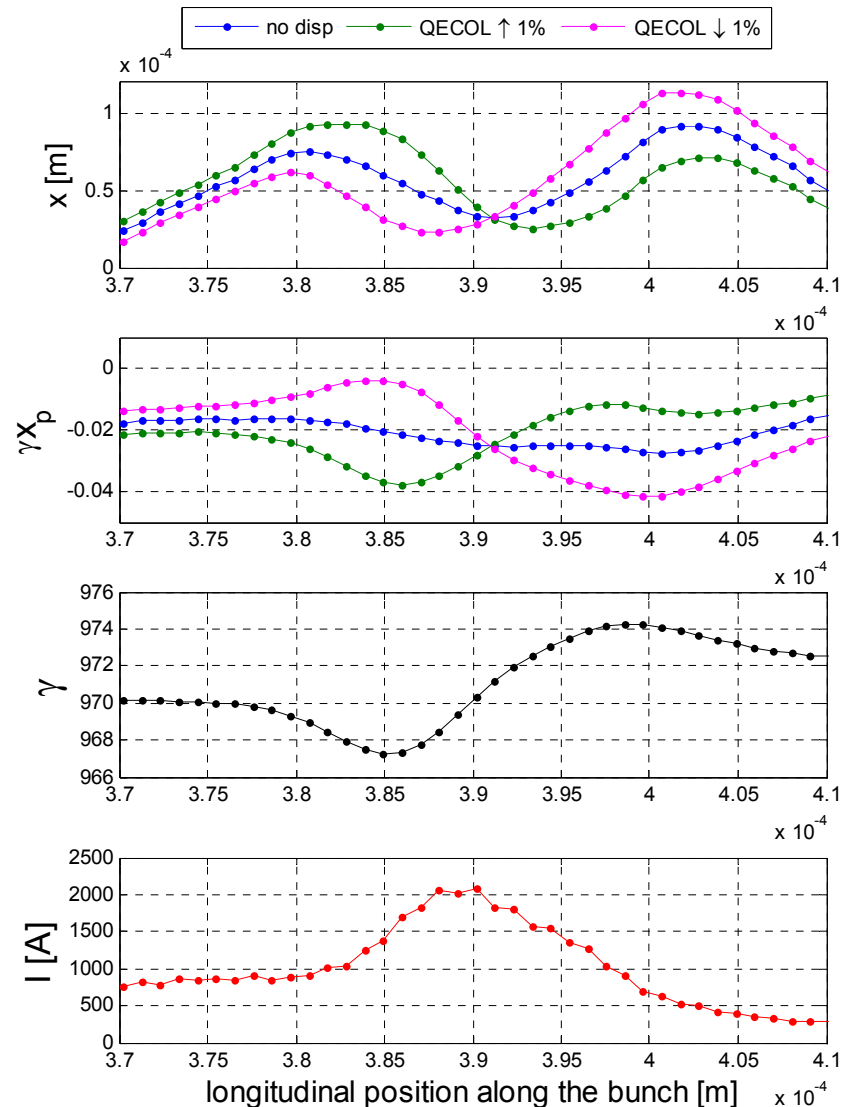
There is a 2<sup>nd</sup> order correlation between x and energy (e.g. due to CSR effects).

In addition:

$$x_0 = 50 \mu\text{m}$$

$$x'_0 = -20 \mu\text{rad}$$

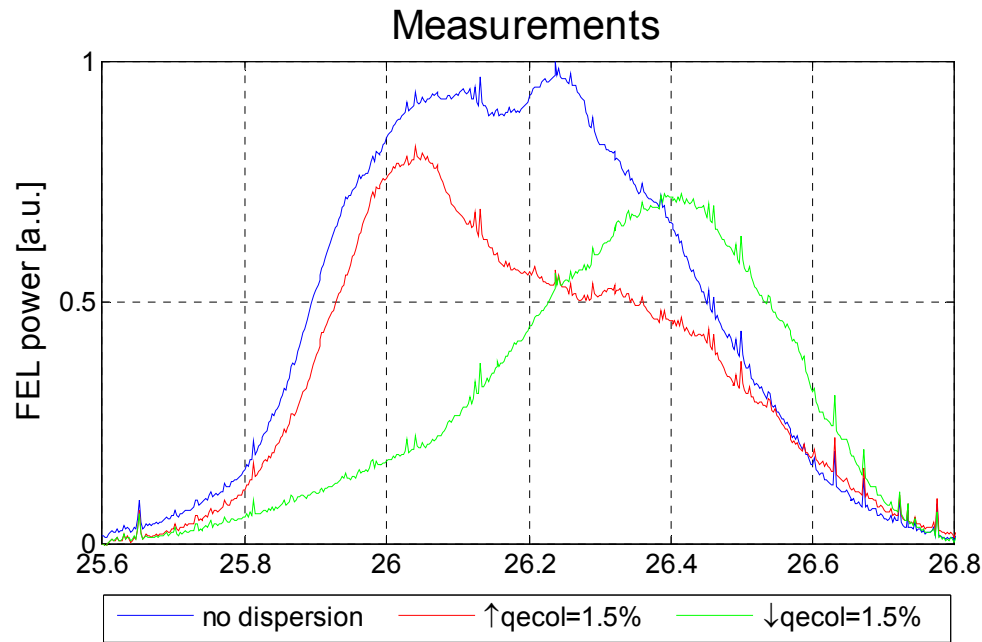
x and x' along the bunch





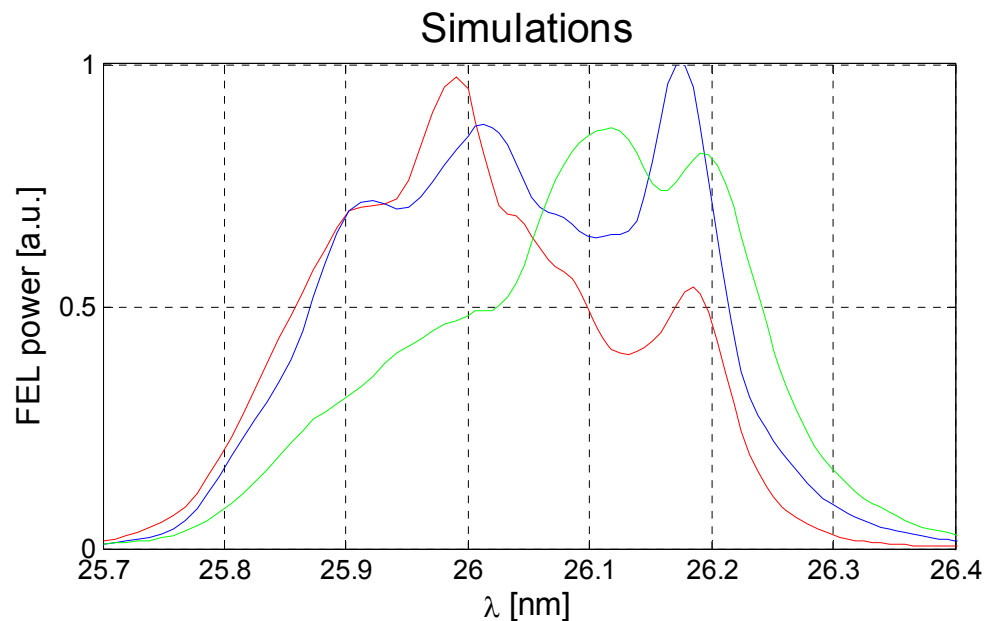
# Dispersion impact on the SASE spectrum

## Measurements versus simulations



Qualitative agreement

$|D_x| > 0 \rightarrow \text{FEL power} \downarrow$   
 $Q_{\text{ECOL}} \uparrow \rightarrow \lambda_c \downarrow$   
 $Q_{\text{ECOL}} \downarrow \rightarrow \lambda_c \uparrow$



Difference: wavelength range is bigger in the measurements (due to a bigger energy chirp)

- Introduction
- Generation mechanisms of dispersion
- Measurement and correction
- Effects on transverse beam quality at FLASH
- Effects on FEL performance at FLASH
- **Conclusion**

# Conclusion

- A method to measure and correct dispersion has been presented. A tool based on this method able to correct the dispersion down to 5 mm has been implemented at FLASH.
- Dispersion correction is a key issue for the optimization of the transverse beam quality at linac-based FEL facilities.
- The SASE power jitter due to electron energy fluctuations was decreased by correcting dispersion.
- The presence of dispersion reduces the FEL power and makes the radiation spectrum narrower.
- It has been shown that dispersion can be used to shift the central wavelength of the SASE spectrum at FLASH.

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