



Transverse emittance measurements at PITZ

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19th of February 2008

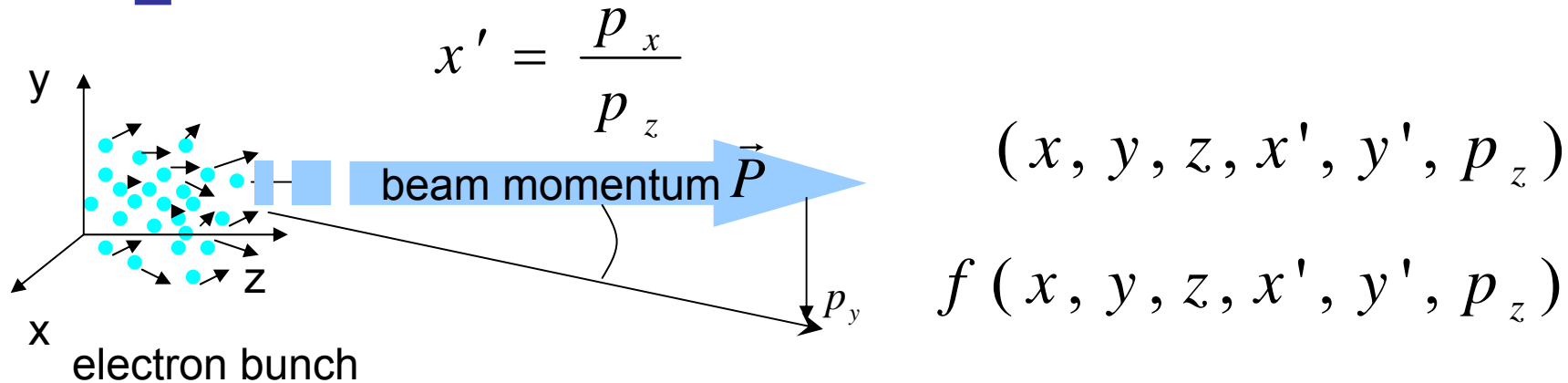
Joint DESY and University of Hamburg
Accelerator Physics Seminar

Outline

- Emittance of the electron beam
- Motivation
 - SASE FEL
 - FLASH, XFEL and PITZ
- PITZ in details
 - hardware setup, operation parameters
- Emittance Measurement SYstem (EMSY)
 - optimization and error analysis
- Emittance measurement results at PITZ
 - optimized parameters
 - two different gun cavities
- Discussion

Emittance

introduction



emittance is related to volume/area occupied by the electrons,
the smaller - the better

- central moments $\langle \dots \rangle$
- 2D projections $f(x, x')$

→ covariance matrix

$$\Sigma_x = \begin{pmatrix} \langle x^2 \rangle & \langle xx' \rangle \\ \langle xx' \rangle & \langle x'^2 \rangle \end{pmatrix}$$

- matrix representation
- transfer matrices

$$\Sigma'_x = R \cdot \Sigma_x \cdot R^T;$$

$$R = D_1 \cdot Q_1 \cdot D_2 \cdot Q_2 \cdot \dots \cdot D_n \cdot Q_n \dots$$

Emittance

definition

$$\Sigma_x = \begin{pmatrix} \langle x^2 \rangle & \langle xx' \rangle \\ \langle xx' \rangle & \langle x'^2 \rangle \end{pmatrix}$$

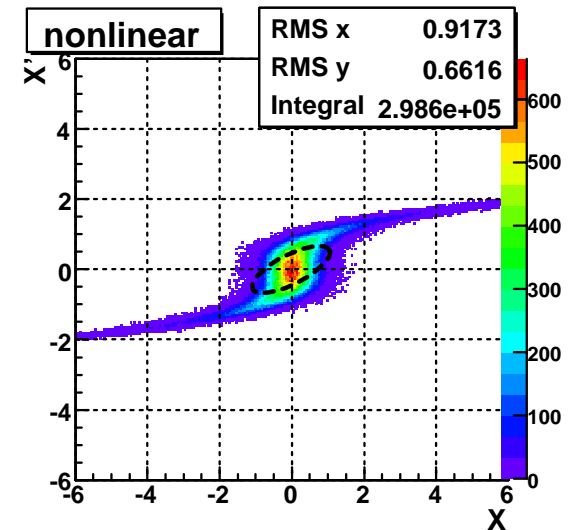
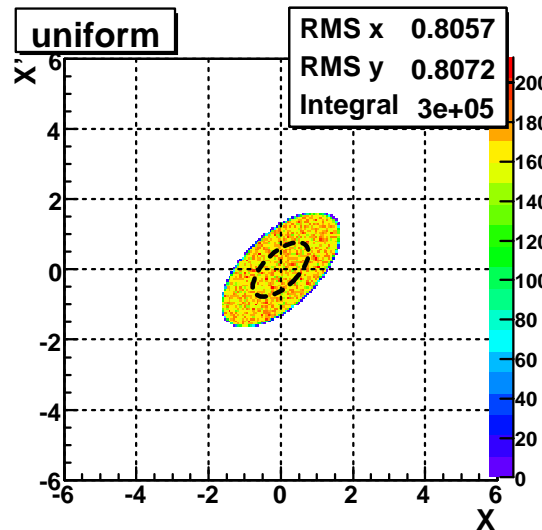
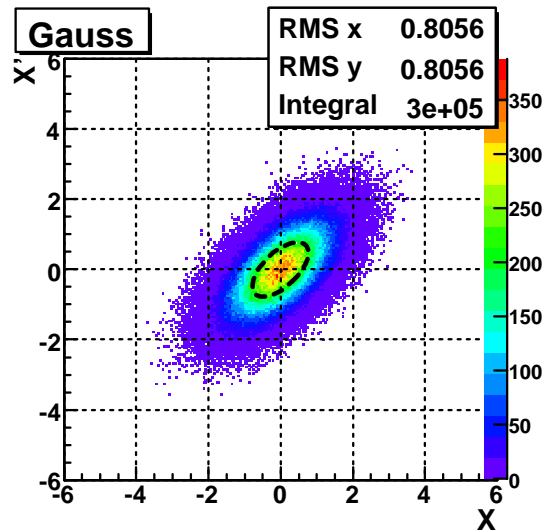
← covariance matrix

$$\det|\Sigma_x| = \varepsilon_{rms}^2$$

$$\det|\Sigma_x| \cdot \beta\gamma = \varepsilon_{rms,n}^2$$

RMS normalized emittance:

$$\varepsilon_{x,rms} = \beta\gamma \cdot \sqrt{\langle x^2 \rangle \cdot \langle x'^2 \rangle - \langle xx' \rangle^2}$$



European XFEL design parameters

■ Electron beam

- high peak current
- short bunch
- small emittance

~5 kA
20 μm
1.4 mm.mrad

■ Undulator

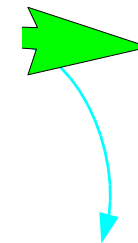
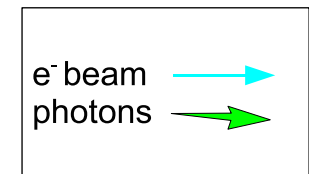
- strong field
- precise alignment
- very long

1.5 T
32 $\mu\text{m}/260\text{m}$
100^s m

■ SASE FEL

- short wavelength
- high brilliance
- ultra short pulses

0.1 nm
10³³ photons/s/mm²/mrad²/0.1%
< 100 fs

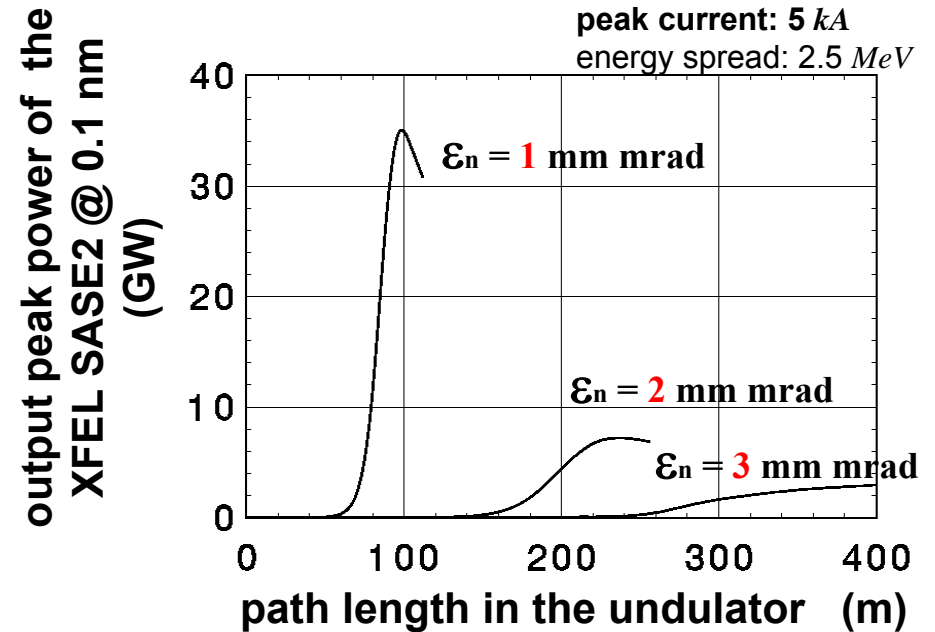
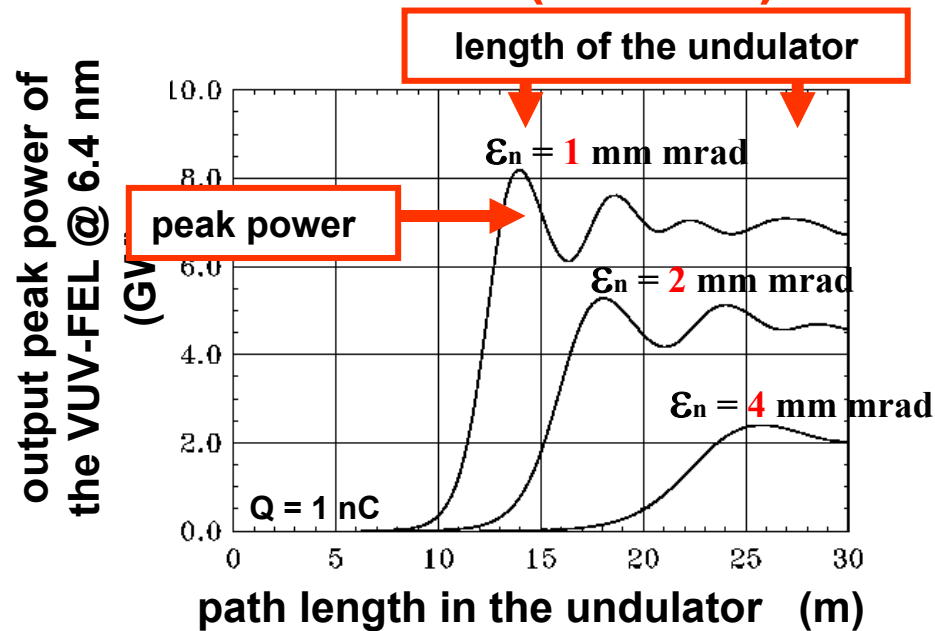


Emittance

the smaller-the better

VUV-FEL (FLASH)

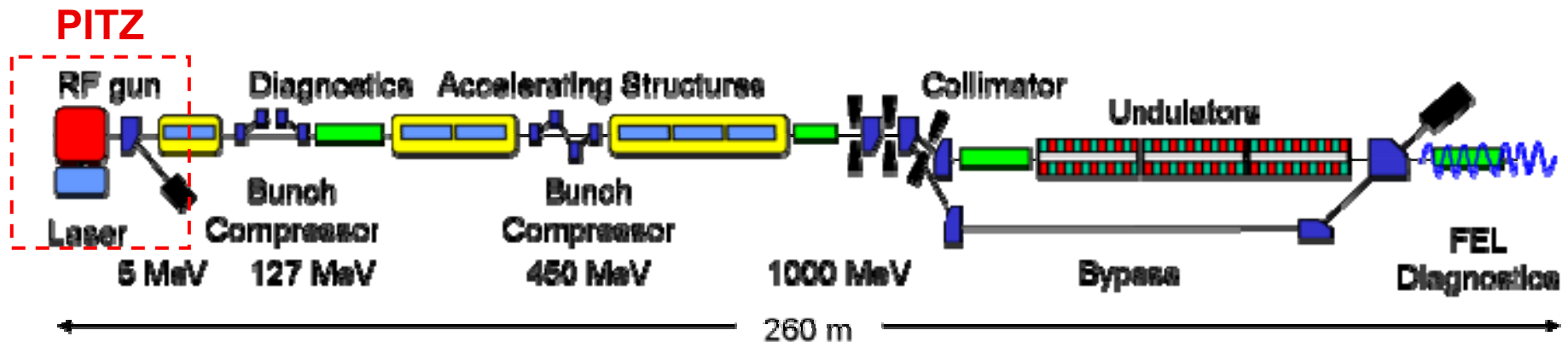
XFEL



- **XFEL goal:** 0.9 mm mrad@injector \Rightarrow 1.4 mm mrad@undulator
- **if even smaller emittance \Rightarrow new horizons:**
shorter wavelength, higher repetition rate

FLASH layout

- e^- source
- pre acceleration
- bunch compression
- further acceleration compression
- final acceleration
- collimation and undulation



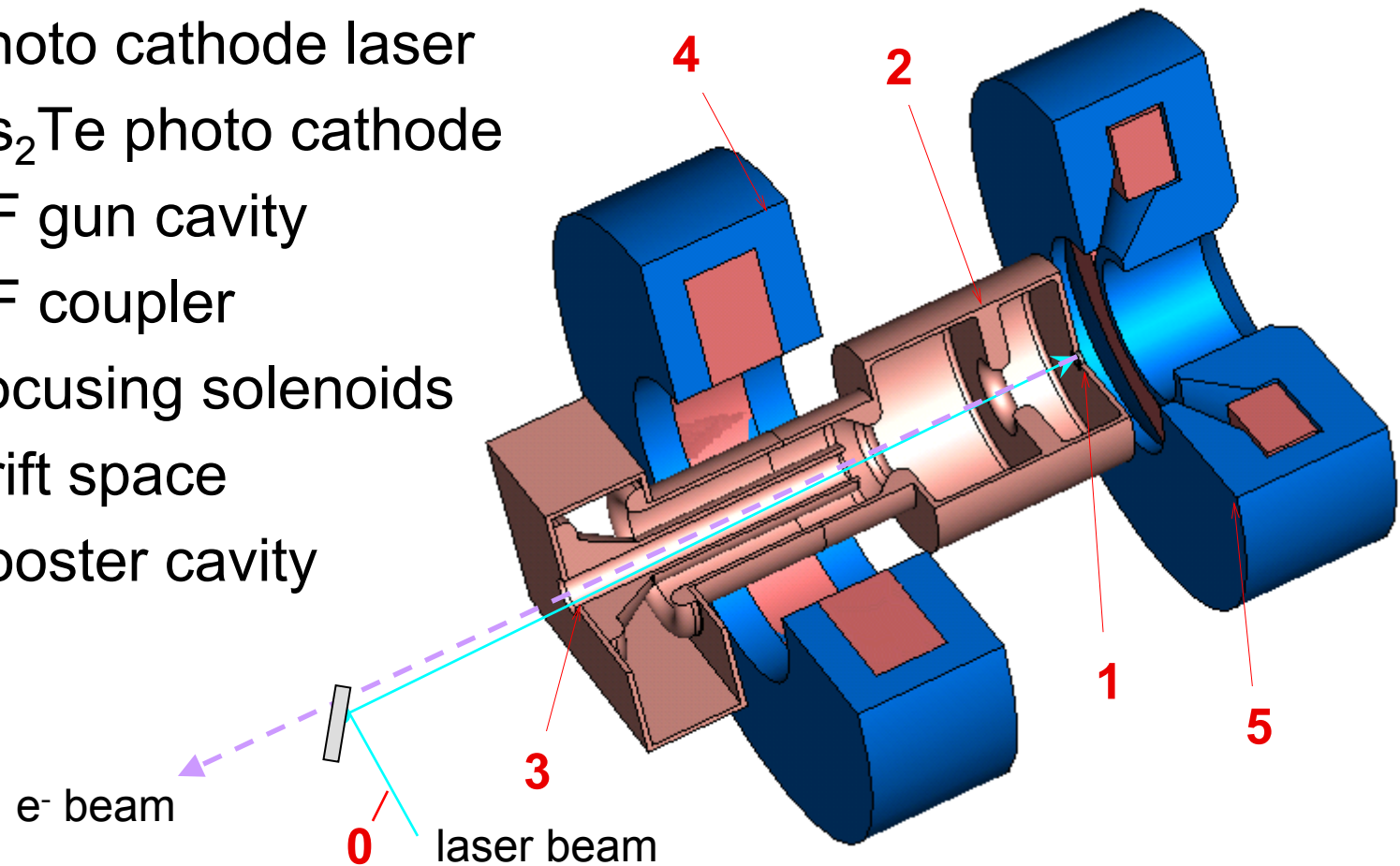
PITZ

- Photo Injector Test-facility at DESY in Zeuthen



RF photo-injector

0. Photo cathode laser
 1. Cs₂Te photo cathode
 2. RF gun cavity
 3. RF coupler
 - 4, 5. Focusing solenoids
- Drift space
Booster cavity



Extraction from Cs₂Te cathode

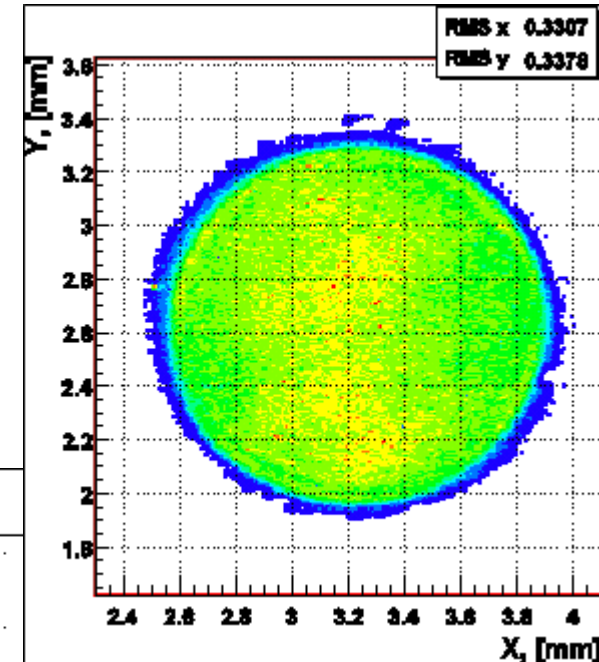
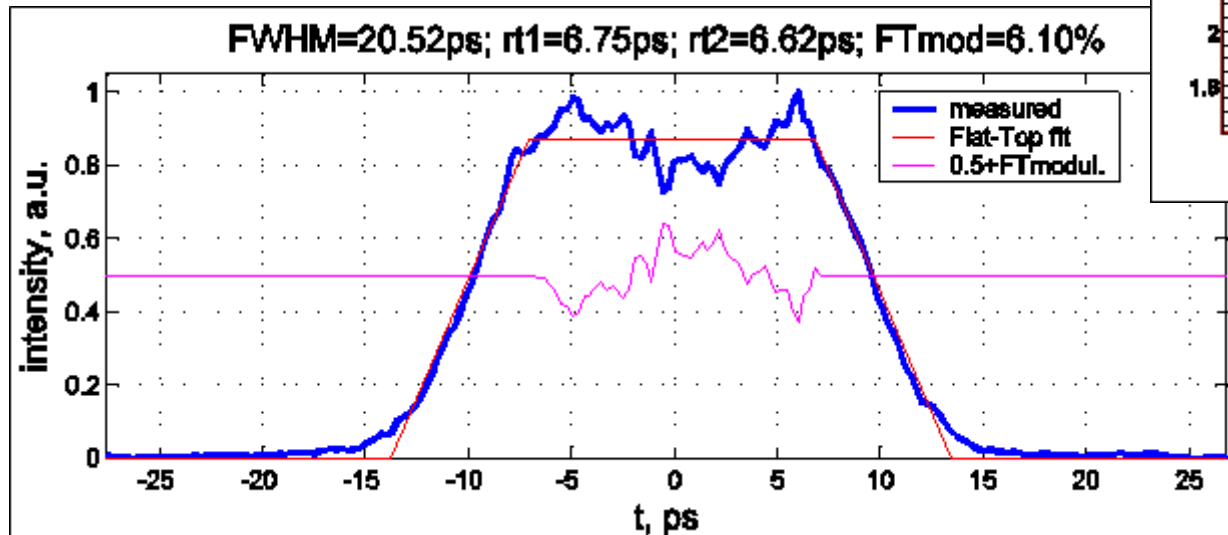
- photo effect - quantum efficiency of Cs₂Te cathode (Q.E.) etc.
- “Schottky effect” – lowering the potential barrier to the vacuum
- thermal emittance – remnant kinetic energy after the electron extraction
- mirror and space charge

Extraction

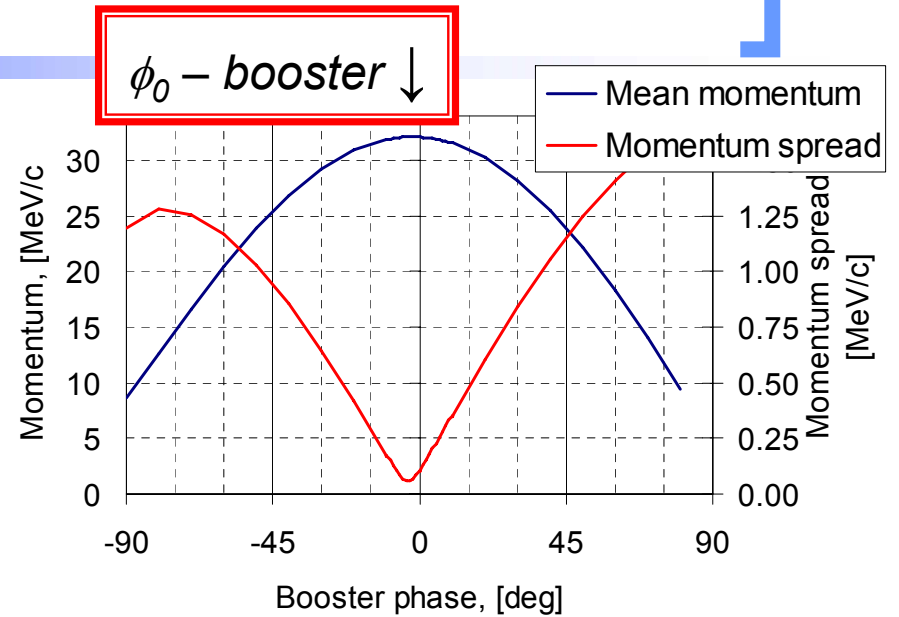
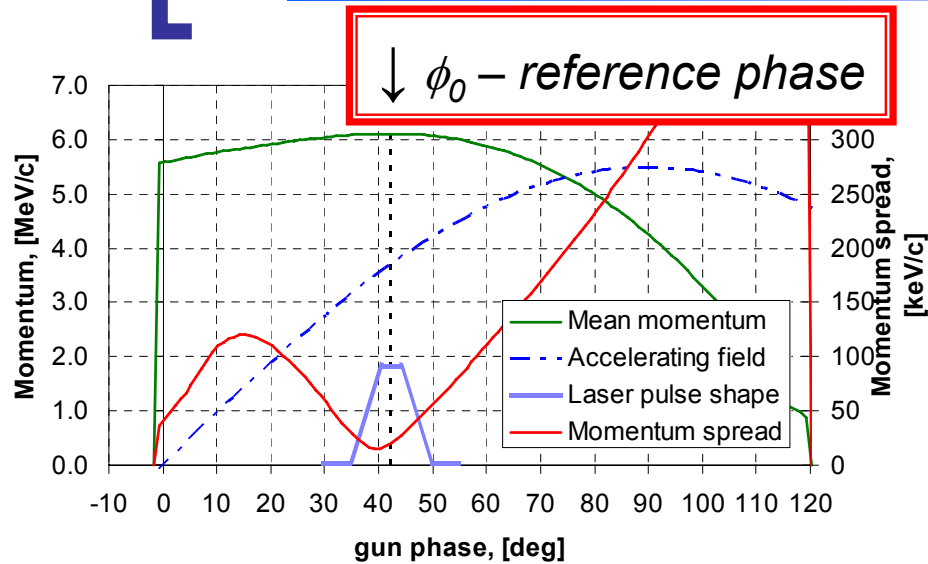
Photo-cathode laser

PTO, pulse-shaper, Nd:YLF pumped amplifier,
frequency converter

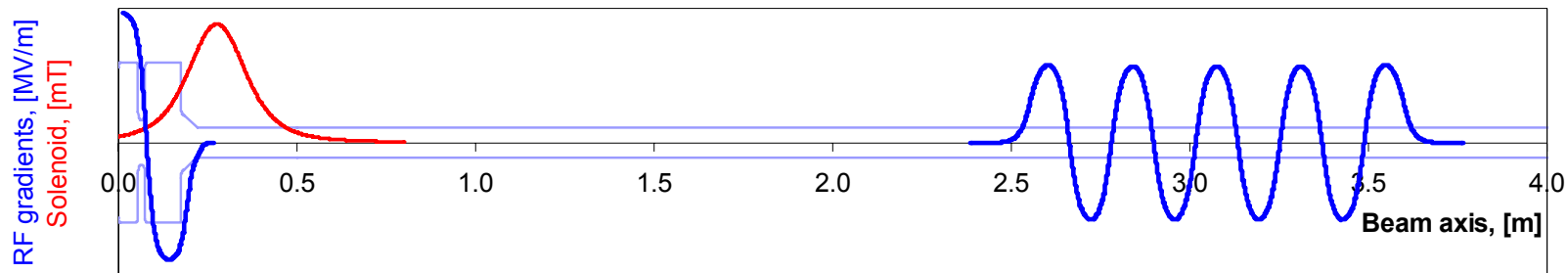
- $\lambda=262 \text{ nm}$
- rise/fall time = 6 ps (2 ps upgrade)
- FWHM = 20 ps
- σ_{xy} – tunable 0.1 to 3 mm diameter



Acceleration

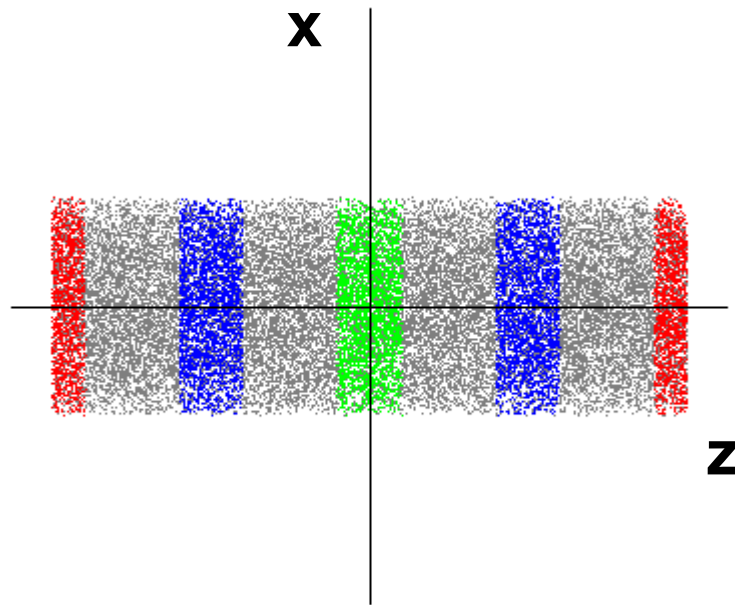


$$E_{acc} = E(z) \cdot \sin(\omega t + \phi)$$

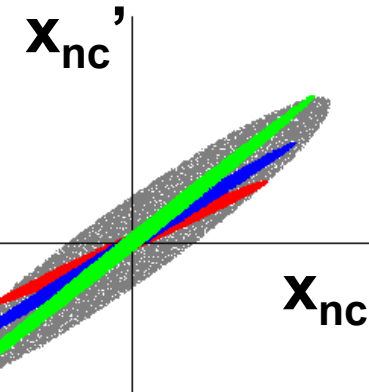


Emittance compensation solenoid, linear space charge

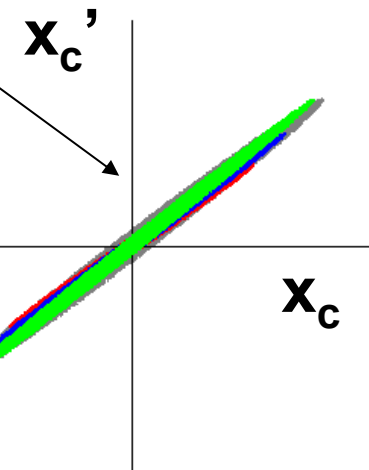
Longitudinal bunch distribution



Space charge induced spread



Space charge is compensated

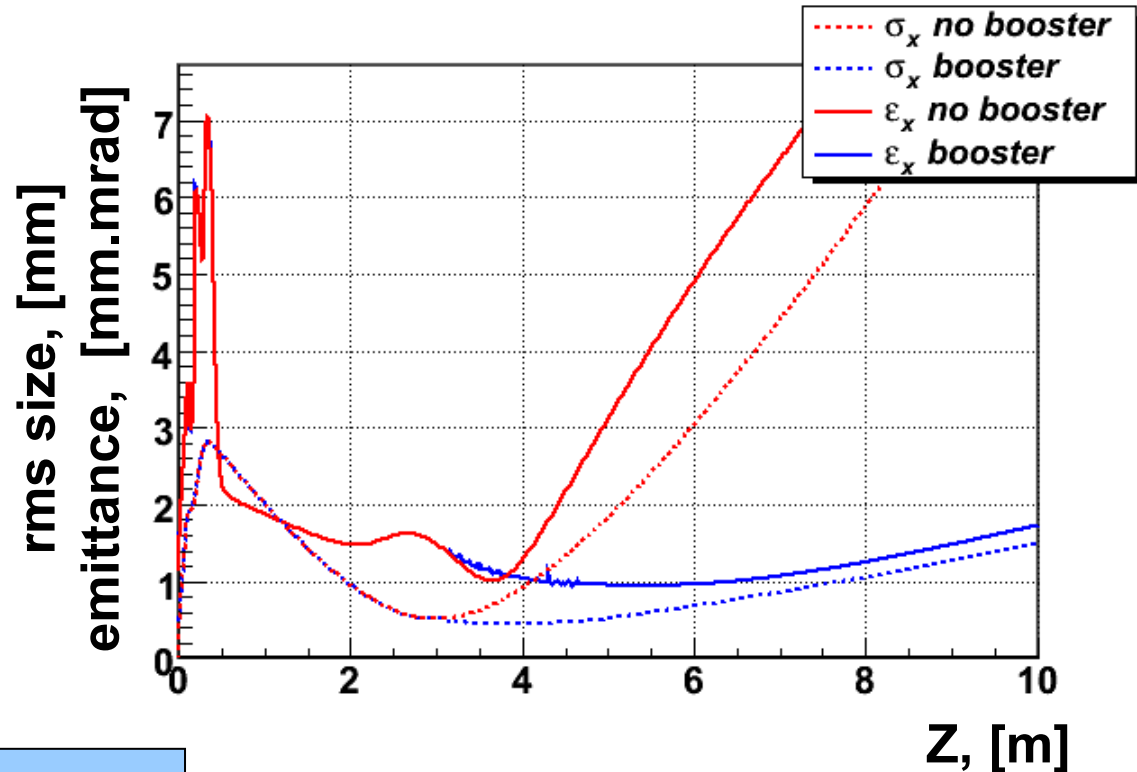


Envelope equation:

$$\sigma_{\perp}'' + \sigma_{\perp}' \frac{\gamma'}{\gamma} + \sigma_{\perp} \frac{\Omega^2 \gamma'^2}{\gamma^2} - \frac{I}{\sigma_{\perp} 2I_A \gamma^3} - \frac{\epsilon_{n,\perp}^2}{\sigma_{\perp}^3 \gamma^2} = 0$$

Emittance conservation booster, invariant envelope

- when space charge and external focusing ratio equals beam rms
 - invariant envelope
 - emittance oscillation damped
 - beam size better contained



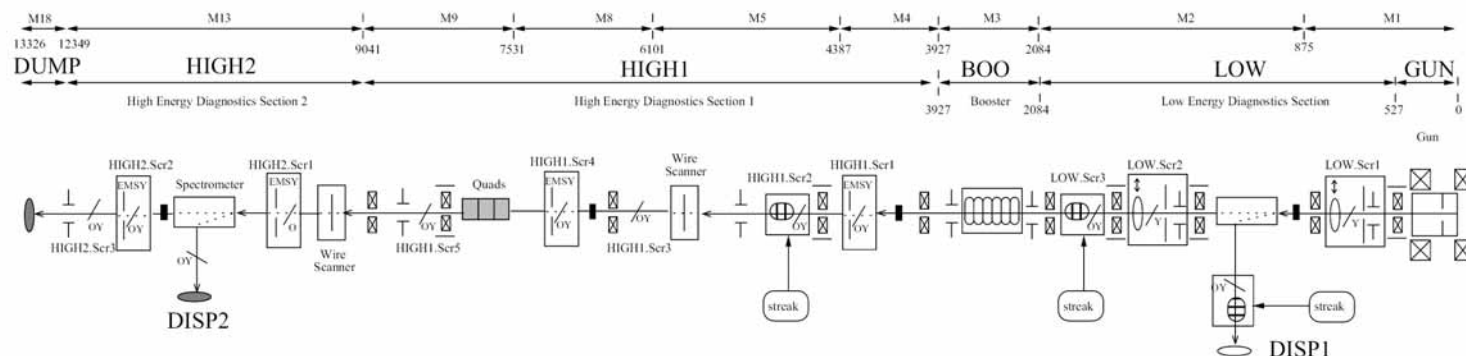
Envelope equation:

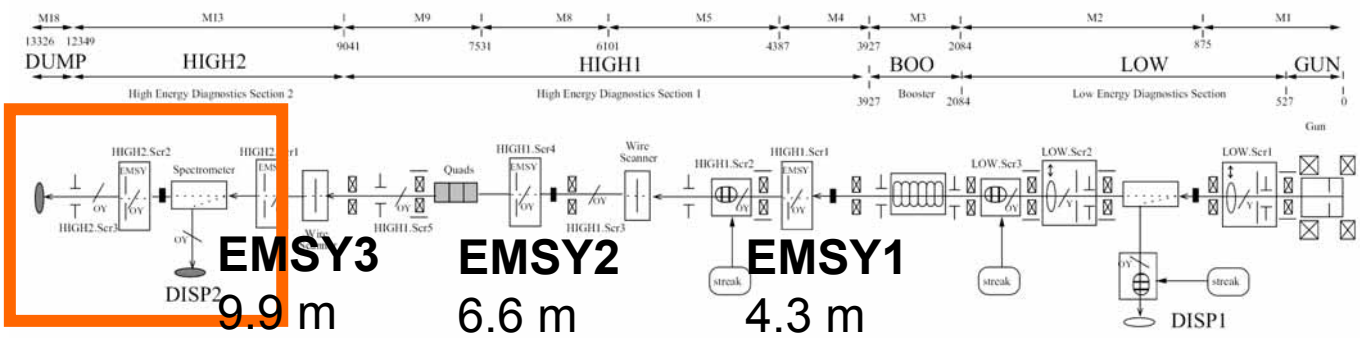
$$\sigma_{\perp}'' + \sigma_{\perp}' \frac{\gamma'}{\gamma} + \sigma_{\perp} \frac{\Omega^2 \gamma'^2}{\gamma^2} - \frac{I}{\sigma_{\perp} 2I_A \gamma^3} - \frac{\epsilon_{n,\perp}^2}{\sigma_{\perp}^3 \gamma^2} = 0$$

PITZ

diagnostic components

- Bunch charge
 - ICT and FC
- Transverse phase space
 - YAG and OTR screens
 - slit masks
- Momentum and momentum spread
 - two dispersive dipole magnets
- Longitudinal phase space
 - Cherenkov and OTR
 - streak camera





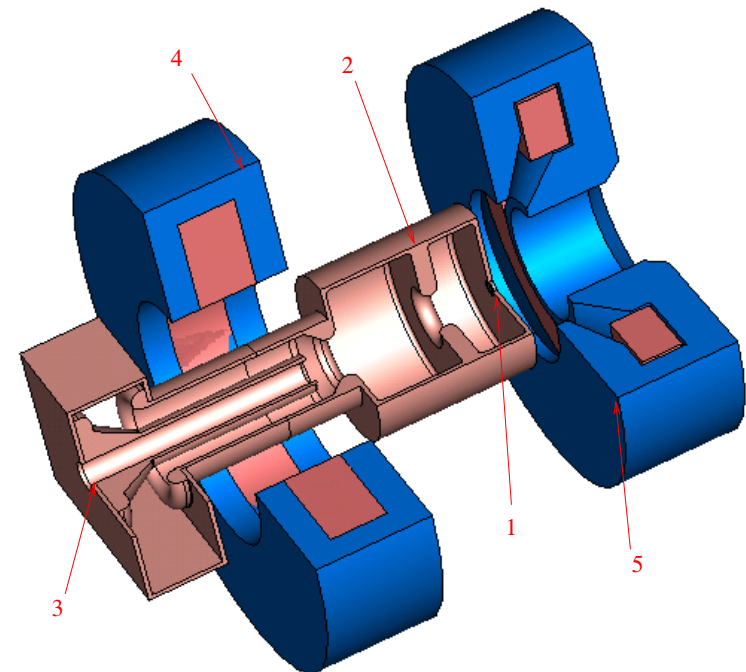
PITZ parameters

- Cathode laser
 - 1 to 800 bunches per train @ 10 Hz rep. rate, 1 μ s bunch spacing
 - flat top micro pulse duration of 20 ps (FWHM) with 6 ps rise/fall
- Charge per bunch $Q = 1$ nC
 - laser energy ~ 1 μ J @ 262 nm wavelength
- RF frequency 1.3 GHz
 - Max accelerating gradient 60 MV/m at the cathode
 - pulse duration 900 μ s with repetition 10 Hz
- Max. mean momentum $P = 14.5$ MeV/c (32 expected)
- Bunch length FWHM ~ 20 ps ($I_p \sim 50$ A)
- Transverse normalized emittance ε_n
 - better than 0.9 mm.mrad !!!

Control parameters

0. Photo cathode laser
 - Transverse shape and size
 - Longitudinal distribution – fixed (limited tuning)
 1. Cs₂Te photo cathode
 - 2, 3. RF gun cavity, RF coupler
 - Amplitude and phase of the RF wave
 - 4, 5. Focusing solenoids
 - focusing strength of the main solenoid (I_{main}), the other compensates I_{main}
- Drift space
- fixed - numerically optimized
- Booster cavity
- Amplitude and phase of the RF wave

red – variable parameter
blue – fixed, numerically optimized
grey – fixed, by the state of the art



Emittance measurement methods – definition reminder

$$\Sigma_x = \begin{pmatrix} \langle x^2 \rangle & \langle xx' \rangle \\ \langle xx' \rangle & \langle x'^2 \rangle \end{pmatrix}$$

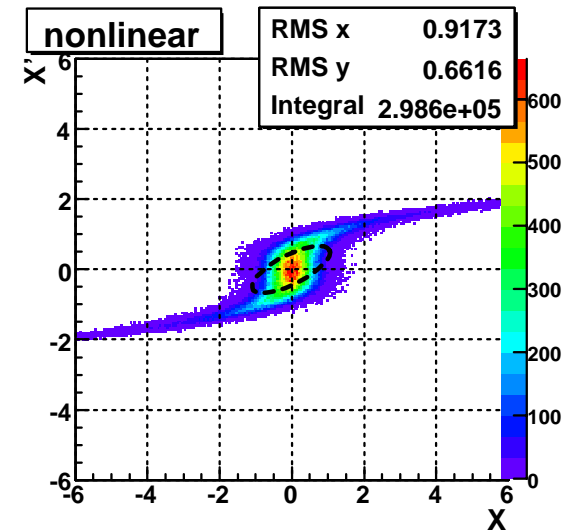
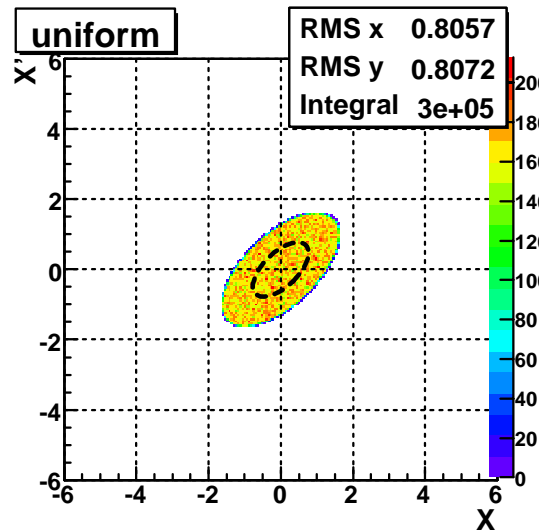
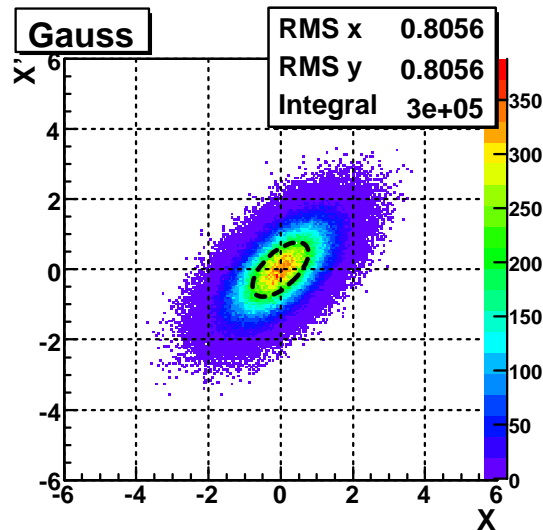
← covariance matrix

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$$\det|\Sigma_x| \cdot \beta\gamma = \varepsilon_{rms,n}^2$$

RMS normalized emittance:

$$\varepsilon_{x,rms} = \beta\gamma \cdot \sqrt{\langle x^2 \rangle \cdot \langle x'^2 \rangle - \langle xx' \rangle^2}$$

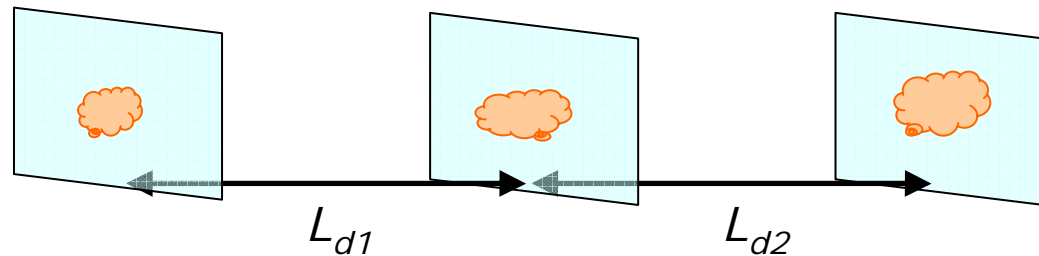


Emittance measurement methods

transfer matrix methods

- Multiple screen method

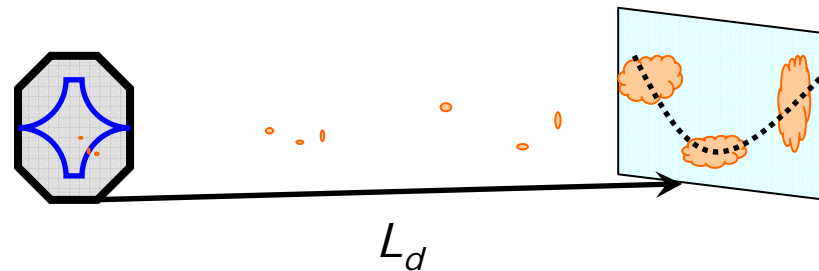
$$\Sigma_x^n = R \cdot \Sigma_x^{n-1} \cdot R^T;$$



- Quadrupole scan technique

$$\sigma_x^2(z) = \left[\sigma_{x0}^2 - 2\alpha_{x0}\epsilon_x L_d + \gamma_{x0}\epsilon_x L_d^2 \right] + \frac{2\sigma_{x0}^2}{f} \left[\frac{\alpha_{x0}}{\beta_{x0}} L_d - L_d \right] + \frac{2\sigma_{x0}^2}{f^2} L_d;$$

here: α, β, γ – are the Twiss parameters; f – the quadrupole focusing strength



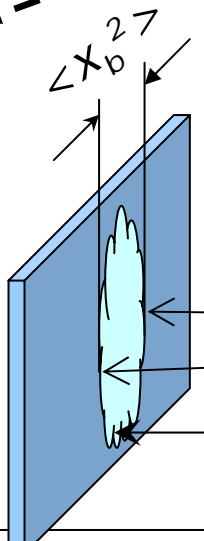
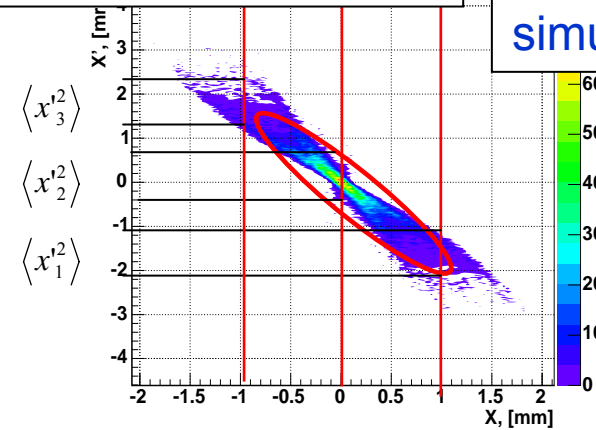
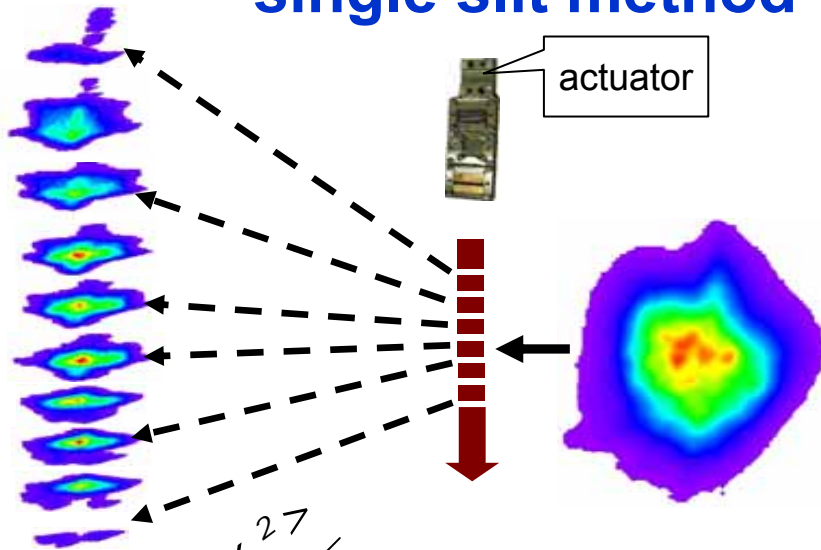
Emittance measurement

methods

single slit method

Automatic measurement proc.

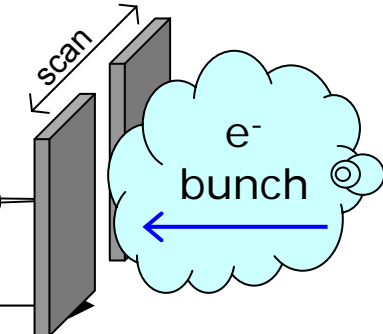
ASTRA simulation



$$\langle x_i'^2 \rangle = \sqrt{\frac{\langle x_b^2 \rangle_i}{L_d^2}}$$

local uncorrelated divergence

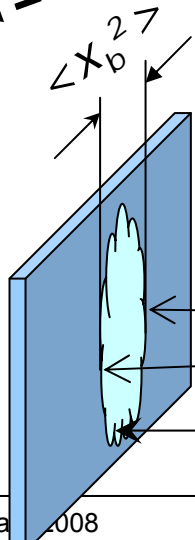
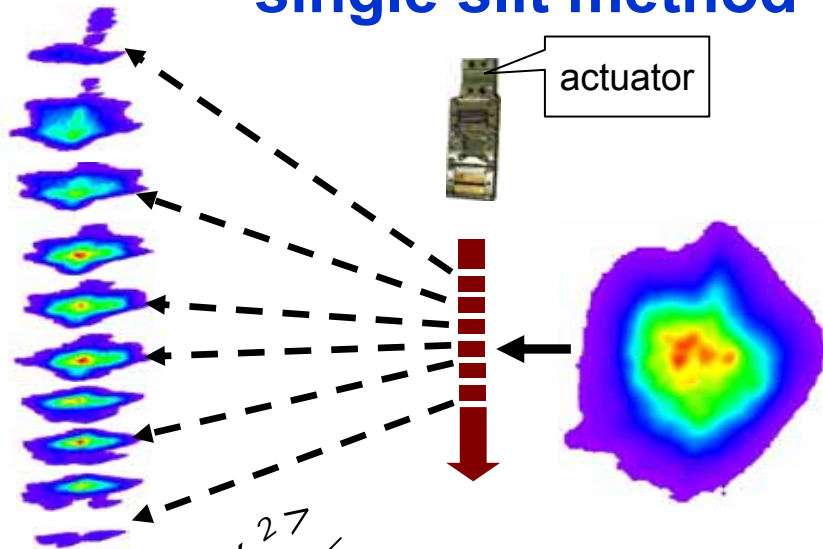
$$\langle x'^2 \rangle = \frac{1}{n} \cdot \sum_{i=1}^n w_i \cdot \langle x_i'^2 \rangle$$



$$L_d = 2.334 \text{ m}$$

Emittance measurement methods

single slit method



$$\langle x_i'^2 \rangle =$$

local ur

$$L_d = 2.334 \text{ m}$$

Automatic measurement proc.

EMWizard

Central control | General options | TV options

450A_g0_b0deg name2

EMSY1 Axis X Y

C Y S1 S2 31

Best single 7.069

Must-have's

skip Mean RMS ϕ_{rel}

Gun 6.799 0.025 [MeV] +5 [deg]

Booster 12.3456 0.0456 [MeV] +20 [deg]

Laser beam:

Xrms Yrms Rise Fall FWHM

0.521 0.498 7.8 7.6 20 skip

Monitor

Gun 61.4 +/- 0

Boo 38.4 +/- 0

Irm 450 +/- 0

ICT 0 +/- 0

777 0 +/- 0

Stop log

From: -10000 um

To: -10000 um

Step: 1000 um

S.O.S. 11 nr. b-lets

10 frames

View ZNPPITZFG1

Grab'n'Save

Open

save type

EMSY

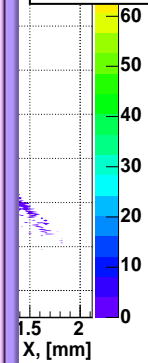
beamlet

MOI

99% Bye-bye!

Current position: 31.000, [mm]

ASTRA simulation



$$\langle x_i'^2 \rangle$$

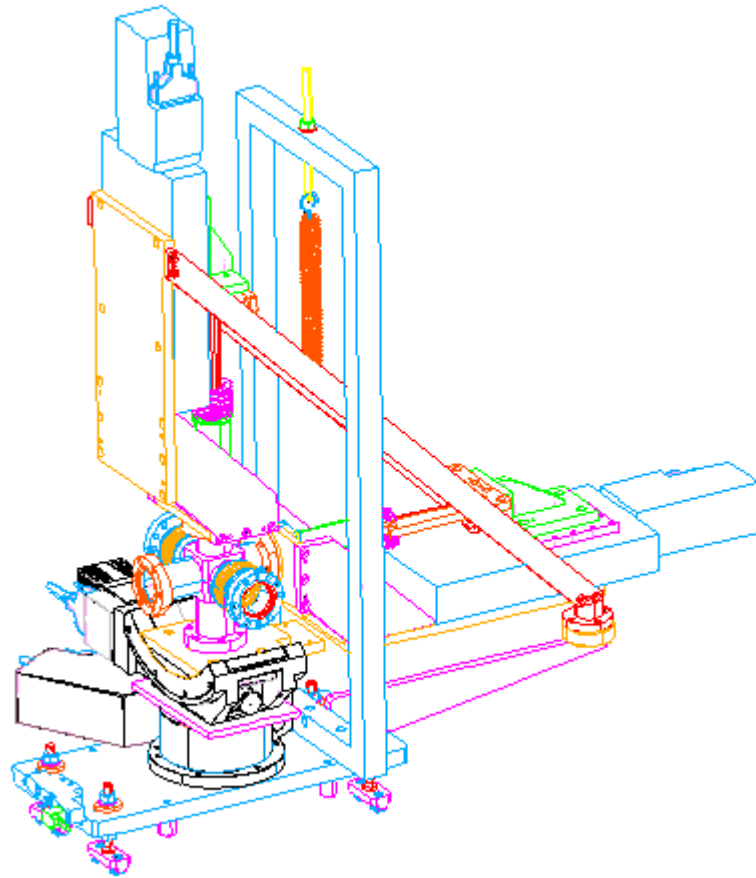
e⁻ bunch

Slit method

general requirements

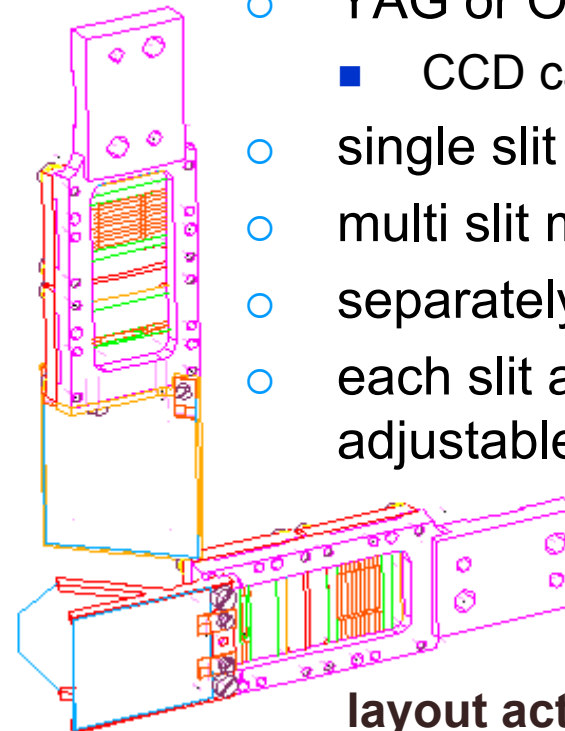
- Emittance dominated beamlets (slit opening)
 - Reliable signal from the beamlets
- The mask thickness must be enough to scatter the residual electrons
- Optimal drift length
 - enough distance for beamlet evolution (max. L_d)
 - resolution of the divergence
 - elimination of the influence from the initial beamlet size
 - minimizing the effect of space charge (min. L_d)

Emittance Measurement SYstem (EMSY)



EMSY layout

- two orthogonal actuators
 - YAG or OTR screen
 - CCD camera
 - single slit mask
 - multi slit mask
 - separately movable
 - each slit acceptance adjustable



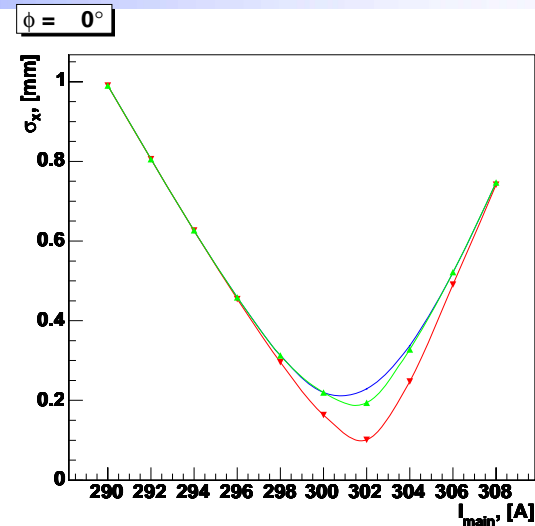
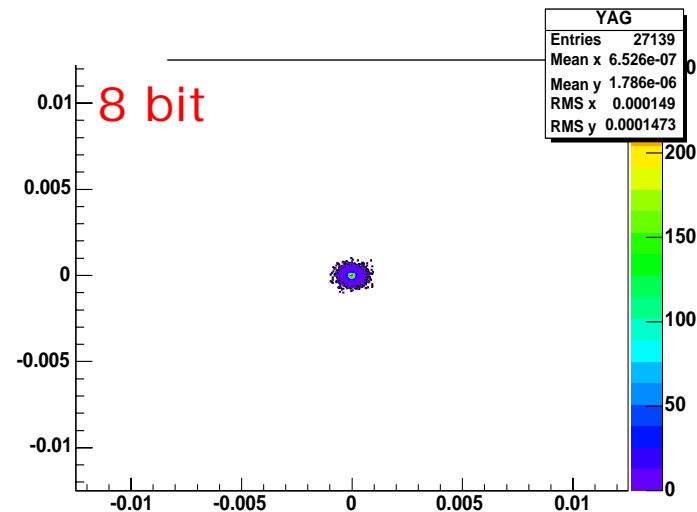
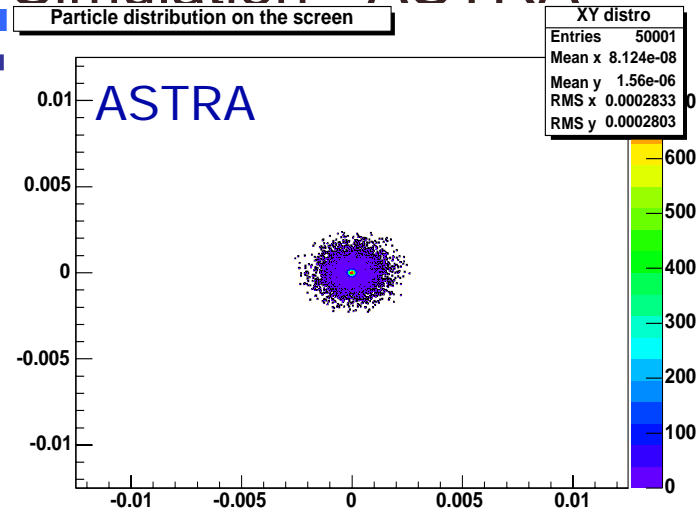
layout actuators

Emittance Measurement: Systematic uncertainty

- beam size measurements
 - screen
 - saturation (YAG), screen geometry, multiple scattering etc.
 - optic lenses
 - CCD camera
- local divergence
 - beamlet size measurements
 - space charge contribution
 - noise from scattered electrons
- momentum measurements
 - dipole field errors
 - beam size associated

Electron beam size measurement

Simulation - ASTRA



- 768x567 CCD chip
- Screen area 20x20 mm
- ASTRA –
 - 750k particles, 1 nC gun only.
 - Beam momentum ~ 5 MeV
- **8 bit** – 1/255
- **12 bit** – 1/4096

Emittance Measurement uncertainty

Space charge effect

- Envelope equations for **non-symmetric beam**
 - Used to calculate the beamlet evolution
 - Estimates the influence of the slit opening due to space charge on the beamlet size
- Uniform distribution used to solve the system
- General parameters:
 - $I = 50, A$
 - $\gamma = 10 \dots 60$
 - $\sigma_x = 0.2 \dots 2, \text{ mm}$
 - σ'_x - scaled such that
 - $\varepsilon_x = 1 \text{ mm.mrad}$

Emittance Measurement uncertainty

Space charge effect

- Envelope equations used

$$\sigma_x'' = \frac{I}{I_a \cdot (\sigma_x + \sigma_y) \cdot \gamma^3} + \frac{\varepsilon_{nx}}{\sigma_x^3 \cdot \gamma^2}$$

$$\sigma_y'' = \frac{I}{I_a \cdot (\sigma_x + \sigma_y) \cdot \gamma^3} + \frac{\varepsilon_{ny}}{\sigma_y^3 \cdot \gamma^2}$$

here:

I - peak current [A], I_a - Alfven current (17.0 kA);
 σ_x - transverse size; σ_x' - transverse divergence;
 ε_x - normalized emittance; γ - Lorentz factor;

$\langle xx' \rangle$ - for now it is assumed to be zero

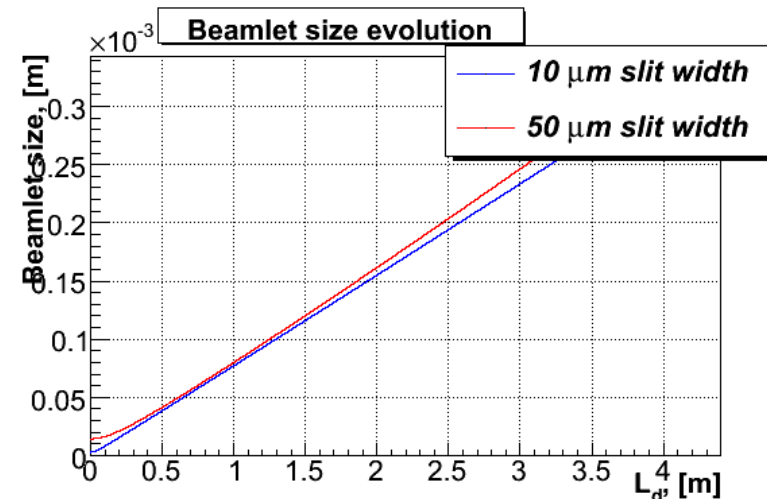
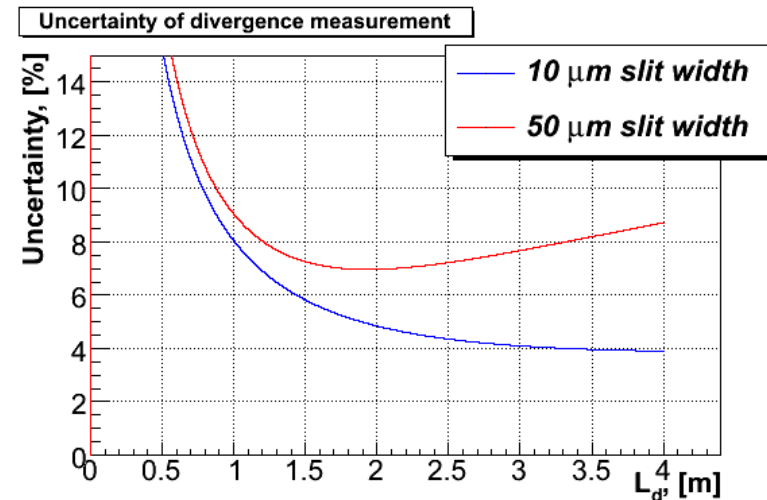
- General parameters:

- I = 50, A
- γ = 10 .. 60
- σ_x = 0.2 .. 2, mm
- σ_x' - scaled such that
- ε_x = 1 mm.mrad

Emittance uncertainty

nominal values at **30 MeV/c**

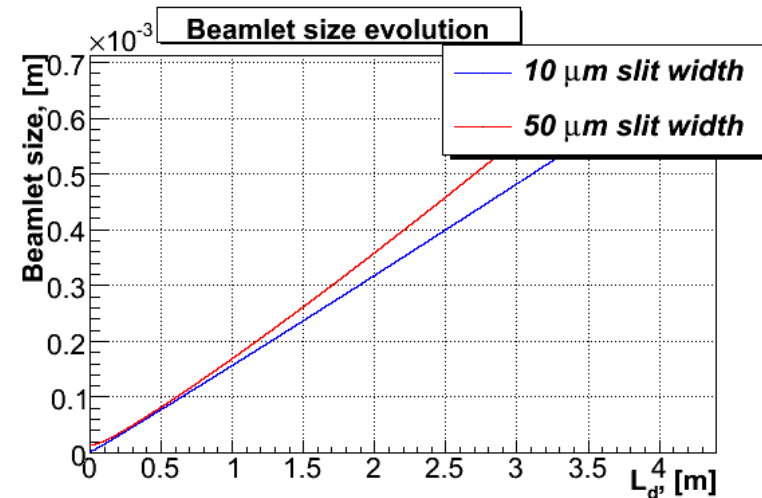
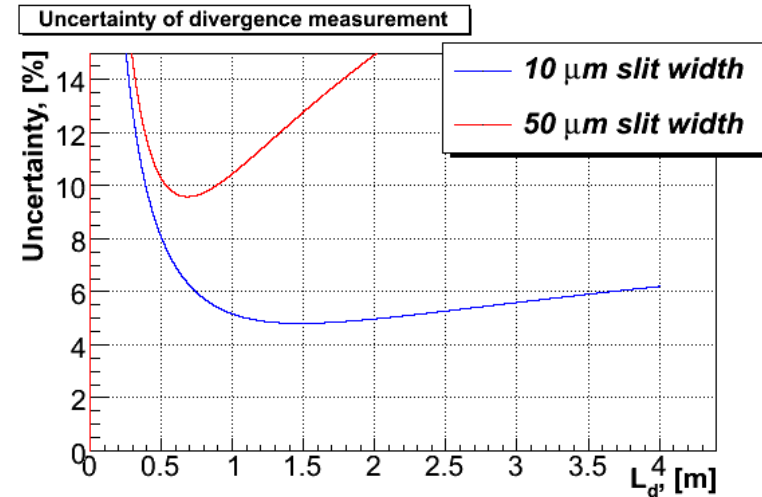
- Asymmetric envelope equations solved for:
 - I = 50 A
 - γ = **58.7 (30 MeV/c)**
 - σ_0 = 0.2 mm
 - σ'_x = **0.0766 mrad**
 - ε_x = **0.9 mm.mrad**
- Optical resolution of **50 lines/mm**
- Uncertainty at $L_d = 2\text{ m}$
 - **4.85 % (10 μm slit)**
 - **155 μm beamlet rms size**



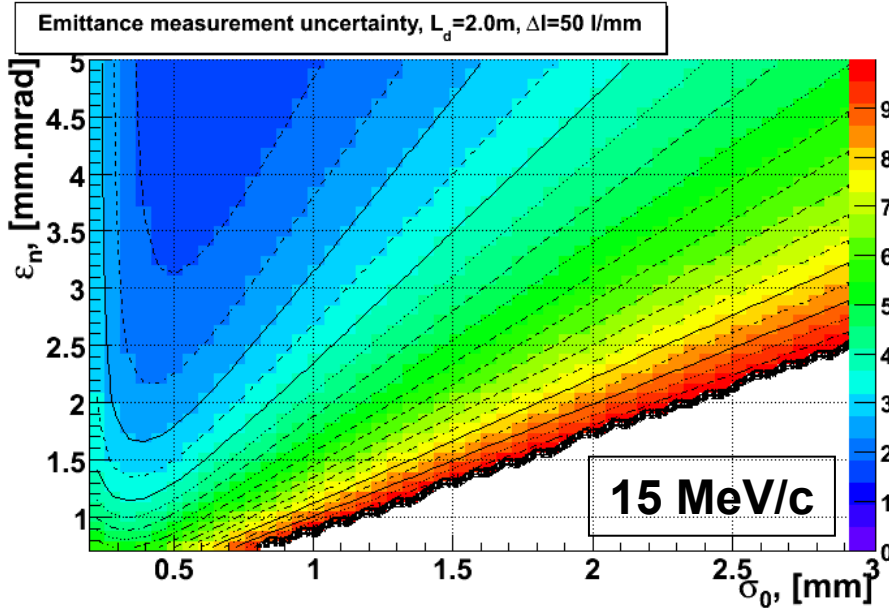
Emittance uncertainty

nominal values at **15 MeV/c**

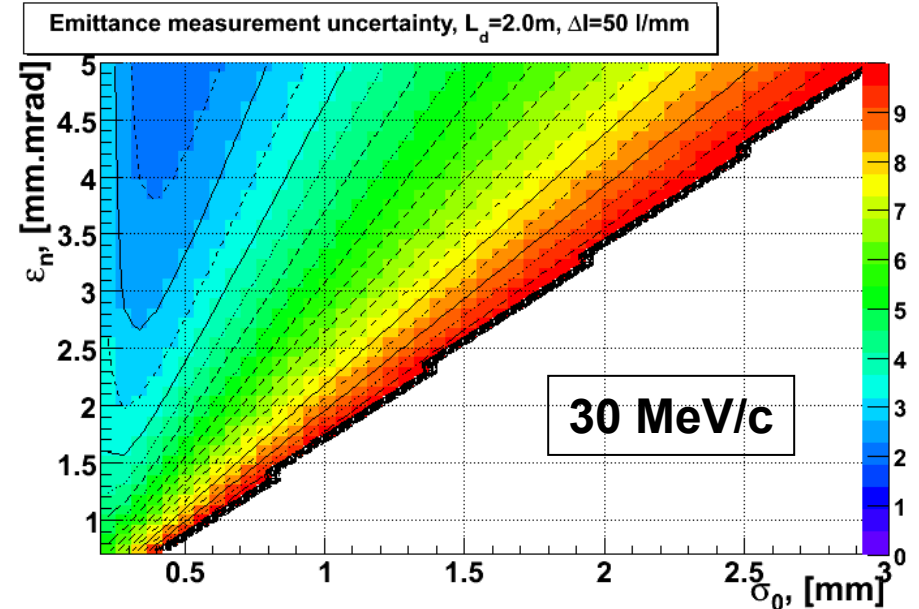
- Asymmetric envelope equations solved for:
 - I = 50 A
 - γ = **29.3 (15 MeV/c)**
 - σ_0 = 0.2 mm
 - σ'_x = **0.153 mrad**
 - ε_x = **0.9 mm.mrad**
- Optical resolution of **50 lines/mm**
- Uncertainty at $L_d = 2$ m
 - **4.98 % (10 μm slit)**
 - **318 μm beamlet rms size**



Emittance uncertainty error map



- Here:
- I = 50, A
 - σ_0 = variable, mm
 - σ'_x - scaled to correspond
 - ϵ_x = variable, mm.mrad

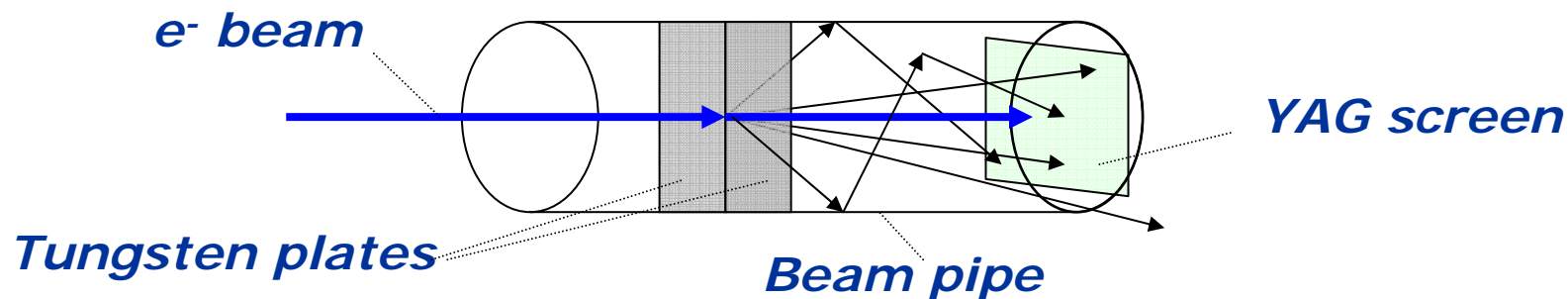
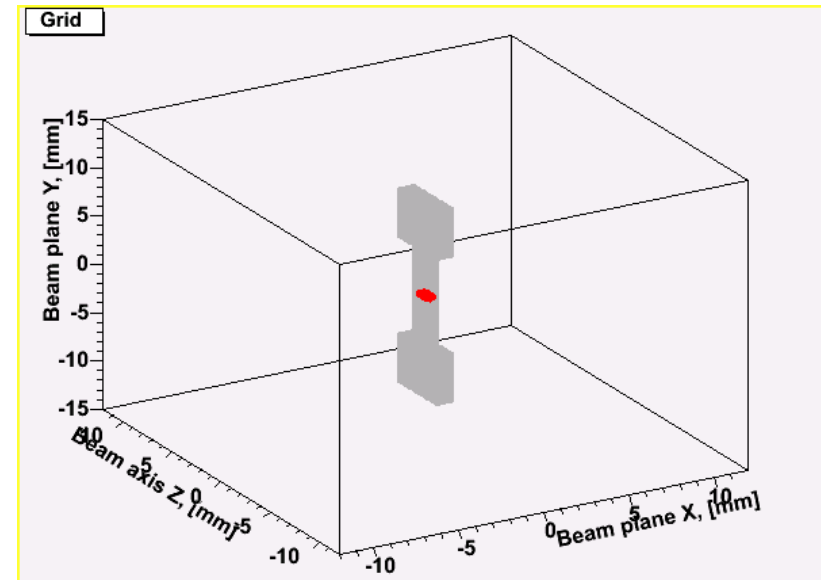


- Uncertainty map
- $L_d = 2\text{ m}$
 - $10\ \mu\text{m slit opening}$
 - 50 lines/mm

GEANT4 simulations

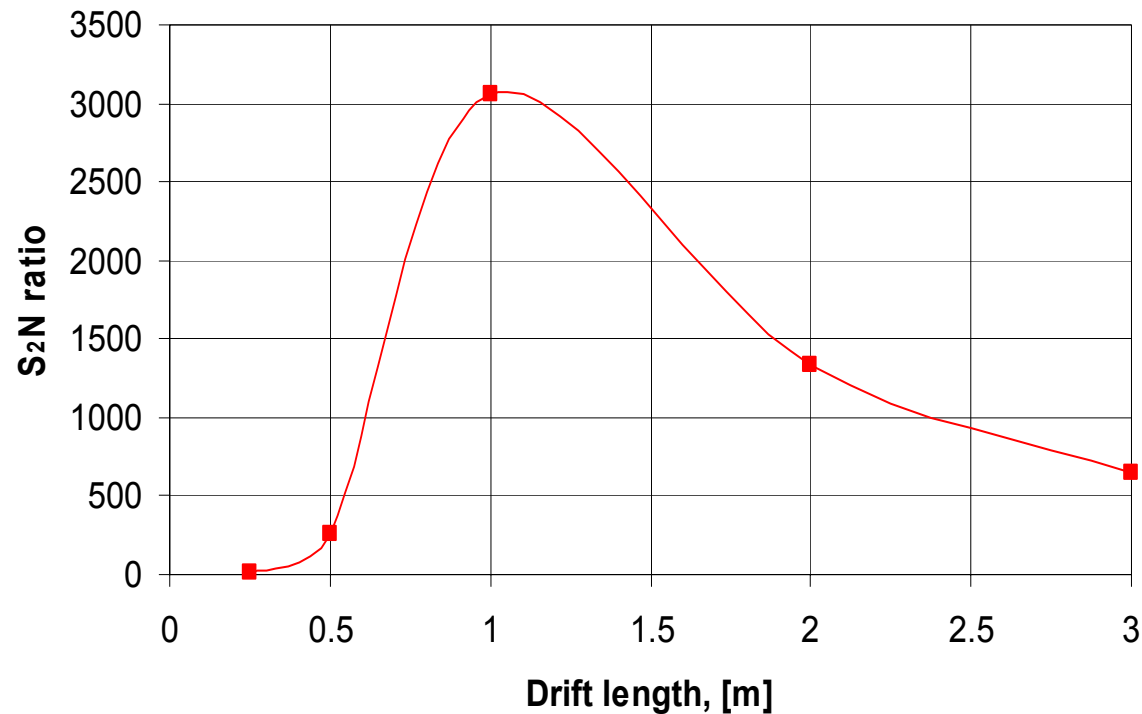
slit mask

- Simplified G4 model
 - The signal to noise ratio
 - The energy deposited in the tungsten
- The plate thickness, the distance to the screen and used as variables



GEANT4 simulations

signal to noise ratio



$$S2N = \frac{C_s}{C_n} \cdot \frac{A_n}{A_s}$$

Here:

C_s – counts signal

C_n – counts noise

A_s – area of the signal

A_n – area of the noise

Slit parameters:

Tungsten

1 mm thickness

10 μm slit opening

EMSY optimization

Conclusions

- The slit mask material is chosen to be **Tungsten**
- The **thickness** of the slit mask must be **1 mm**
- The **slit opening** should be **10 μm**
- **Distance (L_d)** between the screen and the mask **$\sim 2\text{ m}$**
- **12 bit camera** resolution is required
- **optical resolution** better than **50 lines/mm**

Emittance measurements

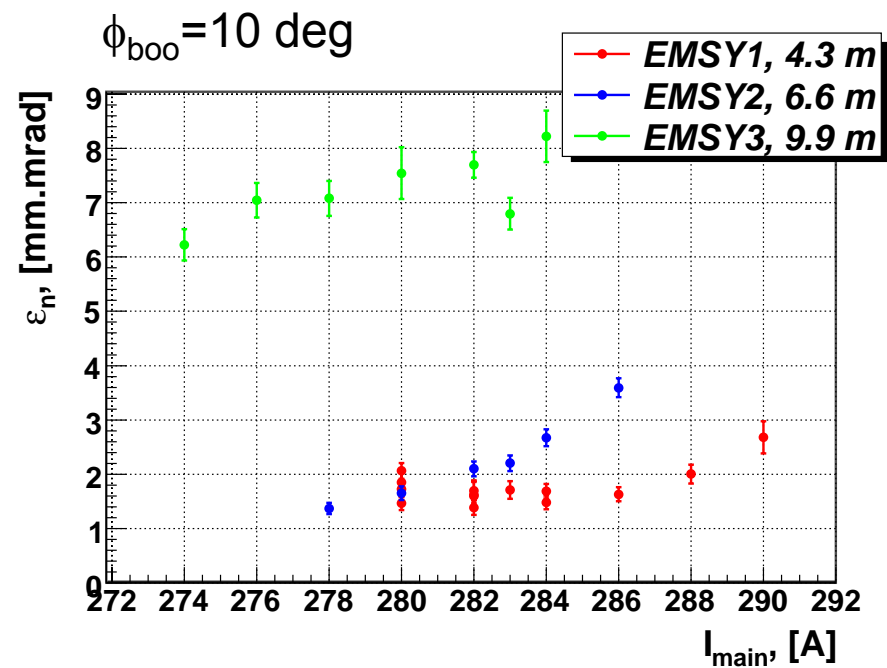
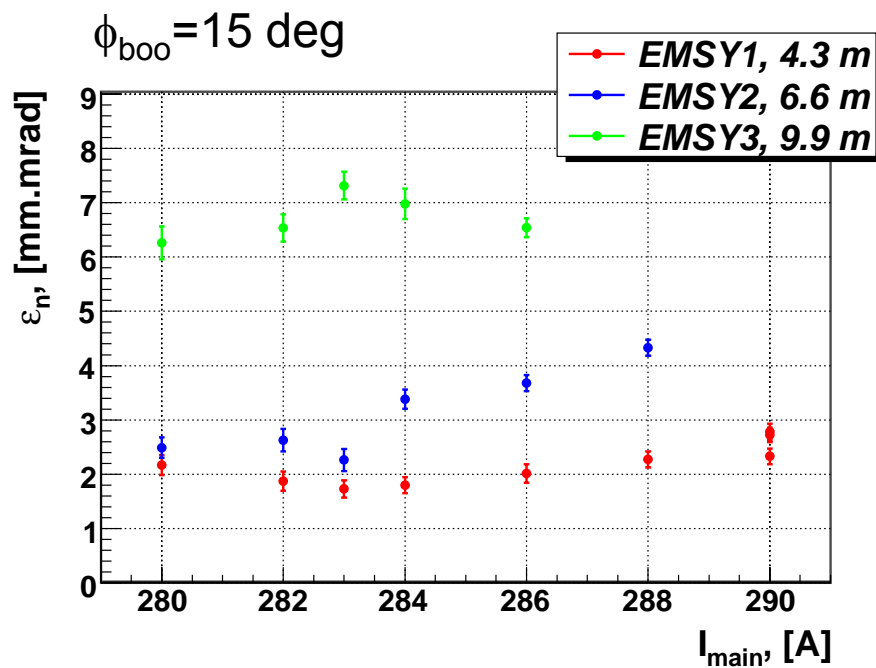
Two different gun cavities of the same prototype

- gun 3.1 (October 2006)
 - max. gradient ~43 MV/m (FLASH spare gun)
 - optimization parameters:
 - I_{main} around the focus at EMSY screen
 - booster phase (phase of the gun fixed ϕ_0+2)
 - emittance measured at **three locations** downstream
 - only 8 bit cameras used
- gun 3.2 (August 2007)
 - max. gradient ~**60 MV/m** (1st test for XFEL gun)
 - optimization parameters:
 - I_{main} scanned around the focus at EMSY screen
 - booster accelerating gradient (phases of gun ϕ_0 and booster ϕ_0 are fixed)
 - different initial beam sizes at the cathode
 - **12 bit** cameras used for beamlet measurements

Emittance measurements

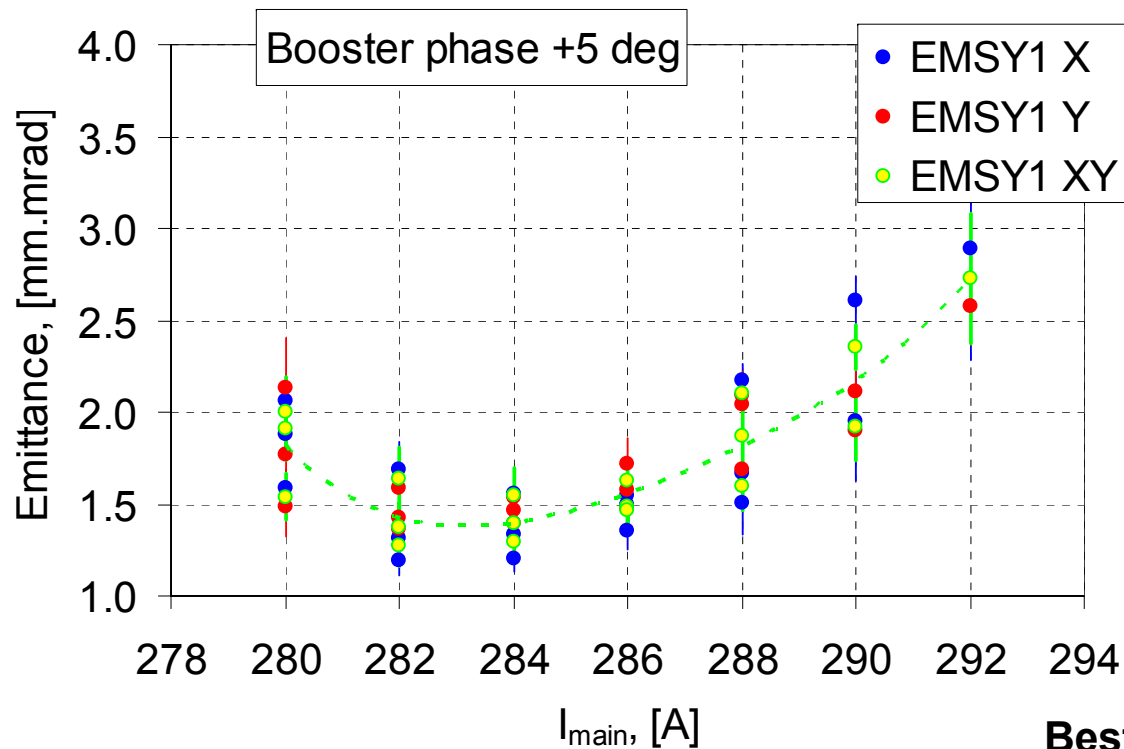
gun 3.1 (October 2006)

- Gun gradient ~ 43 MV/m (at the cathode)
- Final beam momentum ~ 13 MeV/c
- Laser rms spot size ~ 0.51 mm



Emittance measurements

gun 3.1 (October 2006)



Measurement conditions:

mean momentum MeV/c

~ 4.95 @ gun

~ 13.0 @ booster

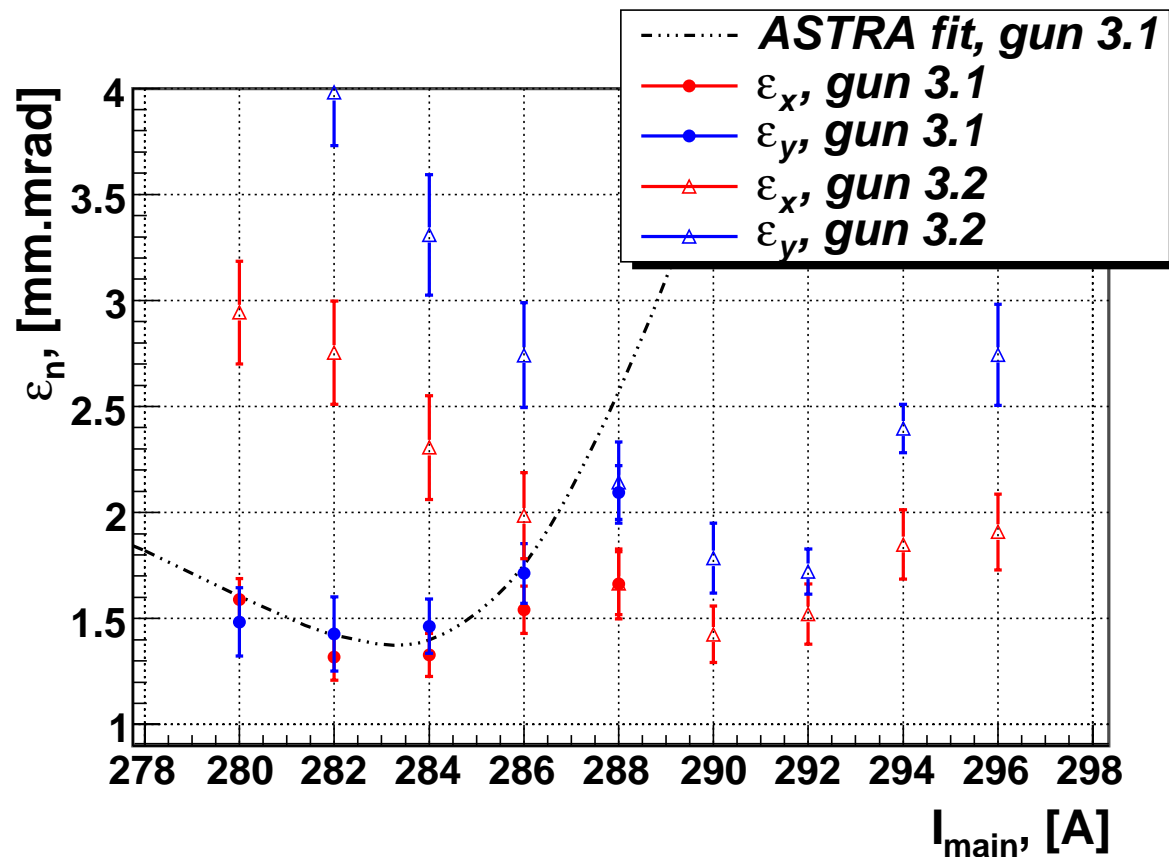
initial rms spot size ~ 0.51 mm

Best measurement taken:

I_{main}	= 282	[A]
ε_x	= 1.32 ± 0.11	[mm mrad]
ε_y	= 1.43 ± 0.17	[mm mrad]

Emittance measurements

Comparison – gun 3.1 vs. gun 3.2



Machine parameters:

- $XY_{ini}=0.51$ mm (rms laser@cath)
- mean momentum MeV/c
 - gun 4.95
 - booster 12.85
 - $\phi_{booster}=\phi_0+5$ deg

Minimum emittance:

- gun 3.1
 - $\epsilon_{xy}=1.37\pm 0.14$ mm.mrad
 - $I_{main}=282$ A (0.166 T)
- gun 3.2
 - $\epsilon_{yy}=1.54\pm 0.15$ mm.mrad
 - $I_{main}=290$ A (0.171 T)

- beamlet observation CCD cameras different (8 & 12 bit)

Emittance measurements

gun 3.2 (August 2007)

- EMSY1 only
- fixed phases @max. momentum gain
- gun gradient ~ **60 MV/m@cathode**
- different laser diameter at cathode
 - Laser aperture (XY_{laser}) - **1.2, 1.5, 1.8** and **2.0** mm
 - rise/fall time ~ 6 ps
 - FWHM ~ 20 ps
- different booster gradients
 - final beam momentum of **9.5, 11, 13** and **14.5** MeV/c

Emittance measurements, gun 3.2 (August 2007)

$XY_{\text{laser}} 1.5 \text{ mm}$

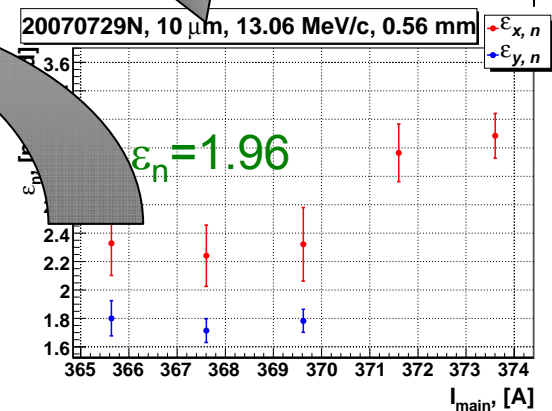
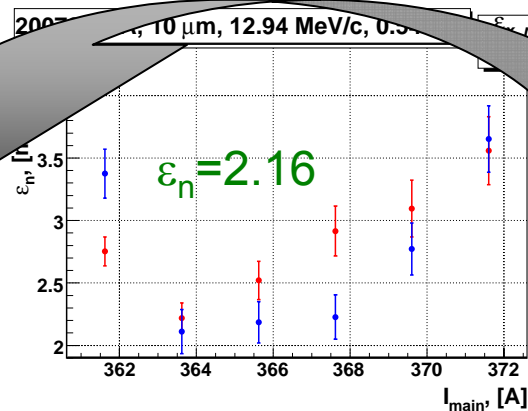
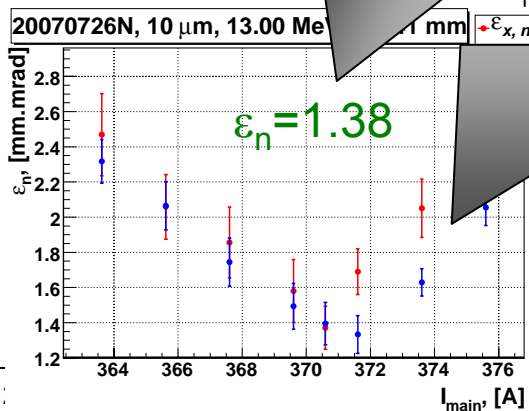
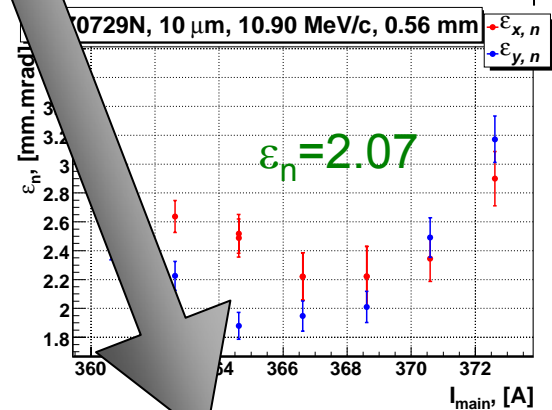
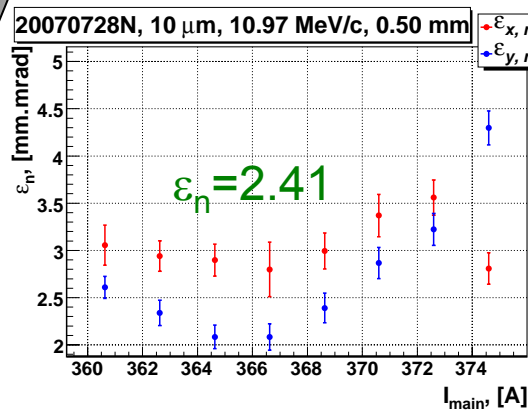
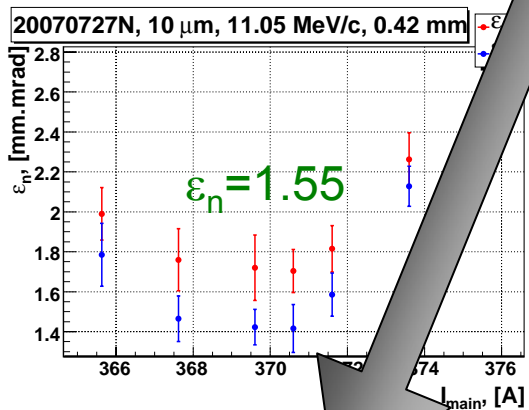
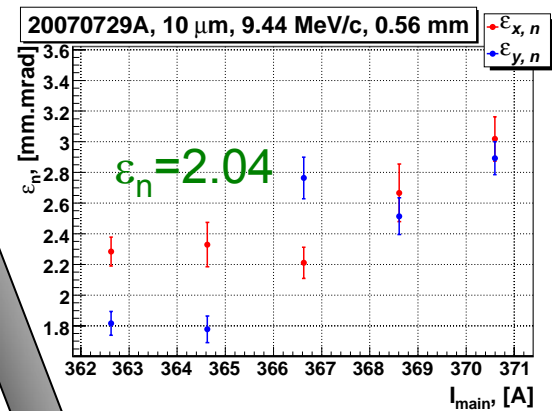
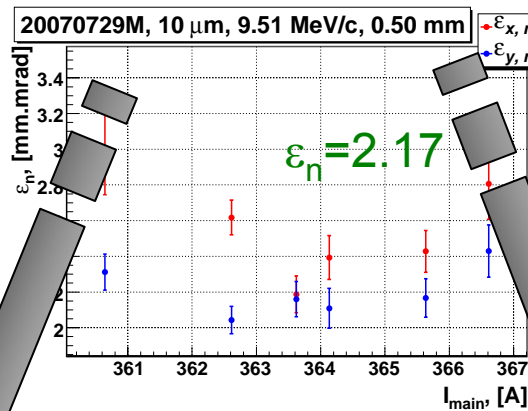
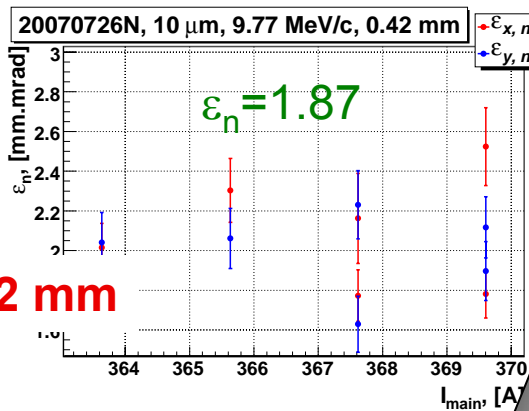
$XY_{\text{laser}} 1.8 \text{ mm}$

$XY_{\text{laser}} 2.0 \text{ mm}$

9 MeV/c
 $XY_{\text{laser}} 1.2 \text{ mm}$

11 MeV/c

13 MeV/c

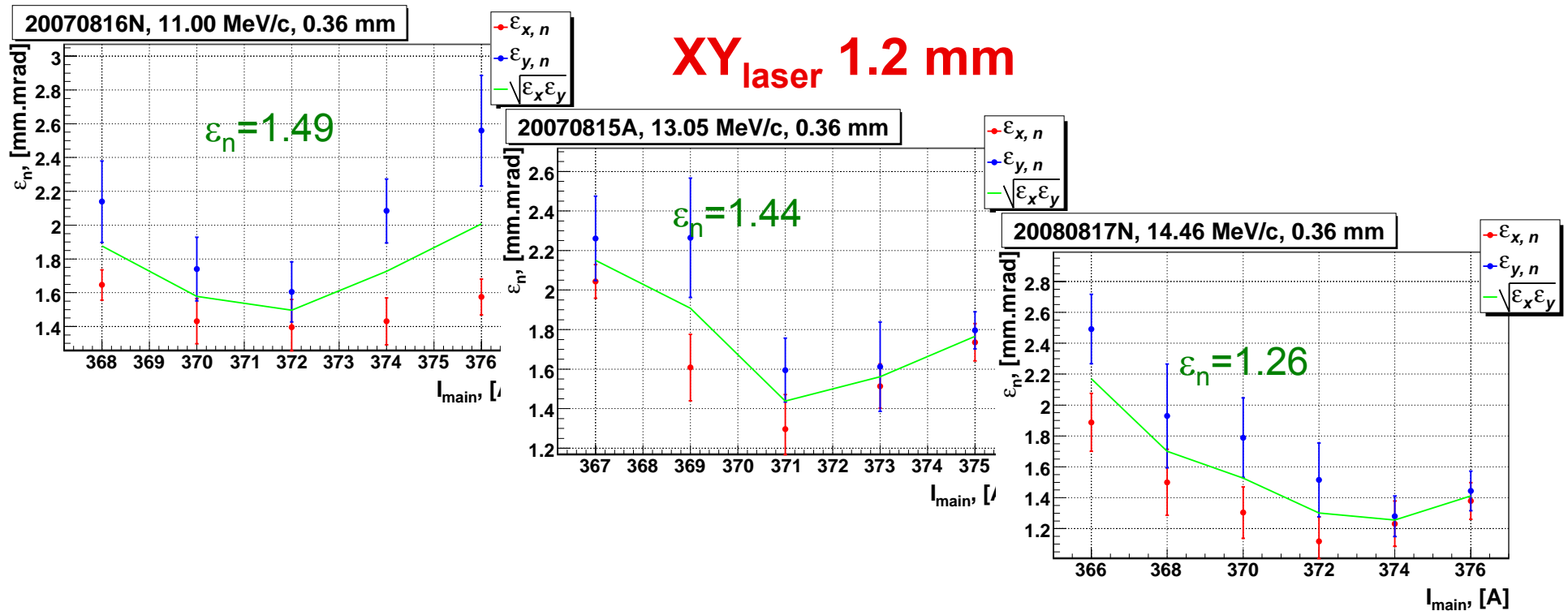


February

Results

gun 3.2 (August 2007)

XY_{laser} 1.2 mm



$P_{\text{mean}} = 11,$

$P_{\text{mean}} = 13,$

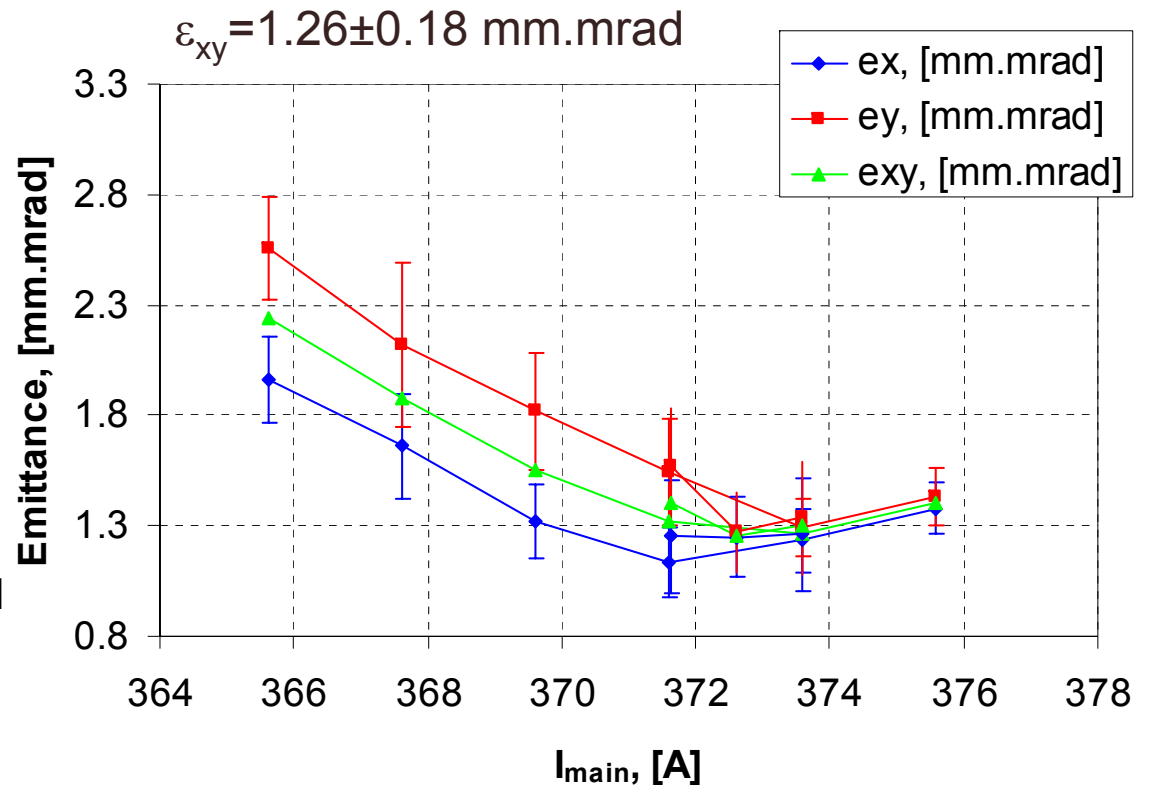
$P_{\text{mean}} = 14.5,$

[MeV/c]

Results

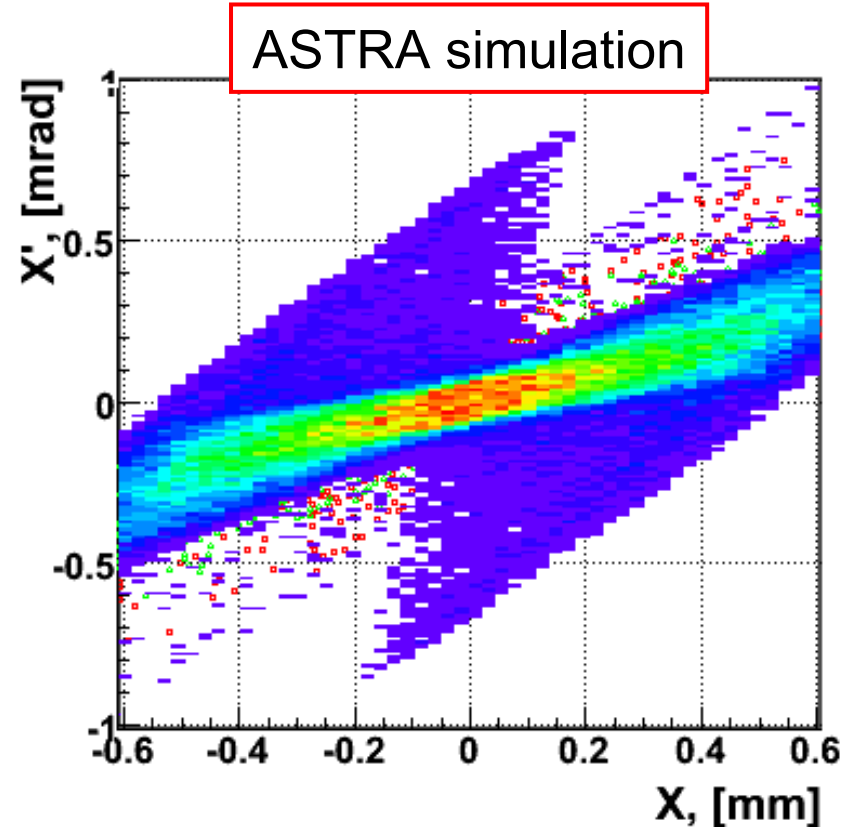
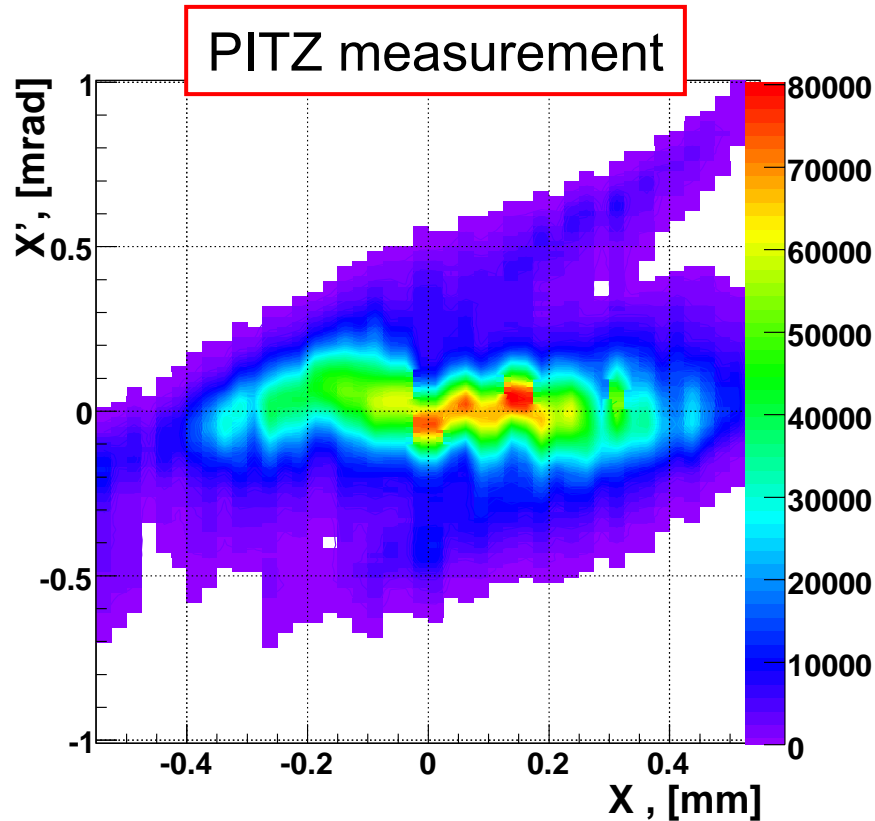
best emittance

- Measurement conditions:
 - Laser
 - XYini=0.36 mm (rms)
 - rise/fall time 6 ps
 - FWHM = 20 ps
 - Maximum gradient ~60 MV/m
 - Gun and booster phases at max. momentum gain
 - $P_{\text{gun}}=6.44$ MeV/c
 - $P_{\text{boo}}=14.46$ MeV/c
 - minimum emittance measured at $I_{\text{main}} = 374$ A (-0.220 T)



Results

best emittance – phase space



- measured phase space distribution
 - $XY_{ini}=0.36$ mm (rms)
 - $P_{boo}=14.46$ MeV/c
 - $I_{main} = 374$ A (-0.220 T)

Summary and outlook

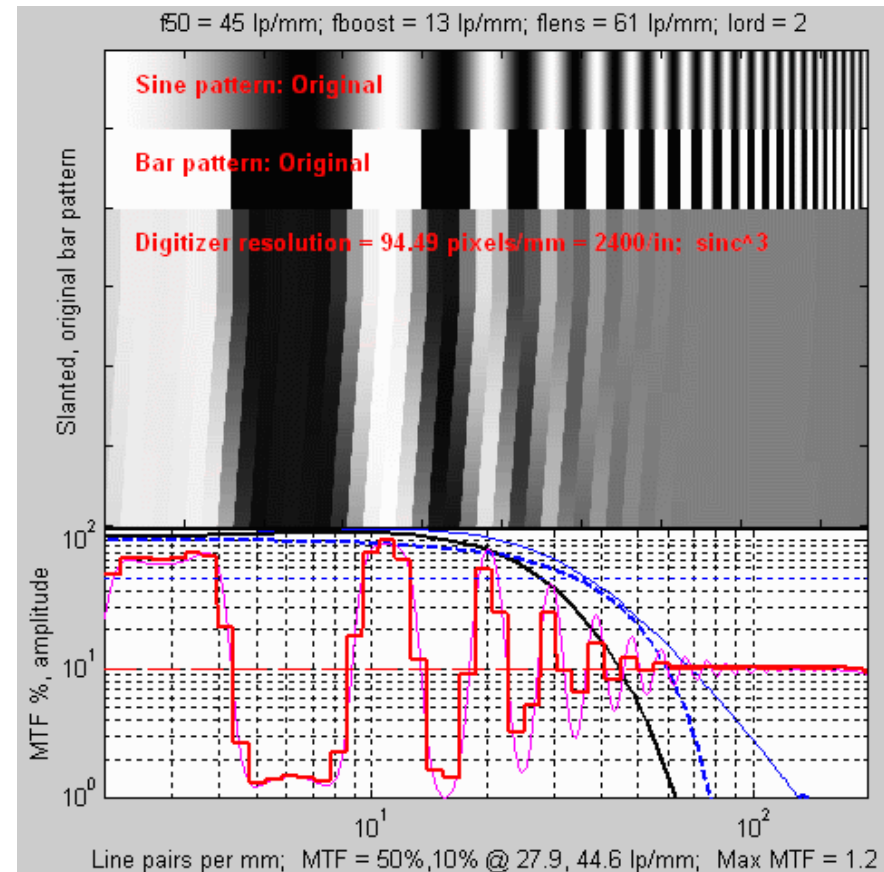
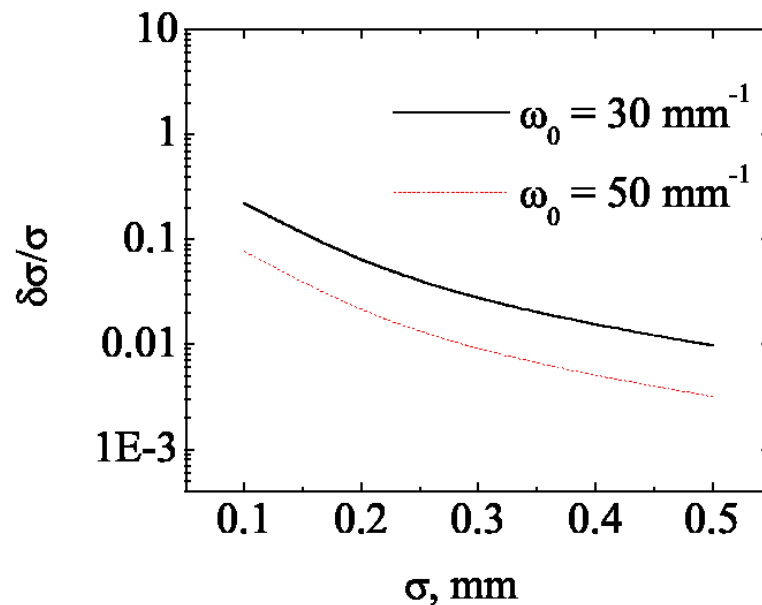
- PITZ is capable of producing electron beams with small emittance
 - the smallest value achieved was $\varepsilon_{xy}=1.26\pm0.18$ mm.mrad (geom. avg.)
- Optimization of the emittance measurement system was done – slit mask, screen setup and readout system
 - wider momentum range
 - lower emittance
- Automatic measurement procedure implemented
 - faster measurements
 - more reliable results
- Main optimization parameters scanned
 - Solenoid strength
 - initial beam size
 - booster gradient
- To be improved:
 - differences between gun3.1 and gun3.2 have to be understood
- upgrade of the laser system is ongoing
 - 2 ps rise/fall times (XFEL milestone)
- in 2008 new booster cavity will be installed
 - improved stability
 - better field quality
 - more flexibility for studying the invariant envelope matching principle

Thank You for the attention!

Electron beam size measurement

optics contribution

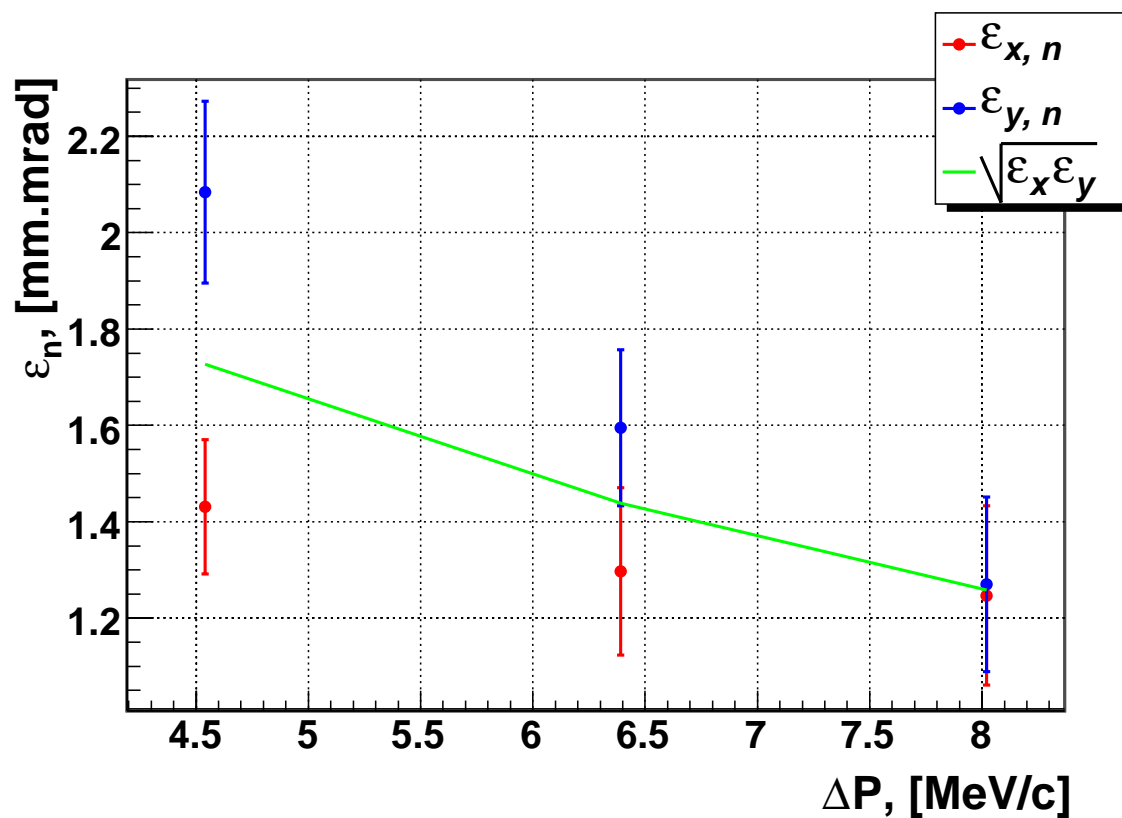
- MTF formalism used
- Uncertainty as a function of beam size



<http://www.normankoren.com/Tutorials/MTF.html>

Results

gun 3.2 (August 2007)



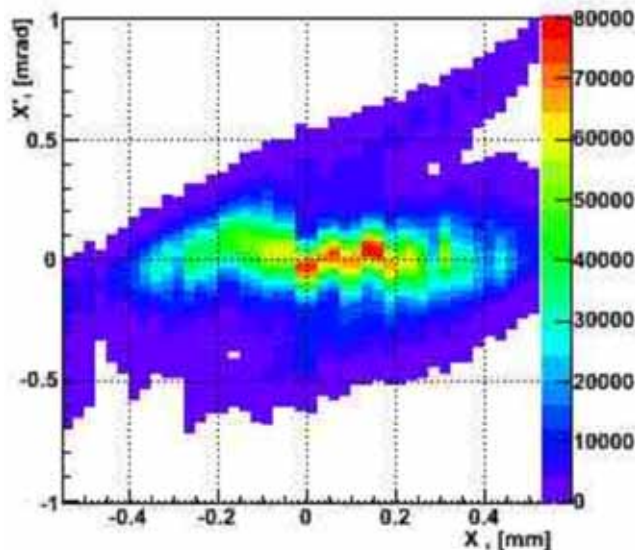
emittance obtained for
different booster
momentum gain

$I_{\text{main}} = 374 \text{ A}$
 $XY_{\text{laser}} = 1.2 \text{ mm}$

Signal / Noise \leftrightarrow RMS \leftrightarrow Core emittance

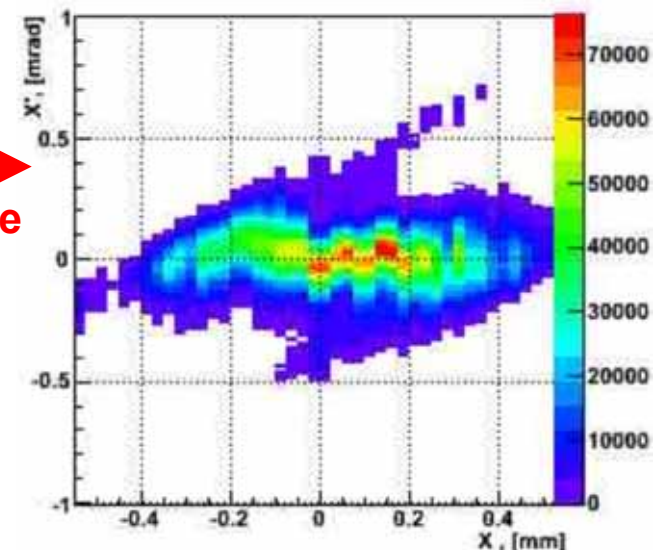
x - x' -phase space distribution for the best emittance measurement, purely reconstructed from subsequent beamlet measurements:

100 % of data



$\rightarrow \epsilon_n = 1.1$ mm mrad

Cut at **5% of max. amplitude**
(i.e. 6.5% of “charge”)
[reasons: by purpose or because of noise, gain, sensitivity, bit depth, ...]



$\rightarrow \epsilon_n = 0.69$ mm mrad

Reminder: This $\epsilon_n \neq 1.25$ mm mrad because the separately measured beam size at the slit position is NOT taken into account here.

\Rightarrow **projected emittance is reduced by 37 % !!**

ASTRA: - 5% in particles \rightarrow -38% in proj. emittance

For 95% RMS $\rightarrow \epsilon_{x,y,n} \approx 0.8$ mm mrad